Package: RelDists (via r-universe)

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Title Estimation for some Reliability Distributions

Version 1.0.2

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BugReports https://github.com/fhernanb/RelDists/issues

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`AddW` *The Additive Weibull family*

Description

The Additive Weibull distribution

Usage

```
AddW(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.
`nu.link`	defines the nu.link, with "log" link as the default for the nu parameter.
`tau.link`	defines the tau.link, with "log" link as the default for the tau parameter.

Details

Additive Weibull distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = (\mu\nu x^{\nu-1} + \sigma\tau x^{\tau-1}) \exp(-\mu x^{\nu} - \sigma x^{\tau}),$

for $x > 0$.

Value

Returns a gamlss.family object which can be used to fit a AddW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J. (2018). A reduced new modified Weibull distribution. Communications in Statistics-Theory and Methods, 47(10), 2297-2313.

Xie, M., & Lai, C. D. (1996). Reliability analysis using an additive Weibull model with bathtub-shaped failure rate function. Reliability Engineering & System Safety, 52(1), 87-93.

See Also

dAddW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
# Will not be run this example because high number is cycles
# is needed in order to get good estimates
## Not run:
y <- rAddW(n=100, mu=1.5, sigma=0.2, nu=3, tau=0.8)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family='AddW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))
exp(coef(mod, what='tau'))

## End(Not run)
```

```
# Example 2
# Generating random values under some model
# Will not be run this example because high number is cycles
# is needed in order to get good estimates
## Not run:
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(1.67 + -3 * x1)
sigma <- exp(0.69 - 2 * x2)
nu <- 3
tau <- 0.8
x <- rAddW(n=n, mu, sigma, nu, tau)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~1, family=AddW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))

## End(Not run)
```

BGE *The Beta Generalized Exponentiated family*

Description

The Beta Generalized Exponentiated family

Usage

```
BGE(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.
tau.link	defines the tau.link, with "log" link as the default for the tau parameter.

Details

The Beta Generalized Exponentiated distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = \frac{\nu\tau}{B(\mu,\sigma)} \exp(-\nu x)(1-\exp(-\nu x))^{\tau\mu-1}(1-(1-\exp(-\nu x))^{\tau})^{\sigma-1}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 0$ and $\tau > 0$.

Value

Returns a gamlss.family object which can be used to fit a BGE distribution in the `gamlss()` function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J. (2018). A reduced new modified Weibull distribution. Communications in Statistics-Theory and Methods, 47(10), 2297-2313.

Barreto-Souza, W., Santos, A. H., & Cordeiro, G. M. (2010). The beta generalized exponential distribution. Journal of statistical Computation and Simulation, 80(2), 159-172.

See Also

dBGE

Examples

```
# Generating some random values with
# known mu, sigma, nu and tau
y <- rBGE(n=100, mu = 1.5, sigma =1.7, nu=1, tau=1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family=BGE,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))
exp(coef(mod, what='tau'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(0.5 - x1)
sigma <- exp(0.8 - x2)
nu <- 1
tau <- 1
x <- rBGE(n=n, mu, sigma, nu, tau)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~1, family=BGE,
              control=gamlss.control(n.cyc=5000, trace=FALSE))
```

```
coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))
```

BS *The Birnbaum-Saunders family*

Description

The function `BS()` defines the Birnbaum-Saunders, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{x^{-3/2}(x+\mu)}{2\sigma\sqrt{2\pi\mu}} \exp\left(\frac{-1}{2\sigma^2}(\frac{x}{\mu}+\frac{\mu}{x}-2)\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization μ is the median of X, $E(X) = \mu(1+\sigma^2/2)$ and $Var(X) = (\mu\sigma)^2(1+5\sigma^2/4)$. The functions proposed here corresponds to the functions created by Roquim et al. (2021) with minor modifications to obtain correct log-likelihoods and random samples.

Value

Returns a gamlss.family object which can be used to fit a BS distribution in the `gamlss()` function.

References

Birnbaum, Z.W. and Saunders, S.C. (1969a). A new family of life distributions. J. Appl. Prob., 6, 319–327.

Roquim, F. V., Ramires, T. G., Nakamura, L. R., Righetto, A. J., Lima, R. R., & Gomes, R. A. (2021). Building flexible regression models: including the Birnbaum-Saunders distribution in the gamlss package. Semina: Ciencias Exatas e Tecnologicas, 42(2), 163-168.

See Also

dBS

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rBS(n=100, mu=0.75, sigma=1.3)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y as BS
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rBS(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=300)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS, data=dat)

summary(mod2)

# Example 3
# Fatigue life (T) measures in cycles (×10-3) of n 101
# aluminum coupons (specimens) of type 6061-T6.
# Taken from Leiva et al. (2006) page 37.
# https://journal.r-project.org/articles/RN-2006-033/RN-2006-033.pdf

y <- c(70, 90, 96, 97, 99, 100, 103, 104,
       104, 105, 107, 108, 108, 108, 109, 109,
       112, 112, 113, 114, 114, 114, 116, 119,
       120, 120, 120, 121, 121, 123, 124, 124,
       124, 124, 124, 128, 128, 129, 129, 130,
       130, 130, 131, 131, 131, 131, 131, 132,
       132, 132, 133, 134, 134, 134, 134, 134,
       136, 136, 137, 138, 138, 138, 139, 139,
       141, 141, 142, 142, 142, 142, 142, 142,
       144, 144, 145, 146, 148, 148, 149, 151,
```

```
       151, 152, 155, 156, 157, 157, 157, 157,
       158, 159, 162, 163, 163, 164, 166, 166,
       168, 170, 174, 196, 212)

mod3 <- gamlss(y~1, sigma.fo=~1, family=BS)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Example 4
# Aggregate payments by the insurer
# in thousand Skr (Swedish currency).
# Taken from Balakrishnan and Kundu (2019) page 65.
# https://onlinelibrary.wiley.com/doi/abs/10.1002/asmb.2348

y <- c(5014, 5855, 6486, 6540, 6656, 6656, 7212, 7541, 7558,
       7797, 8546, 9345, 11762, 12478, 13624, 14451,
       14940, 14963, 15092, 16203, 16229, 16730, 18027,
       18343, 19365, 21782, 24248, 29069, 34267, 38993)

y <- y/10000

mod4 <- gamlss(y~1, sigma.fo=~1, family=BS)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))
```

BS10 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P8 Based on the first Tweedie)*

Description

The function `BS10()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS10(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (representing τ).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (representing ω).

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `mu` represents τ and `sigma` represents ω) has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{\mu^2}\left[\frac{2x}{\mu^2} + \frac{\mu^2}{2x} - 2\right]\right) \frac{[2x+\mu^2]\sqrt{\sigma}}{2\mu^2\sqrt{x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{\mu^2}{2} + \frac{\mu^4}{8\sigma}$ and $Var(X) = \frac{\mu^6}{8\sigma} + \frac{5\mu^8}{64\sigma^2}$.

Value

Returns a `gamlss.family` object which can be used to fit a BS10 distribution in the `gamlss()` function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS10.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(12345)
y <- rBS10(n=100, mu=0.75, sigma=5)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS10)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
```

```
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS10
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(0.5 - 1.6 * x1)      # Aprox 0.75
  sigma <- exp(2.2 - 1.2 * x2)   # Aprox 5
  y <- rBS10(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS10, data=dat)

summary(mod2)
```

BS11 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P9 Based on the second Tweedie)*

Description

The function `BS11()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS11(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (representing β).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (representing ω).

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `mu` represents β and `sigma` represents ω) has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2\mu}\left[\frac{x}{\mu} + \frac{\mu}{x} - 2\right]\right) \frac{[x+\mu]\sqrt{\sigma}}{2\mu\sqrt{x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu + \frac{\mu^2}{2\sigma}$ and $Var(X) = \frac{\mu^3}{\sigma} + \frac{5\mu^4}{4\sigma^2}$.

Value

Returns a gamlss.family object which can be used to fit a BS11 distribution in the gamlss() function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS11.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rBS11(n=100, mu=1, sigma=12)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS11)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS11
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(0.5 - 1 * x1)      # Aprox 1
  sigma <- exp(1.9 + 1.2 * x2)   # Aprox 12
  y <- rBS11(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS11, data=dat)
```

```
summary(mod2)
```

BS12 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P10 Based on the third Tweedie)*

Description

The function `BS12()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS12(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (representing the scale β).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (representing the shape ψ).

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `mu` represents β and `sigma` represents ψ) has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2}\left[\frac{x}{\mu} + \frac{\mu}{x} - 2\right]\right) \frac{[x+\mu]\sqrt{\sigma}}{2\sqrt{\mu x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu + \frac{\mu}{2\sigma}$ and $Var(X) = \frac{\mu^2}{\sigma} + \frac{5\mu^2}{4\sigma^2}$.

Value

Returns a `gamlss.family` object which can be used to fit a BS12 distribution in the `gamlss()` function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS12.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(12345)
y <- rBS12(n=100, mu=1, sigma=30)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS12)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS12
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(0.5 - 1 * x1)      # Aprox 1
  sigma <- exp(2.2 + 2.4 * x2)   # Aprox 30
  y <- rBS12(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS12, data=dat)

summary(mod2)
```

BS13 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P11 Based on the fourth Tweedie)*

Description

The function `BS13()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS13(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter (representing the scale ω).
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter (representing the shape ψ).

Details

The Birnbaum-Saunders distribution with parameters mu and sigma (where mu represents ω and sigma represents ψ) has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2}\left[\frac{x\sigma}{\mu} + \frac{\mu}{x\sigma} - 2\right]\right) \frac{[x\sigma+\mu]}{2\sqrt{\mu x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{\mu}{\sigma} + \frac{\mu}{2\sigma^2}$ and $Var(X) = \frac{\mu^2}{\sigma^3} + \frac{5\mu^2}{4\sigma^4}$.

Value

Returns a gamlss.family object which can be used to fit a BS13 distribution in the gamlss() function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS13.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(123456)
y <- rBS13(n=500, mu=5, sigma=30)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS13,
               control=gamlss.control(n.cyc=300, trace=TRUE))

# Extracting the fitted values for mu and sigma
```

```
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS13
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.1 + 1.1 * x1)      # Aprox 5
  sigma <- exp(2.2 + 2.4 * x2)   # Aprox 30
  y <- rBS13(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS13, data=dat,
               control=gamlss.control(n.cyc=500, trace=TRUE))

summary(mod2)
```

BS2 *The Birnbaum-Saunders family - Santos-Neto et al. (2014)*

Description

The function `BS2()` defines the Birnbaum-Saunders, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS2(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{\exp(\sigma/2)\sqrt{\sigma+1}}{4\sqrt{\pi\mu}x^{3/2}}\left[x+\frac{\mu\sigma}{\sigma+1}\right]\exp\left(\frac{-\sigma}{4}\left(\frac{x(\sigma+1)}{\mu\sigma}+\frac{\mu\sigma}{x(\sigma+1)}\right)\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization $E(X) = \mu$ and $Var(X) = \frac{\mu^2(2\sigma+5)}{(\sigma+1)^2}$.

Value

Returns a gamlss.family object which can be used to fit a BS2 distribution in the `gamlss()` function.

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Barros, M. (2014). A reparameterized Birnbaum–Saunders distribution and its moments, estimation and applications. REVSTAT-Statistical Journal, 12(3), 247-272.

See Also

dBS2.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rBS2(n=50, mu=5, sigma=3)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS2)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS2
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rBS2(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS2, data=dat)

summary(mod2)

# Example 3
# Household expenditures for food in the United States (US) expressed
```

```
# in thousands of US dollars (M$)
# Santos-Neto et al. (2014) page 266.

y <- c(15.998, 16.652, 21.741, 7.431, 10.481, 13.548, 23.256, 17.976,
       14.161, 8.825, 14.184, 19.604, 13.728, 21.141, 17.446, 9.629,
       14.005, 9.160, 18.831, 7.641, 13.882, 9.670, 21.604, 10.866,
       28.980, 10.882, 18.561, 11.629, 18.067, 14.539, 19.192, 25.918,
       28.833, 15.869, 14.910, 9.550, 23.066, 14.751)

mod3 <- gamlss(y~1, sigma.fo=~1, family=BS2)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Example 4
# lifetimes of 6061-T6 aluminum coupons expressed in cycles (×10-3)
# at a maximum stress level of 3.1 psi (×104), until the failure to occur.
# Santos-Neto et al. (2014) page 267.

y <- c(70, 90, 96, 97, 99, 100, 103, 104, 104, 105, 107, 108, 108, 108, 109,
       109, 112, 112, 113, 114, 114, 114, 116, 119, 120, 120, 120, 121, 121,
       123, 124, 124, 124, 124, 124, 128, 128, 129, 129, 130, 130, 130, 131,
       131, 131, 131, 131, 132, 132, 132, 133, 134, 134, 134, 134, 134, 136,
       136, 137, 138, 138, 138, 139, 139, 141, 141, 142, 142, 142, 142, 142,
       142, 144, 144, 145, 146, 148, 148, 149, 151, 151, 152, 155, 156, 157,
       157, 157, 157, 158, 159, 162, 163, 163, 164, 166, 166, 168, 170, 174,
       196, 212)

mod4 <- gamlss(y~1, sigma.fo=~1, family=BS2)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))
```

BS3 *The Birnbaum-Saunders family - Bourguignon & Gallardo (2022)*

Description

The function `BS3()` defines the Birnbaum-Saunders, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS3(mu.link = "log", sigma.link = "logit")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "logit" link as the default for the sigma.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{(1-\sigma)y+\mu}{2\sqrt{2\pi\mu\sigma(1-\sigma)}y^{3/2}} \exp\left[\frac{-1}{2\sigma}\left(\frac{(1-\sigma)y}{\mu} + \frac{\mu}{(1-\sigma)y} - 2\right)\right]$

for $x > 0$, $\mu > 0$ and $0 < \sigma < 1$. In this parameterization $Mode(X) = \mu$ and $Var(X) = (\mu\sigma)^2(1 + 5\sigma^2/4)$.

Value

Returns a gamlss.family object which can be used to fit a BS3 distribution in the `gamlss()` function.

References

Bourguignon, M., & Gallardo, D. I. (2022). A new look at the Birnbaum–Saunders regression model. Applied Stochastic Models in Business and Industry, 38(6), 935-951.

See Also

dBS3.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rBS3(n=50, mu=2, sigma=0.2)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS3)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS3
## Not run:
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
```

```
  inv_logit <- function(x) 1 / (1 + exp(-x))
  sigma <- inv_logit(2 - 1.5 * x2)
  y <- rBS3(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS3, data=dat,
               control=gamlss.control(n.cyc=100))

summary(mod2)

## End(Not run)

# Example 3
# The response variable is the ratio between the average
# rent per acre planted with alfalfa and the corresponding
# average rent for other agricultural uses. The density of
# dairy cows (X2, number per square mile) is the explanatory variable.
library(alr4)
data("landrent")

landrent$ratio <- landrent$Y / landrent$X1

with(landrent, plot(x=X2, y=ratio))

mod3 <- gamlss(ratio~X2, sigma.fo=~X2,
               data=landrent, family=BS3)

summary(mod3)
logLik(mod3)
```

BS4 *The Birnbaum-Saunders family - Ahmed et al. (2008)*

Description

The function `BS4()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS4(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter.

Details

The Birnbaum-Saunders distribution with parameters mu and sigma has density given by

$$f(x|\mu,\sigma) = \frac{1}{2\sqrt{2\pi}}\left[\frac{\sigma}{x\sqrt{x}} + \frac{\mu}{\sqrt{x}}\right]\exp\left(-\frac{1}{2}\left[\frac{\sigma}{\sqrt{x}} - \mu\sqrt{x}\right]^2\right)$$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{\sigma\mu+1/2}{\mu^2}$ and $Var(X) = \frac{\sigma\mu+5/4}{\mu^4}$.

Value

Returns a gamlss.family object which can be used to fit a BS4 distribution in the gamlss() function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Ahmed, S. E., Budsaba, K., Lisawadi, S., & Volodin, A. (2008). Parametric estimation for the Birnbaum-Saunders lifetime distribution based on a new parametrization. Thailand Statistician, 6(2), 213-240.

See Also

dBS4.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(123)
y <- rBS4(n=50, mu=2, sigma=0.2)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS4)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model
```

```
# A function to simulate a data set with Y ~ BS4
## Not run:
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rBS4(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS4, data=dat,
               control=gamlss.control(n.cyc=100))

summary(mod2)

## End(Not run)

# Example 3
# Taken from Ahmed et al. (2008) on page 227
# The response variable is the fatigue
# life of 6061-T6 aluminum coupons.
## Not run:
y <- c(
    70, 90, 96, 97, 99, 100, 103, 104,
    104, 105, 107, 108, 108, 108, 109, 109,
    112, 112, 113, 114, 114, 114, 116, 119,
    120, 120, 120, 121, 121, 123, 124, 124,
    124, 124, 124, 128, 128, 129, 130, 130,
    130, 130, 131, 131, 131, 131, 131, 132,
    132, 132, 133, 134, 134, 134, 134, 134,
    136, 136, 137, 138, 138, 138, 139, 139,
    141, 141, 142, 142, 142, 142, 142, 142,
    144, 144, 145, 146, 148, 148, 149, 151,
    151, 152, 155, 156, 157, 157, 157, 157,
    158, 159, 162, 163, 163, 164, 166, 166,
    168, 170, 174, 196, 212
)

mod3 <- gamlss(y~1, family=BS4,
               control=gamlss.control(n.cyc=3000))

summary(mod3)
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

plot(density(y))
curve(dBS4(x, mu=0.5145121, sigma=67.81761),
      add=TRUE, col="tomato", lwd=2)
```

```
legend("topright", legend=c("Empirical", "Estimated"),
       col=c("black", "tomato"), lty=1)

## End(Not run)

# Example 4
# Taken from Ahmed et al. (2008) on page 228
# The response variable is the fatigue life in
# hours of 10 bearings of a certain type.
## Not run:
y <- c(152.7, 172.0, 172.5, 173.5, 193.0,
       204.7, 216.5, 234.9, 262.6, 422.6)

mod4 <- gamlss(y~1, family=BS4,
               control=gamlss.control(n.cyc=3000))

summary(mod4)
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))

## End(Not run)
```

BS5 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P3 Based on GLM)*

Description

The function `BS5()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS5(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter.

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `sigma` represents the precision parameter δ) has density given by

$f(x|\mu,\sigma) = \frac{\exp(\sigma/2)\sqrt{\sigma+1}}{4\sqrt{\pi\mu}x^{3/2}}\left[x+\frac{\sigma\mu}{\sigma+1}\right]\exp\left(-\frac{\sigma}{4}\left[\frac{x(\sigma+1)}{\sigma\mu}+\frac{\sigma\mu}{x(\sigma+1)}\right]\right)$

for $x>0$, $\mu>0$ and $\sigma>0$. In this parameterization, $E(X)=\mu$ and $Var(X)=\mu^2\left[\frac{2\sigma+5}{(\sigma+1)^2}\right]$.

Value

Returns a `gamlss.family` object which can be used to fit a BS5 distribution in the `gamlss()` function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS5.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(123)
y <- rBS5(n=50, mu=1, sigma=25)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS5)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS5
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.5 - 3 * x1)        # Aprox 1
  sigma <- exp(2.4 + 1.7 * x2)   # Aprox 25
  y <- rBS5(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS5, data=dat)
```

```
summary(mod2)
```

BS6 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P4 Based on the mean)*

Description

The function `BS6()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS6(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter.

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `mu` represents the true mean and `sigma` represents the shape parameter α) has density given by

$$f(x|\mu,\sigma) = \frac{\exp(1/\sigma^2)\sqrt{2+\sigma^2}}{4\sigma\sqrt{\pi\mu}x^{3/2}}\left[x+\frac{2\mu}{2+\sigma^2}\right]\exp\left(-\frac{1}{2\sigma^2}\left[\frac{\{2+\sigma^2\}x}{2\mu}+\frac{2\mu}{\{2+\sigma^2\}x}\right]\right)$$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu$ and $Var(X) = [\mu\sigma]^2\left[\frac{4+5\sigma^2}{(2+\sigma^2)^2}\right]$.

Value

Returns a `gamlss.family` object which can be used to fit a BS6 distribution in the `gamlss()` function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS6.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rBS6(n=50, mu=1, sigma=0.1)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS6)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS6
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.5 - 3 * x1)        # Aprox 1
  sigma <- exp(0.5 - 3.5 * x2)   # Aprox 0.1
  y <- rBS6(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS6, data=dat)

summary(mod2)
```

BS7 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P5 Based on the variance)*

Description

The function `BS7()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS7(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (representing the variance).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (representing the shape).

Details

The Birnbaum-Saunders distribution with parameters `mu` and `sigma` (where `mu` represents the true variance σ^2 and `sigma` represents the shape parameter α) has density given by

$$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2\mu^2}\left[\frac{\mu\sqrt{4+5\mu^2}}{2\sqrt{\sigma}x^{-1}} + \frac{2\sqrt{\sigma}\{x\mu\}^{-1}}{\sqrt{4+5\mu^2}} - 2\right]\right) \times \left[\frac{\{x\mu\}^{-1/2}\{4+5\mu^2\}^{1/4}}{2^{3/2}\sigma^{1/4}} + \frac{\sigma^{1/4}}{\{x\mu\}^{3/2}\sqrt{2}\{4+5\mu^2\}^{1/4}}\right]$$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{[2+\mu^2]\sqrt{\sigma}}{\mu\sqrt{4+5\mu^2}}$ and $Var(X) = \sigma$.

Value

Returns a `gamlss.family` object which can be used to fit a BS7 distribution in the `gamlss()` function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS7.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(12345)
y <- rBS7(n=100, mu=0.2, sigma=10)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS7,
               control=gamlss.control(n.cyc=1000))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
```

```
# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS7
## Not run:
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(0.6 - 4.4 * x1)      # Aprox 0.2
  sigma <- exp(1.6 + 1.5 * x2)   # Aprox 10
  y <- rBS7(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS7, data=dat,
               control=gamlss.control(n.cyc=1000))

summary(mod2)

## End(Not run)
```

BS8 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P6 Based on the variance 2)*

Description

The function `BS8()` defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
BS8(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (representing the variance).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (representing the shape).

Details

The Birnbaum-Saunders distribution with parameters mu and sigma (where mu represents the true variance σ^2 and sigma represents the shape parameter α) has density given by

$$f(x|\mu,\sigma) = \frac{\sqrt{\mu}}{2\sqrt{2\pi\sigma}}\left[\left\{\frac{1}{2x}\sqrt{\frac{5\sigma}{\mu(\mu-1)}}\right\}^{1/2} + \left\{\frac{1}{2x}\sqrt{\frac{5\sigma}{\mu(\mu-1)}}\right\}^{3/2}\right]\exp\left(-\frac{5}{8(\mu-1)}\left[\frac{2x\sqrt{\mu(\mu-1)}}{\sqrt{5\sigma}} + \frac{\sqrt{5\sigma}}{2+\sqrt{\mu(\mu-1)}} - 2\right]\right)$$

for $x > 0$, $\mu > 1$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{[2\mu+3]\sqrt{\sigma}}{\sqrt{20\mu(\mu-1)}}$ and $Var(X) = \sigma$.

Value

Returns a gamlss.family object which can be used to fit a BS8 distribution in the gamlss() function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS8.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma

set.seed(12345)
y <- rBS8(n=10, mu=1.1, sigma=10)

# Fitting the model using default link function
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS8,
               control=gamlss.control(n.cyc=1000))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Fitting again the model using our own link function.
# As mu > 1, we can use
#     link function:    g(mu) = log(mu - 1)
# inv link function: g-1(eta) = exp(eta) + 1

# The following function "log_1_to_inf" is defined with the informatio
```

```
# of the link and inv link functions:

## Not run:

log_1_to_inf <- function() {
  linkfun <- function(mu) { log(mu - 1) }
  linkinv <- function(eta) {
    thresh <- log(.Machine$double.xmax)
    eta <- pmin(thresh, pmax(eta, -700))
    1 + exp(eta)
  }
  mu.eta <- function(eta) {
    thresh <- log(.Machine$double.xmax)
    eta <- pmin(thresh, pmax(eta, -700))
    pmax(exp(eta), .Machine$double.eps)
  }
  valideta <- function(eta) { TRUE }
  link <- "log_1_to_inf"
  structure(list(linkfun = linkfun, linkinv = linkinv, mu.eta = mu.eta,
                 valideta = valideta, name = link), class = "link-gamlss")
}

mod99 <- gamlss(y~1, sigma.fo=~1,
                family=BS8(mu.link = log_1_to_inf()),
                control=gamlss.control(n.cyc=1000))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod99, what="mu")) + 1
exp(coef(mod99, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS8
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.6 - 2.4 * x1) + 1  # Aprox 2.45 with link function log(mu - 1)
  sigma <- exp(1.6 + 1.5 * x2)   # Aprox 10 with link function log(sigma)
  y <- rBS8(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=400)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS8(mu.link = log_1_to_inf()),
               data=dat,
               control=gamlss.control(n.cyc=100))

summary(mod2)
```

```
## End(Not run)
```

BS9 *The Birnbaum-Saunders family - Santos-Neto et al. (2012) (P7 based on the mean and a bounded variance)*

Description

The function BS9() defines the Birnbaum-Saunders distribution, a two-parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
BS9(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter (representing the variance).
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter (representing the shape).

Details

The Birnbaum-Saunders distribution with parameters mu and sigma (where mu represents the true variance σ^2 and sigma represents the shape parameter α) has density given by

$$f(x \mid \mu, \sigma) = \frac{\exp\left(\frac{1}{2(\sigma-1)}\right)(x\sigma + \mu)}{4\sqrt{\pi\sigma(\sigma-1)\mu}\, x^{3/2}} \exp\left[-\frac{1}{4(\sigma-1)}\left(\frac{x\sigma}{\mu} + \frac{\mu}{x\sigma}\right)\right]$$

for $x > 0$, $\mu > 0$ and $\sigma > 1$. In this parameterization, $E(X) = \mu$ and $Var(X) = \frac{\mu^2(\sigma-1)(5\sigma-3)}{\sigma^2}$.

Value

Returns a gamlss.family object which can be used to fit a BS9 distribution in the gamlss() function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

dBS9.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma

set.seed(12345)
y <- rBS9(n=300, mu=2, sigma=2.1)

# Fitting the model using default link function
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=BS9,
               control=gamlss.control(n.cyc=1000))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Fitting again the model using our own link function.
# As sigma > 1, we can use
# inv link function:    g-1(eta) = exp(eta) + 1
#     link function:    g(sigma) = log(sigma - 1)

# The following function "log_1_to_inf" is defined with the information
# of the link and inv link functions:

## Not run:

log_1_to_inf <- function() {
  linkfun <- function(mu) { log(mu - 1) }
  linkinv <- function(eta) {
    thresh <- log(.Machine$double.xmax)
    eta <- pmin(thresh, pmax(eta, -700))
    1 + exp(eta)
  }
  mu.eta <- function(eta) {
    thresh <- log(.Machine$double.xmax)
    eta <- pmin(thresh, pmax(eta, -700))
    pmax(exp(eta), .Machine$double.eps)
  }
  valideta <- function(eta) { TRUE }
  link <- "log_1_to_inf"
  structure(list(linkfun = linkfun, linkinv = linkinv, mu.eta = mu.eta,
                 valideta = valideta, name = link), class = "link-gamlss")
}

mod99 <- gamlss(y~1, sigma.fo=~1,
                family=BS9(sigma.link = log_1_to_inf()),
```

```
                control=gamlss.control(n.cyc=1000))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod99, what="mu"))
exp(coef(mod99, what="sigma")) + 1

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ BS9
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.6 - 2.4 * x1)          # Aprox 1.5 with link function log(mu)
  sigma <- exp(1.6 + 1.5 * x2) + 1   # Aprox 11.5 with link function log(sigma - 1)
  y <- rBS9(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=500)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=BS9(sigma.link = log_1_to_inf()),
               data=dat,
               control=gamlss.control(n.cyc=100))

summary(mod2)


## End(Not run)
```

BTL *The Beta Transformed Lomax distribution*

Description

The Beta Transformed Lomax family

Usage

```
BTL(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Beta Transformed Lomax distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\log \nu}{\nu - 1} \frac{\sigma}{\mu} \left(1 + \frac{x}{\mu}\right)^{-(\sigma+1)} \nu^{\left(1+\frac{x}{\mu}\right)^{-\sigma}}$,

for $\nu \neq 1$, and for $\nu = 1$:

$f(x) = \frac{\sigma}{\mu} \left(1 + \frac{x}{\mu}\right)^{-(\sigma+1)}$,

for $x \geq 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a BTL distribution in the gamlss() function.

Author(s)

Marieth Guillen, <mguillen@unal.edu.co>

References

Kottakkunnan, F. A New Generalization of Lomax Distribution: Estimation and Modelling for Medical Data. J Stat Theory Appl 25, 19 (2026). https://doi.org/10.1007/s44199-026-00171-0

See Also

dBTL

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rBTL(n=300, mu=0.75, sigma=1.3, nu=0.5)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, nu.fo =~1, family=BTL,
               control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
exp(coef(mod1, what="nu"))

# Example 2
# Generating random values under some model
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  x3 <- runif(n)
```

```
  mu <- exp(1.5 - 2.0 * x1)
  sigma <- exp(2.5 - 0.5 * x2)
  nu <- exp(-2.0 + 4.5 * x3)
  y <- rBTL(n, mu, sigma, nu)
  data.frame(y=y, x1=x1, x2=x2, x3=x3)
}

dat <- gendat(n=2000)

mod2 <- gamlss(y~x1, sigma.fo=~x2, nu.fo=~x3, family=BTL, data=dat,
               control=gamlss.control(n.cyc=3000, trace=FALSE))

summary(mod2)
coef(mod2, what="mu")
coef(mod2, what="sigma")
coef(mod2, what="nu")

# Example 3
# Fatigue life (T) measures in cycles (×10-3) of n 101
# aluminum coupons (specimens) of type 6061-T6.
# Taken from Leiva et al. (2006) page 37.
# https://journal.r-project.org/articles/RN-2006-033/RN-2006-033.pdf

y <- c(0.0251, 0.0886, 0.0891, 0.2501, 0.3113, 0.3451,
       0.4763, 0.5650, 0.5671, 0.6566, 0.6748, 0.6751,
       0.6753, 0.7696, 0.8375, 0.8391, 0.8425, 0.8645,
       0.8851, 0.9113, 0.9120, 0.9836, 1.0483, 1.0596,
       1.0773, 1.1733, 1.2570, 1.2766, 1.2985, 1.3211,
       1.3503, 1.3551, 1.4595, 1.4880, 1.5728, 1.5733,
       1.7083, 1.7263, 1.7460, 1.7630, 1.7746, 1.8275,
       1.8375, 1.8503, 1.8808, 1.8878, 1.8881, 1.9316,
       1.9558, 2.0048, 2.0408, 2.0903, 2.1093, 2.1330,
       2.2100, 2.2460, 2.2878, 2.3203, 2.3470, 2.3513,
       2.4951, 2.5260, 2.9911, 3.0256, 3.2678, 3.4045,
       3.4846, 3.7433, 3.7455, 3.9143, 4.8073, 5.4005,
       5.4435, 5.5295, 6.5541, 9.0960)

mod3 <- gamlss(y~1, family=BTL,
               control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))
exp(coef(mod3, what="nu"))
```

---

checklink *Set the Right Link Function for Specified Parameter and Distribution*

Description

This function is used within the distribution family specification of a GAMLSS model to define the right link for each of the parameters of the distribution. This function should not be called by the user unless he/she specify a new distribution family or wishes to change existing link functions in the parameters.

Usage

```
checklink(which.link = NULL, which.dist = NULL, link = NULL, link.List = NULL)
```

Arguments

`which.link`	which parameter link e.g. `which.link="mu.link"`
`which.dist`	which distribution family e.g. `which.dist="Cole.Green"`
`link`	a repetition of `which.link` e.g. `link=substitute(mu.link)`
`link.List`	what link function are required e.g. `link.List=c("inverse", "log", "identity")`

Details

This function is the same `checklink` fuction from gamlss.dist package.

Value

Defines the right link for each parameter.

CJ2 *The two-parameter Chris-Jerry distribution family*

Description

The function `CJ2()` defines The two-parameter Chris-Jerry distribution, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
CJ2(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The two-parameter Chris-Jerry distribution with parameters `mu` and `sigma` has density given by

$f(x;\sigma,\mu) = \frac{\mu^2}{\sigma\mu+2}(\sigma+\mu x^2)e^{-\mu x}; \quad x>0, \quad \mu>0, \quad \sigma>0$

Note: In this implementation we changed the original parameters θ for μ and λ for σ we did it to implement this distribution within gamlss framework.

Value

Returns a gamlss.family object which can be used to fit a CJ2 distribution in the `gamlss()` function.

Author(s)

Manuel Gutierrez Tangarife, <mgutierrezta@unal.edu.co>

References

Chinedu, Eberechukwu Q., et al. "New lifetime distribution with applications to single acceptance sampling plan and scenarios of increasing hazard rates" Symmetry 15.10 (2023): 188.

See Also

dCJ2

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rCJ2(n=500, mu=1, sigma=1.5)

# Fitting the model
require(gamlss)

mod1 <- gamlss(y~1, sigma.fo=~1, family=CJ2,
               control=gamlss.control(n.cyc=5000, trace=TRUE))

# Extracting the fitted values for mu, sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model
gendat <- function(n) {
  x1 <- runif(n, min=0, max=5)
  x2 <- runif(n, min=0, max=5)
  mu <- exp(-0.2 + 1.5 * x1)
  sigma <- exp(1 - 0.7 * x2)
  y <- rCJ2(n=n, mu, sigma)
  data.frame(y=y, x1=x1, x2=x2)
```

```
}

set.seed(123)
datos <- gendat(n=500)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=CJ2, data=datos,
               control=gamlss.control(n.cyc=5000, trace=TRUE))

summary(mod2)
```

CS2e *The Cosine Sine Exponential family*

Description

The Cosine Sine Exponential family

Usage

```
CS2e(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Cosine Sine Exponential distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\pi\sigma\mu \exp(\frac{-x}{\nu})}{2\nu[(\mu \sin(\frac{\pi}{2} \exp(\frac{-x}{\nu})) + \sigma \cos(\frac{\pi}{2} \exp(\frac{-x}{\nu}))]^2}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a CS2e distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Chesneau, C., Bakouch, H. S., & Hussain, T. (2019). A new class of probability distributions via cosine and sine functions with applications. Communications in Statistics-Simulation and Computation, 48(8), 2287-2300.

See Also

dCS2e

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rCS2e(n=100, mu = 0.1, sigma =1, nu=0.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='CS2e',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.45, max=0.55)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(0.2 - x1)
sigma <- exp(0.8 - x2)
nu <- 0.5
x <- rCS2e(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1,family=CS2e,
              control=gamlss.control(n.cyc=50000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

---

dAddW *The Additive Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Additive Weibull distribution with parameters mu, sigma, nu and tau.

Usage

```
dAddW(x, mu, sigma, nu, tau, log = FALSE)

pAddW(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qAddW(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

rAddW(n, mu, sigma, nu, tau)

hAddW(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	shape parameter.
tau	shape parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

Additive Weibull Distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = (\mu\nu x^{\nu-1} + \sigma\tau x^{\tau-1}) \exp(-\mu x^{\nu} - \sigma x^{\tau}),$

for $x > 0$.

Value

dAddW gives the density, pAddW gives the distribution function, qAddW gives the quantile function, rAddW generates random deviates and hAddW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Xie, M., & Lai, C. D. (1996). Reliability analysis using an additive Weibull model with bathtub-shaped failure rate function. Reliability Engineering & System Safety, 52(1), 87-93.

See Also

AddW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dAddW(x, mu=1.5, sigma=0.5, nu=3, tau=0.8), from=0.0001, to=2,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pAddW(x, mu=1.5, sigma=0.5, nu=3, tau=0.8),
      from=0.0001, to=2, col="red", las=1, ylab="F(x)")
curve(pAddW(x, mu=1.5, sigma=0.5, nu=3, tau=0.8, lower.tail=FALSE),
      from=0.0001, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qAddW(p, mu=1.5, sigma=0.2, nu=3, tau=0.8), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pAddW(x, mu=1.5, sigma=0.2, nu=3, tau=0.8),
      from=0, add=TRUE, col="red")

## The random function
hist(rAddW(n=10000, mu=1.5, sigma=0.2, nu=3, tau=0.8), freq=FALSE,
     xlab="x", las=1, main="")
curve(dAddW(x, mu=1.5, sigma=0.2, nu=3, tau=0.8),
      from=0.09, to=5, add=TRUE, col="red")

## The Hazard function
curve(hAddW(x, mu=1.5, sigma=0.2, nu=3, tau=0.8), from=0.001, to=1,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dBGE *The Beta Generalized Exponentiated distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Beta Generalized Exponentiated distribution with parameters mu, sigma, nu and tau.

Usage

```
dBGE(x, mu, sigma, nu, tau, log = FALSE)
```

```
pBGE(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qBGE(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

rBGE(n, mu, sigma, nu, tau)

hBGE(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
tau	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Beta Generalized Exponentiated Distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = \frac{\nu\tau}{B(\mu,\sigma)} \exp(-\nu x)(1-\exp(-\nu x))^{\tau\mu-1}(1-(1-\exp(-\nu x))^{\tau})^{\sigma-1}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 0$ and $\tau > 0$.

Value

dBGE gives the density, pBGE gives the distribution function, qBGE gives the quantile function, rBGE generates random deviates and hBGE gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Barreto-Souza, W., Santos, A. H., & Cordeiro, G. M. (2010). The beta generalized exponential distribution. Journal of statistical Computation and Simulation, 80(2), 159-172.

See Also

BGE

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dBGE(x, mu = 1.5, sigma =1.7, nu=1, tau=1), from = 0, to = 3,
      col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pBGE(x, mu = 1.5, sigma =1.7, nu=1, tau=1), from = 0, to = 6,
      ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pBGE(x, mu = 1.5, sigma =1.7, nu=1, tau=1, lower.tail = FALSE),
      from = 0, to = 6, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qBGE(p = p, mu = 1.5, sigma =1.7, nu=1, tau=1), y = p,
     xlab = "Quantile", las = 1, ylab = "Probability")
curve(pBGE(x, mu = (1/4), sigma =1, nu=1, tau=2), from = 0, add = TRUE,
      col = "red")

## The random function
hist(rBGE(1000, mu = 1.5, sigma =1.7, nu=1, tau=1), freq = FALSE, xlab = "x",
     ylim = c(0, 1), las = 1, main = "")
curve(dBGE(x, mu = 1.5, sigma =1.7, nu=1, tau=1),  from = 0, add = TRUE,
      col = "red", ylim = c(0, 0.5))

## The Hazard function(
par(mfrow=c(1,1))
curve(hBGE(x, mu = 0.9, sigma =0.5, nu=1, tau=1), from = 0, to = 2,
      col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dBS *The Birnbaum-Saunders distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS(x, mu = 1, sigma = 1, log = FALSE)

pBS(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

qBS(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)
```

```
rBS(n, mu = 1, sigma = 1)

hBS(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{x^{-3/2}(x+\mu)}{2\sigma\sqrt{2\pi\mu}} \exp\left(\frac{-1}{2\sigma^2}(\frac{x}{\mu} + \frac{\mu}{x} - 2)\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization μ is the median of X, $E(X) = \mu(1 + \sigma^2/2)$ and $Var(X) = (\mu\sigma)^2(1 + 5\sigma^2/4)$. The functions proposed here corresponds to the functions created by Roquim et al. (2021) with minor modifications to obtain correct log-likelihoods and random samples.

Value

dBS gives the density, pBS gives the distribution function, qBS gives the quantile function, rBS generates random deviates and hBS gives the hazard function.

References

Birnbaum, Z.W. and Saunders, S.C. (1969a). A new family of life distributions. J. Appl. Prob., 6, 319–327.

Roquim, F. V., Ramires, T. G., Nakamura, L. R., Righetto, A. J., Lima, R. R., & Gomes, R. A. (2021). Building flexible regression models: including the Birnbaum-Saunders distribution in the gamlss package. Semina: Ciencias Exatas e Tecnologicas, 42(2), 163-168.

See Also

BS.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS(x, mu=0.5, sigma=0.5),
      from=0.001, to=5,
      ylim=c(0, 2),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dBS(x, mu=1.5, sigma=0.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=0.5",
                            "mu=1.0, sigma=0.5",
                            "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


curve(dBS(x, mu=0.5, sigma=1),
      from=0.001, to=5,
      ylim=c(0, 1.5),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS(x, mu=1, sigma=1),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dBS(x, mu=1.5, sigma=1),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=1",
                            "mu=1.0, sigma=1",
                            "mu=1.5, sigma=1"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


curve(dBS(x, mu=0.5, sigma=1.5),
      from=0.001, to=8,
      ylim=c(0, 2),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS(x, mu=1, sigma=1.5),
      col="tomato",
      lwd=2,
```

```
      add=TRUE)
curve(dBS(x, mu=1.5, sigma=1.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=1.5",
                            "mu=1.0, sigma=1.5",
                            "mu=1.5, sigma=1.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS(x, mu=0.5, sigma=0.5),
      from=0.001, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pBS(x, mu=1.5, sigma=0.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.5, sigma=0.5",
                               "mu=1.0, sigma=0.5",
                               "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)
curve(pBS(x, mu=0.5, sigma=0.5, lower.tail=FALSE),
      from=0.001, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS(x, mu=1, sigma=0.5, lower.tail=FALSE),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pBS(x, mu=1.5, sigma=0.5, lower.tail=FALSE),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=0.5",
                            "mu=1.0, sigma=0.5",
                            "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS(p, mu=2.3, sigma=1.7), y=p, xlab="Quantile",
```

```
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS(x, mu=2.3, sigma=1.7),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS(n=10000, mu=20, sigma=0.5)
hist(x, freq=FALSE)
curve(dBS(x, mu=20, sigma=0.5), from=0, to=100,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS(x, mu=20, sigma=0.5), from=0.001, to=100,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS10 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P8 Based on the first Tweedie)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters mu and sigma.

Usage

```
dBS10(x, mu = 1, sigma = 0.5, log = FALSE)

pBS10(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS10(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS10(n, mu = 1, sigma = 0.5)

hBS10(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing τ (mu > 0).
sigma	parameter representing ω (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{\mu^2}\left[\frac{2x}{\mu^2} + \frac{\mu^2}{2x} - 2\right]\right) \frac{[2x+\mu^2]\sqrt{\sigma}}{2\mu^2\sqrt{x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{\mu^2}{2} + \frac{\mu^4}{8\sigma}$ and $Var(X) = \frac{\mu^6}{8\sigma} + \frac{5\mu^8}{64\sigma^2}$.

Value

`dBS10` gives the density, `pBS10` gives the distribution function, `qBS10` gives the quantile function, `rBS10` generates random deviates and `hBS10` gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS10.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS10(x, mu=0.75, sigma=5),
      from=0.001, to=1.5,
      ylim=c(0, 6.2),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS10(x, mu=1.15, sigma=5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.75, sigma=5",
                            "mu=1.15, sigma=5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS10(x, mu=0.75, sigma=5),
      from=0.00001, to=1.5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS10(x, mu=1.15, sigma=5),
```

```
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.75, sigma=5",
                               "mu=1.15, sigma=5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS10(p, mu=0.75, sigma=5), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS10(x, mu=0.75, sigma=5),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS10(n=10000, mu=0.75, sigma=5)
hist(x, freq=FALSE)
curve(dBS10(x, mu=0.75, sigma=5),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS10(x, mu=0.75, sigma=5), from=0.001, to=2,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS11 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P9 Based on the second Tweedie)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS11(x, mu = 1, sigma = 0.5, log = FALSE)

pBS11(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS11(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS11(n, mu = 1, sigma = 0.5)

hBS11(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing β (mu > 0).
sigma	parameter representing ω (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2\mu}\left[\frac{x}{\mu} + \frac{\mu}{x} - 2\right]\right) \frac{[x+\mu]\sqrt{\sigma}}{2\mu\sqrt{x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu + \frac{\mu^2}{2\sigma}$ and $Var(X) = \frac{\mu^3}{\sigma} + \frac{5\mu^4}{4\sigma^2}$.

Value

dBS11 gives the density, pBS11 gives the distribution function, qBS11 gives the quantile function, rBS11 generates random deviates and hBS11 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS11.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS11(x, mu=1, sigma=12),
      from=0.001, to=2.5,
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS11(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=1, sigma=12",
```

```
                              "mu=1, sigma=0.5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS11(x, mu=1, sigma=12),
      from=0.00001, to=8,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS11(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=1, sigma=12",
                               "mu=1, sigma=0.5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS11(p, mu=1, sigma=12), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS11(x, mu=1, sigma=12),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS11(n=10000, mu=1, sigma=12)
hist(x, freq=FALSE)
curve(dBS11(x, mu=1, sigma=12),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS11(x, mu=1, sigma=12), from=0.001, to=4,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS12 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P10 Based on the third Tweedie)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS12(x, mu = 1, sigma = 0.5, log = FALSE)

pBS12(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS12(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS12(n, mu = 1, sigma = 0.5)

hBS12(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing β (mu > 0).
sigma	parameter representing ψ (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2}\left[\frac{x}{\mu} + \frac{\mu}{x} - 2\right]\right) \frac{[x+\mu]\sqrt{\sigma}}{2\sqrt{\mu x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu + \frac{\mu}{2\sigma}$ and $Var(X) = \frac{\mu^2}{\sigma} + \frac{5\mu^2}{4\sigma^2}$.

Value

dBS12 gives the density, pBS12 gives the distribution function, qBS12 gives the quantile function, rBS12 generates random deviates and hBS12 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS12.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS12(x, mu=1, sigma=30),
      from=0.001, to=2.5,
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS12(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=1, sigma=30",
                            "mu=1, sigma=0.5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS12(x, mu=1, sigma=30),
      from=0.00001, to=8,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS12(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=1, sigma=30",
                               "mu=1, sigma=0.5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS12(p, mu=1, sigma=30), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS12(x, mu=1, sigma=30),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS12(n=10000, mu=1, sigma=30)
hist(x, freq=FALSE)
curve(dBS12(x, mu=1, sigma=30),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS12(x, mu=1, sigma=30), from=0.001, to=4,
      col="tomato", ylab="Hazard function", las=1)
```

dBS13 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P11 Based on the fourth Tweedie)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters mu and sigma.

Usage

```
dBS13(x, mu = 1, sigma = 0.5, log = FALSE)

pBS13(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS13(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS13(n, mu = 1, sigma = 0.5)

hBS13(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing ω (mu > 0).
sigma	parameter representing ψ (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\sigma}{2}\left[\frac{x\sigma}{\mu} + \frac{\mu}{x\sigma} - 2\right]\right) \frac{[x\sigma+\mu]}{2\sqrt{\mu x^3}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{\mu}{\sigma} + \frac{\mu}{2\sigma^2}$ and $Var(X) = \frac{\mu^2}{\sigma^3} + \frac{5\mu^2}{4\sigma^4}$.

Value

dBS13 gives the density, pBS13 gives the distribution function, qBS13 gives the quantile function, rBS13 generates random deviates and hBS13 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS13.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS13(x, mu=5, sigma=30),
      from=0.001, to=0.8,
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS13(x, mu=5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=5, sigma=30",
                            "mu=5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS13(x, mu=5, sigma=30),
      from=0.00001, to=2,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS13(x, mu=5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=5, sigma=30",
                               "mu=5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS13(p, mu=5, sigma=30), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS13(x, mu=5, sigma=30),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS13(n=10000, mu=5, sigma=30)
```

```
hist(x, freq=FALSE)
curve(dBS13(x, mu=5, sigma=30),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS13(x, mu=5, sigma=30), from=0.001, to=1,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS2 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2014)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS2(x, mu = 1, sigma = 1, log = FALSE)

pBS2(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

qBS2(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rBS2(n, mu = 1, sigma = 1)

hBS2(x, mu, sigma)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter.
`sigma`	parameter.
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
`p`	vector of probabilities.
`n`	number of observations.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$f(x) = \frac{\exp(\sigma/2)\sqrt{\sigma+1}}{4\sqrt{\pi\mu}x^{3/2}}\left[x + \frac{\mu\sigma}{\sigma+1}\right]\exp\left(\frac{-\sigma}{4}\left(\frac{x(\sigma+1)}{\mu\sigma} + \frac{\mu\sigma}{x(\sigma+1)}\right)\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization $E(X) = \mu$ and $Var(X) = (\mu\sigma)^2(1+5\sigma^2/4)$. The functions proposed here corresponds to the parameterization proposed by Santos-Neto et al. (2014).

Value

dBS2 gives the density, pBS2 gives the distribution function, qBS2 gives the quantile function, rBS2 generates random deviates and hBS2 gives the hazard function.

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Barros, M. (2014). A reparameterized Birnbaum–Saunders distribution and its moments, estimation and applications. REVSTAT-Statistical Journal, 12(3), 247-272.

See Also

BS2.

Examples

```
#Example 1
#Plotting the mass function for different parameter values
curve(dBS2(x, mu=1.0, sigma=100),
      from=0.001, to=5,
      ylim=c(0, 3),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS2(x, mu=1.5, sigma=100),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dBS2(x, mu=2.0, sigma=100),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=1.0, sigma=100",
                            "mu=1.5, sigma=100",
                            "mu=2.0, sigma=100"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


curve(dBS2(x, mu=1, sigma=2),
      from=0.001, to=2,
      ylim=c(0, 1.1),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS2(x, mu=1, sigma=5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dBS2(x, mu=1, sigma=10),
      col="seagreen",
      lwd=2,
      add=TRUE)
```

```
legend("topright", legend=c("mu=1, sigma=2",
                            "mu=1, sigma=5",
                            "mu=1, sigma=10"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS2(x, mu=0.5, sigma=0.5),
      from=0.001, to=15,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS2(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pBS2(x, mu=1.5, sigma=0.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.5, sigma=0.5",
                               "mu=1.0, sigma=0.5",
                               "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS2(p, mu=2.3, sigma=1.7), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS2(x, mu=2.3, sigma=1.7),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS2(n=10000, mu=2.5, sigma=100)
hist(x, freq=FALSE)
curve(dBS2(x, mu=2.5, sigma=100), from=0, to=10,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS2(x, mu=20, sigma=0.5), from=0.001, to=100,
      col="tomato", ylab="Hazard function", las=1)
```

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters mu and sigma.

Usage

```
dBS3(x, mu = 1, sigma = 0.5, log = FALSE)

pBS3(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS3(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS3(n, mu = 1, sigma = 0.5)

hBS3(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x) = \frac{\exp(\sigma/2)\sqrt{\sigma+1}}{4\sqrt{\pi\mu x^{3/2}}}\left[x + \frac{\mu\sigma}{\sigma+1}\right]\exp\left(\frac{-\sigma}{4}\left(\frac{x(\sigma+1)}{\mu\sigma} + \frac{\mu\sigma}{x(\sigma+1)}\right)\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization $E(X) = \mu$ and $Var(X) = (\mu\sigma)^2(1+5\sigma^2/4)$. The functions proposed here corresponds to the parameterization proposed by Santos-Neto et al. (2014).

Value

dBS3 gives the density, pBS3 gives the distribution function, qBS3 gives the quantile function, rBS3 generates random deviates and hBS3 gives the hazard function.

References

Bourguignon, M., & Gallardo, D. I. (2022). A new look at the Birnbaum–Saunders regression model. Applied Stochastic Models in Business and Industry, 38(6), 935-951.

See Also

BS3.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS3(x, mu=2, sigma=0.2),
      from=0.001, to=10,
      ylim=c(0, 0.4),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS3(x, mu=2, sigma=0.4),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=2, sigma=0.2",
                            "mu=2, sigma=0.4"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS3(x, mu=2, sigma=0.2),
      from=0.00001, to=10,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS3(x, mu=2, sigma=0.4),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2, sigma=0.2",
                               "mu=2, sigma=0.4"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS3(p, mu=2, sigma=0.2), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS3(x, mu=2, sigma=0.2),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS3(n=10000, mu=2, sigma=0.2)
hist(x, freq=FALSE)
curve(dBS3(x, mu=2, sigma=0.2), from=0, to=10,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS3(x, mu=2, sigma=0.2), from=0.001, to=4,
      col="tomato", ylab="Hazard function", las=1)
```

dBS4 *The Birnbaum-Saunders distribution - Ahmed et al. (2008)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters mu and sigma.

Usage

```
dBS4(x, mu = 1, sigma = 0.5, log = FALSE)

pBS4(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS4(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS4(n, mu = 1, sigma = 0.5)

hBS4(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter (mu > 0).
sigma	parameter (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$$f(x|\mu,\sigma) = \frac{1}{2\sqrt{2\pi}}\left[\frac{\sigma}{x\sqrt{x}} + \frac{\mu}{\sqrt{x}}\right]\exp\left(-\frac{1}{2}\left[\frac{\sigma}{\sqrt{x}} - \mu\sqrt{x}\right]^2\right)$$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization $E(X) = \frac{\sigma\mu+1/2}{\mu^2}$ and $Var(X) = \frac{\sigma\mu+5/4}{\mu^4}$.

Value

dBS4 gives the density, pBS4 gives the distribution function, qBS4 gives the quantile function, rBS4 generates random deviates and hBS4 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Ahmed, S. E., Budsaba, K., Lisawadi, S., & Volodin, A. (2008). Parametric estimation for the Birnbaum-Saunders lifetime distribution based on a new parametrization. Thailand Statistician, 6(2), 213-240.

See Also

BS4.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS4(x, mu=2, sigma=30),
      from=0.001, to=40,
      ylim=c(0, 0.20),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS4(x, mu=1, sigma=20),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=2, sigma=30",
                            "mu=1, sigma=20"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS4(x, mu=2, sigma=30),
      from=0.00001, to=40,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS4(x, mu=1, sigma=20),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2, sigma=30",
                               "mu=1, sigma=20"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS4(p, mu=2, sigma=30), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
```

```
curve(pBS4(x, mu=2, sigma=30),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS4(n=10000, mu=2, sigma=30)
hist(x, freq=FALSE)
curve(dBS4(x, mu=2, sigma=30), from=0, to=30,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS4(x, mu=2, sigma=30), from=0.001, to=40,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS5 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P3 Based on GLM)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS5(x, mu = 1, sigma = 0.5, log = FALSE)

pBS5(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS5(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS5(n, mu = 1, sigma = 0.5)

hBS5(x, mu, sigma)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter (`mu > 0`).
`sigma`	precision parameter δ (`sigma > 0`).
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
`p`	vector of probabilities.
`n`	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{\exp(\sigma/2)\sqrt{\sigma+1}}{4\sqrt{\pi\mu}x^{3/2}}\left[x+\frac{\sigma\mu}{\sigma+1}\right]\exp\left(-\frac{\sigma}{4}\left[\frac{x(\sigma+1)}{\sigma\mu}+\frac{\sigma\mu}{x(\sigma+1)}\right]\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization $E(X) = \mu$ and $Var(X) = \mu^2\left[\frac{2\sigma+5}{(\sigma+1)^2}\right]$.

Value

dBS5 gives the density, pBS5 gives the distribution function, qBS5 gives the quantile function, rBS5 generates random deviates and hBS5 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS5.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS5(x, mu=1, sigma=2),
      from=0.001, to=2,
      ylim=c(0, 1.5),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS5(x, mu=1, sigma=25),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=1, sigma=2",
                            "mu=1, sigma=25"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS5(x, mu=1, sigma=2),
      from=0.00001, to=6,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
```

```
curve(pBS5(x, mu=1, sigma=25),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=1, sigma=2",
                               "mu=1, sigma=25"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS5(p, mu=1, sigma=2), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS5(x, mu=1, sigma=2),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS5(n=10000, mu=1, sigma=25)
hist(x, freq=FALSE)
curve(dBS5(x, mu=1, sigma=25),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS5(x, mu=1, sigma=25), from=0.001, to=6,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS6 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P4 Based on the mean)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS6(x, mu = 1, sigma = 0.5, log = FALSE)

pBS6(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS6(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS6(n, mu = 1, sigma = 0.5)

hBS6(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing the mean (mu > 0).
sigma	parameter representing the shape α (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \frac{\exp(1/\sigma^2)\sqrt{2+\sigma^2}}{4\sigma\sqrt{\pi\mu}x^{3/2}}\left[x+\frac{2\mu}{2+\sigma^2}\right]\exp\left(-\frac{1}{2\sigma^2}\left[\frac{\{2+\sigma^2\}x}{2\mu}+\frac{2\mu}{\{2+\sigma^2\}x}\right]\right)$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \mu$ and $Var(X) = [\mu\sigma]^2\left[\frac{4+5\sigma^2}{(2+\sigma^2)^2}\right]$.

Value

dBS6 gives the density, pBS6 gives the distribution function, qBS6 gives the quantile function, rBS6 generates random deviates and hBS6 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS6.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS6(x, mu=2, sigma=0.1),
      from=0.001, to=3,
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS6(x, mu=2, sigma=0.75),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=2, sigma=0.1",
```

```
                              "mu=2, sigma=0.75"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS6(x, mu=2, sigma=0.1),
      from=0.00001, to=6,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS6(x, mu=2, sigma=0.75),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2, sigma=0.1",
                               "mu=2, sigma=0.75"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS6(p, mu=1, sigma=2), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS6(x, mu=1, sigma=2),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS6(n=10000, mu=2, sigma=0.1)
hist(x, freq=FALSE)
curve(dBS6(x, mu=2, sigma=0.1),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS6(x, mu=2, sigma=0.1), from=0.001, to=6,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS7 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P5 Based on the variance)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS7(x, mu = 0.5, sigma = 10, log = FALSE)

pBS7(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS7(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS7(n, mu = 1, sigma = 0.5)

hBS7(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing the shape (mu > 0).
sigma	parameter representing the variance (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$$f(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2\mu^2}\left[\frac{\mu\sqrt{4+5\mu^2}}{2\sqrt{\sigma}x^{-1}} + \frac{2\sqrt{\sigma}\{x\mu\}^{-1}}{\sqrt{4+5\mu^2}} - 2\right]\right) \times \left[\frac{\{x\mu\}^{-1/2}\{4+5\mu^2\}^{1/4}}{2^{3/2}\sigma^{1/4}} + \frac{\sigma^{1/4}}{\{x\mu\}^{3/2}\sqrt{2}\{4+5\mu^2\}^{1/4}}\right]$$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{[2+\mu^2]\sqrt{\sigma}}{\mu\sqrt{4+5\mu^2}}$ and $Var(X) = \sigma$.

Value

dBS7 gives the density, pBS7 gives the distribution function, qBS7 gives the quantile function, rBS7 generates random deviates and hBS7 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS7.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS7(x, mu=0.1, sigma=10),
      from=0.001, to=40,
      ylim=c(0, 0.20),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS7(x, mu=0.5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.1, sigma=10",
                            "mu=0.5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS7(x, mu=0.1, sigma=10),
      from=0.00001, to=50,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS7(x, mu=0.5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.1, sigma=10",
                               "mu=0.5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS7(p, mu=0.1, sigma=10), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS7(x, mu=0.1, sigma=10),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS7(n=10000, mu=0.1, sigma=10)
hist(x, freq=FALSE)
curve(dBS7(x, mu=0.1, sigma=10),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS7(x, mu=0.1, sigma=10), from=0.001, to=60,
      col="tomato", ylab="Hazard function", las=1)
```

dBS8 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P6 Based on the variance 2)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters mu and sigma.

Usage

```
dBS8(x, mu = 0.5, sigma = 10, log = FALSE)

pBS8(q, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

qBS8(p, mu = 1, sigma = 0.5, lower.tail = TRUE, log.p = FALSE)

rBS8(n, mu = 1, sigma = 0.5)

hBS8(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing the shape (mu > 0).
sigma	parameter representing the variance (sigma > 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Birnbaum-Saunders with parameters mu and sigma has density given by

$$f(x|\mu,\sigma) = \frac{\sqrt{\mu}}{2\sqrt{2\pi\sigma}}\left[\left\{\frac{1}{2x}\sqrt{\frac{5\sigma}{\mu(\mu-1)}}\right\}^{1/2} + \left\{\frac{1}{2x}\sqrt{\frac{5\sigma}{\mu(\mu-1)}}\right\}^{3/2}\right]\exp\left(-\frac{5}{8(\mu-1)}\left[\frac{2x\sqrt{\mu(\mu-1)}}{\sqrt{5\sigma}} + \frac{\sqrt{5\sigma}}{2+\sqrt{\mu(\mu-1)}} - 2\right]\right)$$

for $x > 0$, $\mu > 1$ and $\sigma > 0$. In this parameterization, $E(X) = \frac{[2\mu+3]\sqrt{\sigma}}{\sqrt{20\mu(\mu-1)}}$ and $Var(X) = \sigma$.

Value

dBS8 gives the density, pBS8 gives the distribution function, qBS8 gives the quantile function, rBS8 generates random deviates and hBS8 gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS8.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS8(x, mu=1.05, sigma=10),
      from=0.001, to=25,
      ylim=c(0, 0.25),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS8(x, mu=1.5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=1.05, sigma=10",
                            "mu=1.5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS8(x, mu=1.5, sigma=10),
      from=0.00001, to=30,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS8(x, mu=2.5, sigma=10),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=1.5, sigma=10",
                               "mu=2.5, sigma=10"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS8(p, mu=1.5, sigma=10), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS8(x, mu=1.5, sigma=10),
```

```
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS8(n=10000, mu=1.5, sigma=10)
hist(x, freq=FALSE)
curve(dBS8(x, mu=1.5, sigma=10),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS8(x, mu=1.5, sigma=10), from=0.001, to=60,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBS9 *The Birnbaum-Saunders distribution - Santos-Neto et al. (2012) (P7 based on the mean and a bounded variance)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Birnbaum-Saunders distribution with parameters `mu` and `sigma`.

Usage

```
dBS9(x, mu = 0.5, sigma = 10, log = FALSE)

pBS9(q, mu = 1, sigma = 2, lower.tail = TRUE, log.p = FALSE)

qBS9(p, mu = 1, sigma = 2, lower.tail = TRUE, log.p = FALSE)

rBS9(n, mu = 1, sigma = 2)

hBS9(x, mu, sigma)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter representing the shape (`mu` > `0`).
`sigma`	parameter representing the variance (`sigma` > `0`).
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
`p`	vector of probabilities.
`n`	number of observations.

Details

The Birnbaum-Saunders with parameters `mu` and `sigma` has density given by

$$f(x \mid \mu, \sigma) = \frac{\exp\left(\frac{1}{2(\sigma-1)}\right)(x\sigma + \mu)}{4\sqrt{\pi\sigma(\sigma-1)\mu}\, x^{3/2}} \exp\left[-\frac{1}{4(\sigma-1)}\left(\frac{x\sigma}{\mu} + \frac{\mu}{x\sigma}\right)\right]$$

for $x > 0$, $\mu > 0$ and $\sigma > 1$. In this parameterization, $E(X) = \mu$ and $Var(X) = \frac{\mu^2(\sigma-1)(5\sigma-3)}{\sigma^2}$.

Value

`dBS9` gives the density, `pBS9` gives the distribution function, `qBS9` gives the quantile function, `rBS9` generates random deviates and `hBS9` gives the hazard function.

Author(s)

David Villegas Ceballos, <david.villegas1@udea.edu.co>

References

Santos-Neto, M., Cysneiros, F. J. A., Leiva, V., & Ahmed, S. E. (2012). On new parameterizations of the Birnbaum-Saunders distribution. Pakistan Journal of Statistics, 28(1), 1-26.

See Also

BS9.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dBS9(x, mu=2, sigma=1.1),
      from=0.001, to=3,
      ylim=c(0, 1.0),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dBS9(x, mu=2, sigma=2.1),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=2, sigma=1.1",
                            "mu=2, sigma=2.1"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBS9(x, mu=2, sigma=1.1),
      from=0.00001, to=7,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
```

```
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBS9(x, mu=2, sigma=2.1),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2, sigma=1.1",
                               "mu=2, sigma=2.1"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qBS9(p, mu=2, sigma=1.1), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBS9(x, mu=2, sigma=1.1),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBS9(n=10000, mu=2, sigma=1.1)
hist(x, freq=FALSE)
curve(dBS9(x, mu=2, sigma=1.1),
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hBS9(x, mu=2, sigma=1.1), from=0.001, to=60,
      col="tomato", ylab="Hazard function", las=1)
```

---

dBTL *The Beta Transformed Lomax distribution*

Description

Density, distribution function, quantile function and random generation for the Beta Transformed Lomax distribution with parameters `mu`, `sigma` and `nu`.

Usage

```
dBTL(x, mu = 1.5, sigma = 1.5, nu = 2, log = FALSE)

pBTL(q, mu = 1.5, sigma = 1.5, nu = 2, lower.tail = TRUE, log.p = FALSE)

qBTL(p, mu = 1.5, sigma = 1.5, nu = 2, lower.tail = TRUE, log.p = FALSE)

rBTL(n, mu = 1.5, sigma = 1.5, nu = 2)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Beta Transformed Lomax distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\log \nu}{\nu - 1} \frac{\sigma}{\mu} \left(1 + \frac{x}{\mu}\right)^{-(\sigma+1)} \nu^{\left(1+\frac{x}{\mu}\right)^{-\sigma}}$,

for $\nu \neq 1$, and for $\nu = 1$:

$f(x) = \frac{\sigma}{\mu} \left(1 + \frac{x}{\mu}\right)^{-(\sigma+1)}$,

for $x \geq 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dBTL gives the density, pBTL gives the distribution function, qBTL gives the quantile function and rBTL generates random deviates.

Author(s)

Marieth Guillen, <mguillen@unal.edu.co>

References

Kottakkunnan, F. A New Generalization of Lomax Distribution: Estimation and Modelling for Medical Data. J Stat Theory Appl 25, 19 (2026). https://doi.org/10.1007/s44199-026-00171-0

See Also

BTL.

Examples

```
# Example 1
# Plotting the density function for different parameter values
curve(dBTL(x, sigma=0.1, mu=0.1, nu=0.01),
      ylim=c(0, 1.5),
      from=0, to=1.5, col="cadetblue3",
      las=1, ylab="f(x)")
curve(dBTL(x, sigma=0.25, mu=0.1, nu=0.01),
```

```
      add=TRUE, col= "purple")
curve(dBTL(x, sigma=0.5, mu=0.1, nu=0.01),
      add=TRUE, col="goldenrod")
curve(dBTL(x, sigma=0.75, mu=0.1, nu=0.01),
      add=TRUE, col="tomato")
curve(dBTL(x, sigma=0.95, mu=0.1, nu=0.01),
      add=TRUE, col="blue")
legend("topright", col=c("cadetblue3", "purple", "goldenrod", "tomato", "blue"),
       lty=1, bty="n", legend=c("sigma=0.1, mu=0.1, nu=0.01",
                                "sigma=0.25, mu=0.1, nu=0.01",
                                "sigma=0.5, mu=0.1, nu=0.01",
                                "sigma=0.75, mu=0.1, nu=0.01",
                                "sigma=0.95, mu=0.1, nu=0.01"))

curve(dBTL(x, sigma=1.1, mu=0.1, nu=0.01),
      ylim=c(0, 7),
      from=0, to=1.5, col="cadetblue3",
      las=1, ylab="f(x)")
curve(dBTL(x, sigma=1.5, mu=0.1, nu=0.01),
      add=TRUE, col= "purple")
curve(dBTL(x, sigma=2, mu=0.1, nu=0.01),
      add=TRUE, col="goldenrod")
curve(dBTL(x, sigma=2.5, mu=0.1, nu=0.01),
      add=TRUE, col="tomato")
curve(dBTL(x, sigma=3, mu=0.1, nu=0.01),
      add=TRUE, col="blue")
legend("topright", col=c("cadetblue3", "purple", "goldenrod", "tomato", "blue"),
       lty=1, bty="n", legend=c("sigma=1.1, mu=0.1, nu=0.01",
                                "sigma=1.5, mu=0.1, nu=0.01",
                                "sigma=2, mu=0.1, nu=0.01",
                                "sigma=2.5, mu=0.1, nu=0.01",
                                "sigma=3, mu=0.1, nu=0.01"))

# Example 2
# Checking if the cumulative curves converge to 1
curve(pBTL(x, sigma=0.95, mu=0.1, nu=1.2),
      from=0, to=6,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBTL(x, sigma=1.5, mu=0.1, nu=1.2),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pBTL(x, sigma=2.5, mu=0.1, nu=1.2),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("sigma=0.95, mu=0.1, nu=1.2",
                               "sigma=1.5, mu=0.1, nu=1.2",
                               "sigma=2.5, mu=0.1, nu=1.2"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)
```

```
curve(pBTL(x, sigma=0.95, mu=0.1, nu=1.2, lower.tail=FALSE),
      from=0, to=6,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pBTL(x, sigma=1.5, mu=0.1, nu=1.2, lower.tail=FALSE),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pBTL(x, sigma=2.5, mu=0.1, nu=1.2, lower.tail=FALSE),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("sigma=0.95, mu=0.1, nu=1.2",
                            "sigma=1.5, mu=0.1, nu=1.2",
                            "sigma=2.5, mu=0.1, nu=1.2"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.9, length.out=100)
plot(x=qBTL(p, mu=2.5, sigma=1.5, nu=0.5), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pBTL(q=x, mu=2.5, sigma=1.5, nu=0.5),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rBTL(n=1000, mu=0.5, sigma=3, nu=1.5)
hist(x, freq=FALSE)
curve(dBTL(x, mu=0.5, sigma=3, nu=1.5), from=0,
      add=TRUE, col="tomato", lwd=2)
```

---

dCJ2 *The two-parameter Chris-Jerry distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the two-parameter Chris-Jerry distribution with parameters `mu` and `sigma`.

Usage

```
dCJ2(x, mu, sigma, log = FALSE)

pCJ2(q, mu, sigma, log.p = FALSE, lower.tail = TRUE)

qCJ2(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)
```

```
rCJ2(n, mu, sigma)

hCJ2(x, mu, sigma, log = FALSE)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The two-parameter Chris-Jerry distribution with parameters mu and sigma has density given by

$f(x;\sigma,\mu) = \frac{\mu^2}{\sigma\mu+2}(\sigma+\mu x^2)e^{-\mu x}; \quad x>0, \quad \mu>0, \quad \sigma>0$

Note: In this implementation we changed the original parameters θ for μ and λ for σ, we did it to implement this distribution within gamlss framework.

Value

dCJ2 gives the density, pCJ2 gives the distribution function, qCJ2 gives the quantile function, rCJ2 generates random deviates and hCJ2 gives the hazard function.

Author(s)

Manuel Gutierrez Tangarife, <mgutierrezta@unal.edu.co>

References

Chinedu, Eberechukwu Q., et al. "New lifetime distribution with applications to single acceptance sampling plan and scenarios of increasing hazard rates" Symmetry 15.10 (2023): 188.

See Also

CJ2

Examples

```
# Example 1
# Plotting the density function for different parameter values
curve(dCJ2(x, mu=3.5, sigma=0.01),
      from=0.0001, to=5,
      ylim=c(0, 1),
      col="red", lwd=2,
```

```
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dCJ2(x, mu=2, sigma=0.05),
      col="green",
      lwd=2,
      add=TRUE)
curve(dCJ2(x, mu=1.5, sigma=0.01),
      col="blue",
      lwd=2,
      add=TRUE)
curve(dCJ2(x, mu=2.5, sigma=0.01),
      col="lightblue",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=3.5, sigma=0.01",
                            "mu=2, sigma=0.05",
                            "mu=1.5, sigma=0.01",
                            "mu=2.5, sigma=0.1"),
       col=c( "red", "green","blue","lightblue"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pCJ2(x, mu=2.7, sigma=0.1),
      from=0.0001, to=5,
      ylim=c(0, 1),
      col="red", lwd=2,
      main="Cumulative function",
      xlab="x", ylab="f(x)")
curve(pCJ2(x, mu=2.3, sigma=0.5),
      col="green",
      lwd=2,
      add=TRUE)
curve(pCJ2(x, mu=2.8, sigma=0.2),
      col="blue",
      lwd=2,
      add=TRUE)
curve(pCJ2(x, mu=3.8, sigma=0.3),
      col="lightblue",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2.75, sigma=0.1",
                            "mu=2.3, sigma=0.5",
                            "mu=2.8, sigma=0.2",
                            "mu=3.8, sigma=0.3"),
       col=c( "red", "green","blue","lightblue"), lwd=2, cex=0.6)

# Example 3
# Checking the quantile function
p <- seq(from=0.0001, to=0.99999, length.out=100)
plot(x=qCJ2(p, mu=2.3, sigma=1.7), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pCJ2(x, mu=2.3, sigma=1.7),
      from=0.0001, add=TRUE, col="red", lwd=2.5)
```

```
# Example 4
# Comparing the random generator output with
# the theoretical probabilities
x <- rCJ2(n=10000, mu=1.5, sigma=2.5)
hist(x, freq=FALSE)
curve(dCJ2(x, mu=1.5, sigma=2.5), from=0.001, to=8,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hCJ2(x, mu=0.85, sigma=0.15),
      from=0.0001, to=5,
      ylim=c(0, 1),
      col="red", lwd=2,
      main="Hazard function",
      xlab="x", ylab="f(x)")
curve(hCJ2(x, mu=1, sigma=0.05),
      col="green",
      lwd=2,
      add=TRUE)
curve(hCJ2(x, mu=0.9, sigma=0.1),
      col="blue",
      lwd=2,
      add=TRUE)
curve(hCJ2(x, mu=1.15, sigma=0.1),
      col="lightblue",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.85, sigma=0.15",
                               "mu=1, sigma=0.05",
                               "mu=0.9, sigma=0.1",
                               "mu=1.15, sigma=0.1"),
       col=c( "red", "green","blue","lightblue"), lwd=2, cex=0.5)
```

---

dCS2e *The Cosine Sine Exponential distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Cosine Sine Exponential distribution with parameters mu, sigma and nu.

Usage

```
dCS2e(x, mu, sigma, nu, log = FALSE)

pCS2e(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qCS2e(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)
```

```
rCS2e(n, mu, sigma, nu)

hCS2e(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Cosine Sine Exponential Distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\pi\sigma\mu \exp(\frac{-x}{\nu})}{2\nu[(\mu \sin(\frac{\pi}{2}\exp(\frac{-x}{\nu}))+\sigma\cos(\frac{\pi}{2}\exp(\frac{-x}{\nu}))]^2}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dCS2e gives the density, pCS2e gives the distribution function, qCS2e gives the quantile function, rCS2e generates random deviates and hCS2e gives the hazard function.

Author(s)

Juan Pablo Ramirez

References

Chesneau, C., Bakouch, H. S., & Hussain, T. (2019). A new class of probability distributions via cosine and sine functions with applications. Communications in Statistics-Simulation and Computation, 48(8), 2287-2300.

See Also

CS2e

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
par(mfrow=c(1,1))
curve(dCS2e(x, mu=1, sigma=0.1, nu =0.1), from=0, to=1,
      ylim=c(0, 3), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pCS2e(x, mu=1, sigma=0.1, nu =0.1),
      from=0, to=1,  col="red", las=1, ylab="F(x)")
curve(pCS2e(x, mu=1, sigma=0.1, nu =0.1, lower.tail=FALSE),
      from=0, to=1, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qCS2e(p, mu=0.1, sigma=1, nu=0.1), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pCS2e(x, mu=0.1, sigma=1, nu=0.1), from=0, add=TRUE, col="red")

## The random function
hist(rCS2e(n=10000, mu=0.1, sigma=1, nu=0.1), freq=FALSE,
     xlab="x", las=1, main="")
curve(dCS2e(x, mu=0.1, sigma=1, nu=0.1), from=0, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hCS2e(x, mu=1, sigma=0.1, nu =0.1), from=0, to=1, ylim=c(0, 10),
      col=2, ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dEEG *The Extended Exponential Geometric distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Extended Exponential Geometric distribution with parameters `mu` and `sigma`.

Usage

```
dEEG(x, mu, sigma, log = FALSE)

pEEG(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qEEG(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)
```

```
rEEG(n, mu, sigma)

hEEG(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Extended Exponential Geometric distribution with parameters mu, and sigmahas density given by

$f(x) = \mu\sigma \exp(-\mu x)(1 - (1 - \sigma)\exp(-\mu x))^{-2},$

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

Value

dEEG gives the density, pEEG gives the distribution function, qEEG gives the quantile function, rEEG generates random deviates and hEEG gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Adamidis, K., Dimitrakopoulou, T., & Loukas, S. (2005). On an extension of the exponential-geometric distribution. Statistics & probability letters, 73(3), 259-269.

See Also

EEG

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
par(mfrow=c(1,1))
curve(dEEG(x, mu = 1, sigma =3), from = 0, to = 10,
      col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pEEG(x, mu = 1, sigma =3), from = 0, to = 10,
      ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pEEG(x, mu = 1, sigma =3, lower.tail = FALSE),
      from = 0, to = 6, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qEEG(p = p, mu = 1, sigma =0.5), y = p,
     xlab = "Quantile", las = 1, ylab = "Probability")
curve(pEEG(x, mu = 1, sigma =0.5), from = 0, add = TRUE,
      col = "red")

## The random function
hist(rEEG(1000, mu = 1, sigma =1), freq = FALSE, xlab = "x",
     ylim = c(0, 0.9), las = 1, main = "")
curve(dEEG(x, mu = 1, sigma =1),  from = 0, add = TRUE,
      col = "red", ylim = c(0, 0.8))

## The Hazard function
par(mfrow=c(1,1))
curve(hEEG(x, mu = 1, sigma =0.5), from = 0, to = 2,
      col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dEGG *The four parameter Exponentiated Generalized Gamma distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the four parameter Exponentiated Generalized Gamma distribution with parameters `mu`, `sigma`, `nu` and `tau`.

Usage

```
dEGG(x, mu, sigma, nu, tau, log = FALSE)

pEGG(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)
```

```
qEGG(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

rEGG(n, mu, sigma, nu, tau)

hEGG(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
tau	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

Four-Parameter Exponentiated Generalized Gamma distribution with parameters mu, sigma, nu and tau has density given by

$$f(x) = \frac{\nu\sigma}{\mu\Gamma(\tau)}\left(\frac{x}{\mu}\right)^{\sigma\tau-1}\exp\left\{-\left(\frac{x}{\mu}\right)^{\sigma}\right\}\left\{\gamma_1\left(\tau,\left(\frac{x}{\mu}\right)^{\sigma}\right)\right\}^{\nu-1},$$

for $x > 0$.

Value

dEGG gives the density, pEGG gives the distribution function, qEGG gives the quantile function, rEGG generates random deviates and hEGG gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Cordeiro, G. M., Ortega, E. M., & Silva, G. O. (2011). The exponentiated generalized gamma distribution with application to lifetime data. Journal of statistical computation and simulation, 81(7), 827-842.

See Also

EGG

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dEGG(x, mu=0.1, sigma=0.8, nu=10, tau=1.5), from=0.000001, to=1.5, ylim=c(0, 2.5),
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pEGG(x, mu=0.1, sigma=0.8, nu=10, tau=1.5),
      from=0.000001, to=1.5, col="red", las=1, ylab="F(x)")
curve(pEGG(x, mu=0.1, sigma=0.8, nu=10, tau=1.5, lower.tail=FALSE),
      from=0.000001, to=1.5, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qEGG(p, mu=0.1, sigma=0.8, nu=10, tau=1.5), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pEGG(x, mu=0.1, sigma=0.8, nu=10, tau=1.5),
      from=0.00001, add=TRUE, col="red")

## The random function
hist(rEGG(n=100, mu=0.1, sigma=0.8, nu=10, tau=1.5), freq=FALSE,
     xlab="x", las=1, main="")
curve(dEGG(x, mu=0.1, sigma=0.8, nu=10, tau=1.5),
      from=0.0001, to=2, add=TRUE, col="red")

## The Hazard function
curve(hEGG(x,  mu=0.1, sigma=0.8, nu=10, tau=1.5), from=0.0001, to=1.5,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dEMWEx *The Exponentiated Modified Weibull Extension distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Exponentiated Modifien Weibull Extension distribution with parameters `mu`, `sigma`, `nu` and `tau`.

Usage

```
dEMWEx(x, mu, sigma, nu, tau, log = FALSE)

pEMWEx(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qEMWEx(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)
```

```
rEMWEx(n, mu, sigma, nu, tau)

hEMWEx(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
tau	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Exponentiated Modified Weibull Extension Distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = \nu\sigma\tau(\frac{x}{\mu})^{\sigma-1}\exp((\frac{x}{\mu})^{\sigma} + \nu\mu(1-\exp((\frac{x}{\mu})^{\sigma})))(1-\exp(\nu\mu(1-\exp((\frac{x}{\mu})^{\sigma}))))^{\tau-1}$,

for $x > 0$, $\nu > 0$, $\mu > 0$, $\sigma > 0$ and $\tau > 0$.

Value

dEMWEx gives the density, pEMWEx gives the distribution function, qEMWEx gives the quantile function, rEMWEx generates random deviates and hEMWEx gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Sarhan, A. M., & Apaloo, J. (2013). Exponentiated modified Weibull extension distribution. Reliability Engineering & System Safety, 112, 137-144.

See Also

EMWEx

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dEMWEx(x, mu = 49.046, sigma =3.148, nu=0.00005, tau=0.1), from=0, to=100,
      col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pEMWEx(x, mu = (1/4), sigma =1, nu=1, tau=2), from = 0, to = 1,
      ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pEMWEx(x, mu = (1/4), sigma =1, nu=1, tau=2, lower.tail = FALSE),
      from = 0, to = 1, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qEMWEx(p = p, mu = 49.046, sigma =3.148, nu=0.00005, tau=0.1), y = p,
     xlab = "Quantile", las = 1, ylab = "Probability")
curve(pEMWEx(x, mu = 49.046, sigma =3.148, nu=0.00005, tau=0.1), from = 0, add = TRUE,
      col = "red")

## The random function
hist(rEMWEx(1000, mu = (1/4), sigma =1, nu=1, tau=2), freq = FALSE, xlab = "x",
     las = 1, main = "")
curve(dEMWEx(x, mu = (1/4), sigma =1, nu=1, tau=2),  from = 0, add = TRUE,
      col = "red", ylim = c(0, 0.5))

## The Hazard function(
par(mfrow=c(1,1))
curve(hEMWEx(x, mu = 49.046, sigma =3.148, nu=0.00005, tau=0.1), from = 0, to = 80,
      col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dEOFNH *The Extended Odd Frechet-Nadarajah-Haghighi*

Description

Density, distribution function, quantile function, random generation and hazard function for the Extended Odd Fr?chet-Nadarajah-Haghighi distribution with parameters mu, sigma, nu and tau.

Usage

```
dEOFNH(x, mu, sigma, nu, tau, log = FALSE)

pEOFNH(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qEOFNH(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)
```

```
rEOFNH(n, mu, sigma, nu, tau)

hEOFNH(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
tau	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

Tthe Extended Odd Frechet-Nadarajah-Haghighi mu, sigma, nu and tau has density given by

$f(x) = \frac{\mu\sigma\nu\tau(1+\nu x)^{\sigma-1}e^{(1-(1+\nu x)^{\sigma})}[1-(1-e^{(1-(1+\nu x)^{\sigma})})^{\mu}]^{\tau-1}}{(1-e^{(1-(1+\nu x)^{\sigma})})^{\mu\tau+1}} e^{-[(1-e^{(1-(1+\nu x)^{\sigma})})^{-\mu}-1]^{\tau}},$

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 0$ and $\tau > 0$.

Value

dEOFNH gives the density, pEOFNH gives the distribution function, qEOFNH gives the quantile function, rEOFNH generates random numbers and hEOFNH gives the hazard function.

Author(s)

Helber Santiago Padilla, <hspadillar@unal.edu.co>

References

Nasiru, S. (2018). Extended Odd Fréchet-G Family of Distributions Journal of Probability and Statistics, 2018(1), 2931326.

See Also

EOFNH

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

##The probability density function
par(mfrow=c(1, 1))

curve(dEOFNH(x, mu=18.5, sigma=5.1, nu=0.1, tau=0.1),
      from=0, to=10, ylim=c(0, 0.25),
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pEOFNH(x,mu=18.5, sigma=5.1, nu=0.1, tau=0.1), from = 0, to = 10,
ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pEOFNH(x, mu=18.5, sigma=5.1, nu=0.1, tau=0.1, lower.tail = FALSE),
from = 0, to = 10, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

##The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qEOFNH(p, mu=18.5, sigma=5.1, nu=0.1, tau=0.1), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pEOFNH(x, mu=18.5, sigma=5.1, nu=0.1, tau=0.1), from=0, add=TRUE, col="red")

##The random function
hist(rEOFNH(n=10000, mu=18.5, sigma=5.1, nu=0.1, tau=0.1), freq=FALSE,
     xlab="x", las=1, main="")
curve(dEOFNH(x, mu=18.5, sigma=5.1, nu=0.1, tau=0.1), from=0, add=TRUE, col="red", ylim=c(0,1.25))

##The Hazard function
par(mfrow=c(1,1))
curve(hEOFNH(x, mu=18.5, sigma=5.1, nu=0.1, tau=0.1), from=0, to=10, ylim=c(0, 1),
     col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dEW *The Exponentiated Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the exponentiated Weibull distribution with parameters mu, sigma and nu.

Usage

```
dEW(x, mu, sigma, nu, log = FALSE)

pEW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)
```

```
qEW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rEW(n, mu, sigma, nu)

hEW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	scale parameter.
sigma, nu	shape parameters.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Exponentiated Weibull Distribution with parameters mu, sigma and nu has density given by

$f(x) = \nu\mu\sigma x^{\sigma-1}\exp(-\mu x^{\sigma})(1-\exp(-\mu x^{\sigma}))^{\nu-1}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dEW gives the density, pEW gives the distribution function, qEW gives the quantile function, rEW generates random deviates and hEW gives the hazard function.

See Also

EW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dEW(x, mu=2, sigma=1.5, nu=0.5), from=0, to=2,
      ylim=c(0, 2.5), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pEW(x, mu=2, sigma=1.5, nu=0.5),
      from=0, to=2,  col="red", las=1, ylab="F(x)")
curve(pEW(x, mu=2, sigma=1.5, nu=0.5, lower.tail=FALSE),
      from=0, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
```

```
plot(x=qEW(p, mu=2, sigma=1.5, nu=0.5), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pEW(x, mu=2, sigma=1.5, nu=0.5), from=0, add=TRUE, col="red")

## The random function
hist(rEW(n=10000, mu=2, sigma=1.5, nu=0.5), freq=FALSE,
     xlab="x", las=1, main="")
curve(dEW(x, mu=2, sigma=1.5, nu=0.5), from=0, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hEW(x, mu=2, sigma=1.5, nu=0.5), from=0, to=2, ylim=c(0, 7),
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dEXL *The exponentiated XLindley distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the exponentiated XLindley distribution with parameters mu and sigma.

Usage

```
dEXL(x, mu, sigma, log = FALSE)

pEXL(q, mu, sigma, log.p = FALSE, lower.tail = TRUE)

qEXL(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rEXL(n, mu, sigma)

hEXL(x, mu, sigma, log = FALSE)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The exponentiated XLindley with parameters `mu` and `sigma` has density given by

$f(x) = \frac{\sigma\mu^2(2+\mu+x)\exp(-\mu x)}{(1+\mu)^2}\left[1-\left(1+\frac{\mu x}{(1+\mu)^2}\right)\exp(-\mu x)\right]^{\sigma-1}$

for $x \geq 0$, $\mu \geq 0$ and $\sigma \geq 0$.

Note: In this implementation we changed the original parameters δ for μ and α for σ, we did it to implement this distribution within gamlss framework.

Value

`dEXL` gives the density, `pEXL` gives the distribution function, `qEXL` gives the quantile function, `rEXL` generates random deviates and `hEXL` gives the hazard function.

Author(s)

Manuel Gutierrez Tangarife, <mgutierrezta@unal.edu.co>

References

Alomair, A. M., Ahmed, M., Tariq, S., Ahsan-ul-Haq, M., & Talib, J. (2024). An exponentiated XLindley distribution with properties, inference and applications. Heliyon, 10(3).

See Also

EXL.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dEXL(x, mu=0.5, sigma=0.5),
      from=0, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dEXL(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dEXL(x, mu=1.5, sigma=0.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=0.5",
                            "mu=1.0, sigma=0.5",
                            "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)
```

```
curve(dEXL(x, mu=0.5, sigma=1),
      from=0, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dEXL(x, mu=1, sigma=1),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dEXL(x, mu=1.5, sigma=1),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=1",
                            "mu=1.0, sigma=1",
                            "mu=1.5, sigma=1"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


curve(dEXL(x, mu=0.5, sigma=1.5),
      from=0., to=8,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dEXL(x, mu=1, sigma=1.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dEXL(x, mu=1.5, sigma=1.5),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=1.5",
                            "mu=1.0, sigma=1.5",
                            "mu=1.5, sigma=1.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1
curve(pEXL(x, mu=0.5, sigma=0.5),
      from=0, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="f(x)")
curve(pEXL(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pEXL(x, mu=1.5, sigma=0.5),
      col="seagreen",
```

```
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.5, sigma=0.5",
                               "mu=1.0, sigma=0.5",
                               "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)


# Example 3
# The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qEXL(p, mu=2.3, sigma=1.7), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pEXL(x, mu=2.3, sigma=1.7),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Comparing quantile, density and cumulative
p <- c(0.25, 0.5, 0.75)
quantile <- qEXL(p=p, mu=2.3, sigma=1.7)

for(i in quantile){
  print(integrate(dEXL, lower=0, upper=i, mu=2.3, sigma=1.7))
}

pEXL(q=quantile, mu=2.3, sigma=1.7)

# Example 4
# The random function
x <- rEXL(n=10000, mu=1.5, sigma=2.5)
hist(x, freq=FALSE)
curve(dEXL(x, mu=1.5, sigma=2.5), from=0, to=20,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hEXL(x, mu=1.5, sigma=2), from=0.001, to=4,
      col="tomato", ylab="Hazard function", las=1)
```

---

dExW *The Extended Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Extended Weibull distribution with parameters `mu`, `sigma` and `nu`.

Usage

```
dExW(x, mu, sigma, nu, log = FALSE)
```

```
pExW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qExW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rExW(n, mu, sigma, nu)

hExW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Extended Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu x^{\sigma-1} exp(-\mu x^{\sigma})}{[1-(1-\nu)exp(-\mu x^{\sigma})]^2}$,

for $x > 0$.

Value

dExW gives the density, pExW gives the distribution function, qExW gives the quantile function, rExW generates random deviates and hExW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Zhang, T., & Xie, M. (2007). Failure data analysis with extended Weibull distribution. Communications in Statistics—Simulation and Computation, 36(3), 579-592.

See Also

ExW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dExW(x, mu=0.3, sigma=2, nu=0.05), from=0.0001, to=2,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pExW(x, mu=0.3, sigma=2, nu=0.05),
      from=0.0001, to=2, col="red", las=1, ylab="F(x)")
curve(pExW(x, mu=0.3, sigma=2, nu=0.05, lower.tail=FALSE),
      from=0.0001, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qExW(p, mu=0.3, sigma=2, nu=0.05), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pExW(x, mu=0.3, sigma=2, nu=0.05),
      from=0, add=TRUE, col="red")

## The random function
hist(rExW(n=10000, mu=0.3, sigma=2, nu=0.05), freq=FALSE,
     xlab="x", ylim=c(0, 2), las=1, main="")
curve(dExW(x, mu=0.3, sigma=2, nu=0.05),
      from=0.001, to=4, add=TRUE, col="red")

## The Hazard function
curve(hExW(x, mu=0.3, sigma=2, nu=0.05), from=0.001, to=4,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dExWALD *The Ex-Wald distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Ex-Wald distribution with parameter μ, σ and ν.

Usage

```
dExWALD(x, mu = 1.5, sigma = 1.5, nu = 2, log = FALSE)

pExWALD(q, mu = 1.5, sigma = 1.5, nu = 2, lower.tail = TRUE, log.p = FALSE)

qExWALD(p, mu = 1.5, sigma = 1.5, nu = 2)

rExWALD(n, mu = 1.5, sigma = 1.5, nu = 2)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
nu	vector of the nu parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of random values to return.

Details

The Wald distribution with parameters μ, σ and ν has density given by

$f(x|\mu,\sigma,\nu) = \frac{1}{\nu}\exp(\frac{-x}{\nu} + \sigma(\mu - k))F_W(x|k,\sigma)$ for $k \geq 0$

$f(x|\mu,\sigma,\nu) = \frac{1}{\nu}\exp\left(\frac{-(\sigma-\mu)^2}{2x}\right) Re\left(w(k'\sqrt{x/2} + \frac{\sigma i}{\sqrt{2x}})\right)$ for $k < 0$

where $k = \sqrt{\mu^2 - \frac{2}{\nu}}$, $k' = \sqrt{\frac{2}{\nu} - \mu^2}$ and F_W corresponds to the cumulative function of the Wald distribution.

More details about those expressions can be found on page 680 from Heathcote (2004).

Value

dExWALD gives the density, pExWALD gives the distribution function, qExWALD gives the quantile function, rExWALD generates random deviates.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Schwarz, W. (2001). The ex-Wald distribution as a descriptive model of response times. Behavior Research Methods, Instruments, & Computers, 33, 457-469.

Heathcote, A. (2004). Fitting Wald and ex-Wald distributions to response time data: An example using functions for the S-PLUS package. Behavior Research Methods, Instruments, & Computers, 36, 678-694.

See Also

ExWALD

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dExWALD(x, mu=0.15, sigma=52.5, nu=50), ylim=c(0, 0.005),
      from=0, to=1200, col="cadetblue3", las=1, ylab="f(x)")

curve(dExWALD(x, mu=0.20, sigma=70, nu=50),
      add=TRUE, col= "purple")

curve(dExWALD(x, mu=0.25, sigma=87.5, nu=50),
      add=TRUE, col="goldenrod")

curve(dExWALD(x, mu=0.20, sigma=70, nu=115),
      add=TRUE, col="tomato")

curve(dExWALD(x, mu=0.20, sigma=70, nu=35),
      add=TRUE, col="blue")

legend("topright", col=c("cadetblue3", "purple", "goldenrod",
                         "tomato", "blue"),
       lty=1, bty="n",
       legend=c("mu=0.15, sigma=52.5, nu=50",
                "mu=0.20, sigma=70.0, nu=50",
                "mu=0.25, sigma=87.5, nu=50",
                "mu=0.20, sigma=70.0, nu=115",
                "mu=0.20, sigma=70.0, nu=35"))

# Example 2
# Checking if the cumulative curves converge to 1
curve(pExWALD(x, mu=0.15, sigma=52.5, nu=50), ylim=c(0, 1),
      from=0, to=1200, col="cadetblue3", las=1, ylab="F(x)")

curve(pExWALD(x, mu=0.20, sigma=70, nu=50),
      add=TRUE, col= "purple")

curve(pExWALD(x, mu=0.25, sigma=87.5, nu=50),
      add=TRUE, col="goldenrod")

curve(pExWALD(x, mu=0.20, sigma=70, nu=115),
      add=TRUE, col="tomato")

curve(pExWALD(x, mu=0.20, sigma=70, nu=35),
      add=TRUE, col="blue")

legend("bottomright", col=c("cadetblue3", "purple", "goldenrod",
                         "tomato", "blue"),
       lty=1, bty="n",
       legend=c("mu=0.15, sigma=52.5, nu=50",
                "mu=0.20, sigma=70.0, nu=50",
                "mu=0.25, sigma=87.5, nu=50",
                "mu=0.20, sigma=70.0, nu=115",
                "mu=0.20, sigma=70.0, nu=35"))
```

```
# Example 3
# Checking the quantile function
mu <- 5
sigma <- 3
nu <- 2
p <- seq(from=0.1, to=0.99, length.out=100)
plot(x=qExWALD(p, mu=mu, sigma=sigma, nu=nu), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pExWALD(x, mu=mu, sigma=sigma, nu=nu), from=0, add=TRUE, col="red")

# Example 4
# Comparing the random generator output with
# the theoretical probabilities
mu <- 0.2
sigma <- 70
nu <- 35
x <- rExWALD(n=10000, mu=mu, sigma=sigma, nu=nu)
hist(x, freq=FALSE)
curve(dExWALD(x, mu=mu, sigma=sigma, nu=nu), col="tomato", add=TRUE)
```

---

dFWE *The Flexible Weibull Extension distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Flexible Weibull Extension distribution with parameters `mu` and `sigma`.

Usage

```
dFWE(x, mu, sigma, log = FALSE)

pFWE(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qFWE(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rFWE(n, mu, sigma)

hFWE(x, mu, sigma)
```

Arguments

`x, q`	vector of quantiles.
`mu`	parameter.
`sigma`	parameter.
`log, log.p`	logical; if TRUE, probabilities p are given as log(p).

lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Flexible Weibull extension with parameters mu and sigma has density given by

$f(x) = (\mu + \sigma/x^2)\exp(\mu x - \sigma/x)\exp(-\exp(\mu x - \sigma/x))$

for $x > 0$.

Value

dFWE gives the density, pFWE gives the distribution function, qFWE gives the quantile function, rFWE generates random deviates and hFWE gives the hazard function.

See Also

FWE

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dFWE(x, mu=0.75, sigma=0.5), from=0, to=3,
      ylim=c(0, 1.7), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pFWE(x, mu=0.75, sigma=0.5), from=0, to=3,
      col="red", las=1, ylab="F(x)")
curve(pFWE(x, mu=0.75, sigma=0.5, lower.tail=FALSE),
      from=0, to=3, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qFWE(p, mu=0.75, sigma=0.5), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pFWE(x, mu=0.75, sigma=0.5), from=0, add=TRUE, col="red")

## The random function
hist(rFWE(n=1000, mu=2, sigma=0.5), freq=FALSE, xlab="x",
     ylim=c(0, 2), las=1, main="")
curve(dFWE(x, mu=2, sigma=0.5), from=0, to=3, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hFWE(x, mu=0.75, sigma=0.5), from=0, to=2, ylim=c(0, 2.5),
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

dGammaW *The Gamma Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Gamma Weibull distribution with parameters mu, sigma, nu and tau.

Usage

```
dGammaW(x, mu, sigma, nu, log = FALSE)

pGammaW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qGammaW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rGammaW(n, mu, sigma, nu)

hGammaW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Gamma Weibull Distribution with parameters mu, sigma and nu has density given by
$f(x) = \frac{\sigma\mu^{\nu}}{\Gamma(\nu)} x^{\nu\sigma-1} \exp(-\mu x^{\sigma})$,
for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dGammaW gives the density, pGammaW gives the distribution function, qGammaW gives the quantile function, rGammaW generates random deviates and hGammaW gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Stacy, E. W. (1962). A generalization of the gamma distribution. The Annals of mathematical statistics, 1187-1192.

See Also

GammaW

Examples

```
# Example 1
# Plotting the mass function for different parameter values

## The probability density function
curve(dGammaW(x, mu=2, sigma=1.5, nu=0.5),
      from=0, to=2,
      col="red", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dGammaW(x, mu=2.4, sigma=1.5, nu=1.3),
      col="blue",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=2.0, sigma=1.5, nu=0.5",
                            "mu=2.4, sigma=1.5, nu=1.3"),
       col=c("red", "blue"), lwd=2, cex=0.6)

# Example 2
# Checking if the cumulative curves converge to 1

curve(pGammaW(x, mu=0.5, sigma=2, nu=1),
      from=0, to=3,
      col="red", lwd=2, ylab="F(x)")
curve(pGammaW(x, mu=2.4, sigma=1.5, nu=1.3),
      col="blue",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=2.0, sigma=1.5, nu=0.5",
                               "mu=2.4, sigma=1.5, nu=1.3"),
       col=c("red", "blue"), lwd=2, cex=0.6)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qGammaW(p, mu=2.3, sigma=1.7, nu=1.2), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pGammaW(x, mu=2.3, sigma=1.7, nu=1.2),
      from=0, add=TRUE, col="tomato", lwd=2.5)
```

```
# Example 4
# The random function
x <- rGammaW(n=10000, mu=2.4, sigma=1.5, nu=1.3)
hist(x, freq=FALSE)
curve(dGammaW(x, mu=2.4, sigma=1.5, nu=1.3),
      add=TRUE, col="tomato", lwd=2)

# The Hazard function
curve(hGammaW(x, mu=2.4, sigma=1.5, nu=1.3), from=0, to=5,
      col="red", ylab="Hazard function", las=1)
```

---

dGAo *The gamma distribution in its original parameterization*

Description

Density, distribution function, quantile function, random generation and hazard function for the gamma original distribution with parameters `mu` and `sigma`.

Usage

```
dGAo(x, mu = 1, sigma = 1, log = FALSE)

pGAo(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

qGAo(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rGAo(n, mu = 1, sigma = 1)

hGAo(x, mu, sigma)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter.
`sigma`	parameter.
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
`p`	vector of probabilities.
`n`	number of observations.

Details

The gamma original with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{x^{\mu-1}e^{-x/\sigma}}{\sigma^{\mu}\Gamma(\mu)}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. The parameter μ is the shape parameter and σ is the scale parameter. In this parameterization μ is the median of X, $E(X) = \mu\sigma$ and $Var(X) = \mu\sigma^2$.

Value

dGAo gives the density, pGAo gives the distribution function, qGAo gives the quantile function, rGAo generates random deviates and hGAo gives the hazard function.

References

Abramowitz M, Stegun IA (1972). Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables. Dover Publications, New York. ISBN 0486612724. Chapter 6: Gamma and Related Functions.

See Also

GAo.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dGAo(x, mu=7.5, sigma=1),
      from=0.001, to=20,
      ylim=c(0, 0.5),
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dGAo(x, mu=1, sigma=2),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(dGAo(x, mu=5, sigma=1),
      col="seagreen",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=7.5, sigma=1",
                            "mu=1 , sigma=2",
                            "mu=5, sigma=1"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.6)


# Example 2
# Checking if the cumulative curves converge to 1
curve(pGAo(x, mu=0.5, sigma=0.5),
      from=0.001, to=5,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pGAo(x, mu=1, sigma=0.5),
      col="tomato",
      lwd=2,
      add=TRUE)
curve(pGAo(x, mu=1.5, sigma=0.5),
      col="seagreen",
```

```
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.5, sigma=0.5",
                               "mu=1.0, sigma=0.5",
                               "mu=1.5, sigma=0.5"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)


# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qGAo(p, mu=2.3, sigma=1.7), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pGAo(x, mu=2.3, sigma=1.7),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
x <- rGAo(n=10000, mu=20, sigma=0.5)
hist(x, freq=FALSE)
curve(dGAo(x, mu=20, sigma=0.5), from=0, to=100,
      add=TRUE, col="tomato", lwd=2)

# Example 5
# The Hazard function
curve(hGAo(x, mu=20, sigma=0.5), from=0.001, to=100,
      col="tomato", ylab="Hazard function", las=1)
```

---

dGGD *The Generalized Gompertz distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the generalized Gompertz distribution with parameters `mu` `sigma` and `nu`.

Usage

```
dGGD(x, mu, sigma, nu, log = FALSE)

pGGD(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qGGD(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rGGD(n, mu, sigma, nu)

hGGD(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu, nu	scale parameter.
sigma	shape parameters.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Generalized Gompertz Distribution with parameters mu, sigma and nu has density given by
$f(x) = \nu\mu \exp(-\frac{\mu}{\sigma}(\exp(\sigma x - 1)))(1 - \exp(-\frac{\mu}{\sigma}(\exp(\sigma x - 1))))^{(\nu-1)}$,
for $x \geq 0$, $\mu > 0$, $\sigma \geq 0$ and $\nu > 0$.

Value

dGGD gives the density, pGGD gives the distribution function, qGGD gives the quantile function, rGGD generates random deviates and hGGD gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

El-Gohary, A., Alshamrani, A., & Al-Otaibi, A. N. (2013). The generalized Gompertz distribution. Applied mathematical modelling, 37(1-2), 13-24.

See Also

GGD

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
par(mfrow = c(1, 1))
curve(dGGD(x, mu=1, sigma=0.3, nu=1.5), from = 0, to = 4,
      col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pGGD(x, mu=1, sigma=0.3, nu=1.5), from = 0, to = 4,
      ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pGGD(x, mu=1, sigma=0.3, nu=1.5, lower.tail = FALSE),
      from = 0, to = 4, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")
```

```
## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qGGD(p=p, mu=1, sigma=0.3, nu=1.5), y = p,
     xlab = "Quantile", las = 1, ylab = "Probability")
curve(pGGD(x, mu=1, sigma=0.3, nu=1.5), from = 0, add = TRUE,
      col = "red")

## The random function
hist(rGGD(1000, mu=1, sigma=0.3, nu=1.5), freq = FALSE, xlab = "x",
     las = 1, ylim = c(0, 0.7), main = "")
curve(dGGD(x,mu=1, sigma=0.3, nu=1.5), from = 0, to =8, add = TRUE,
      col = "red")

## The Hazard function
par(mfrow=c(1,1))
curve(hGGD(x, mu=1, sigma=0.3, nu=1.5), from = 0, to = 3, col = "red",
      ylab = "The hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dGIW *The Generalized Inverse Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Generalized Inverse Weibull distribution with parameters mu, sigma and nu.

Usage

```
dGIW(x, mu, sigma, nu, log = FALSE)

pGIW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qGIW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rGIW(n, mu, sigma, nu)

hGIW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).

lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Generalized Inverse Weibull distribution mu, sigma and nu has density given by

$f(x) = \nu\sigma\mu^{\sigma}x^{-(\sigma+1)}exp\{-\nu(\frac{\mu}{x})^{\sigma}\}$,

for $x > 0$.

Value

dGIW gives the density, pGIW gives the distribution function, qGIW gives the quantile function, rGIW generates random deviates and hGIW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

De Gusmao, F. R., Ortega, E. M., & Cordeiro, G. M. (2011). The generalized inverse Weibull distribution. Statistical Papers, 52, 591-619.

See Also

GIW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dGIW(x, mu=3, sigma=5, nu=0.5), from=0.001, to=8,
      col="red", ylab="f(x)", las=1)

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pGIW(x, mu=3, sigma=5, nu=0.5),
      from=0.0001, to=14, col="red", las=1, ylab="F(x)")
curve(pGIW(x, mu=3, sigma=5, nu=0.5, lower.tail=FALSE),
      from=0.0001, to=14, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qGIW(p, mu=3, sigma=5, nu=0.5), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pGIW(x, mu=3, sigma=5, nu=0.5),
```

```
      from=0, add=TRUE, col="red")

## The random function
hist(rGIW(n=1000, mu=3, sigma=5, nu=0.5), freq=FALSE,
     xlab="x", ylim=c(0, 0.8), las=1, main="")
curve(dGIW(x, mu=3, sigma=5, nu=0.5),
      from=0.001, to=14, add=TRUE, col="red")

## The Hazard function
curve(hGIW(x, mu=3, sigma=5, nu=0.5), from=0.001, to=30,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dGLIN *The Generalized Lindley Type II (GLIN) distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Generalized Lindley Type II, GLIN(), distribution with parameters μ and σ.

Usage

```
dGLIN(x, mu, sigma, log = FALSE)

pGLIN(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qGLIN(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rGLIN(n, mu, sigma)

hGLIN(x, mu = 0.5, sigma = 0.5)
```

Arguments

x, q	vector of positive quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of random values to return.

Details

The Generalized Lindley Type II distribution with parameters `mu` and `sigma` has probability density function

$f(x|\mu,\sigma) = \frac{\mu^2}{\mu+1}\left(1 + \frac{\mu^{\sigma-2}x^{\sigma-1}}{\Gamma(\sigma)}\right)e^{-\mu x}$,

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

The distribution is a two-parameter extension of the classical Lindley distribution and belongs to the class of finite mixtures involving exponential and gamma components. It provides additional flexibility for modeling positively skewed lifetime data.

The original parameters of the distribution are denoted by θ and α. In the GAMLSS implementation, they are re-parameterized as $\mu = \theta$ and $\sigma = \alpha$.

The r-th raw moment is given by

$E(X^r) = \frac{1}{\mu^r(\mu+1)}\left[\mu\Gamma(r+1) + \frac{\Gamma(r+\sigma)}{\Gamma(\sigma)}\right]$.

In particular, the mean is

$E(X) = \frac{\mu+\sigma}{\mu(\mu+1)}$.

and the variance is

$Var(X) = \frac{\mu^2+\mu(\sigma^2-\sigma+2)+\sigma}{\mu^2(\mu+1)^2}$.

The GLIN distribution is a flexible two-parameter extension of the classical Lindley distribution and is suitable for modeling positive lifetime and survival data.

Value

`dGLIN` gives the density, `pGLIN` gives the distribution function, `qGLIN` gives the quantile function, and `rGLIN` generates random deviates.

Author(s)

Sofia Cadavid Rueda, <socadavidr@unal.edu.co>

References

Ekhosuehi, N., Opone, F., & Odobaire, F. (2018). A New Generalized Two Parameter Lindley Distribution. Journal of the Nigerian Statistical Association, 30, 547–566.

See Also

GLIN.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
x_vals <- seq(0, 6, length.out = 500)
# Calculate densities
d1 <- dGLIN(x_vals, mu = 0.7, sigma = 1.4)
d2 <- dGLIN(x_vals, mu = 0.3, sigma = 1.2)
```

```
d3 <- dGLIN(x_vals, mu = 3.0, sigma = 1.0)
d4 <- dGLIN(x_vals, mu = 6.0, sigma = 1.0)
# Plot
plot(x_vals, d1, type = "l", col = "red", lwd = 2, lty = 1,
     ylim = c(0, 5), xlim = c(0, 6),
     xlab = "x", ylab = "f(x)",
     main = "Probability Density Function of the GLIN Distribution",
     las = 1)
lines(x_vals, d2, col = "black", lwd = 2, lty = 2)
lines(x_vals, d3, col = "yellow", lwd = 2, lty = 1)
lines(x_vals, d4, col = "green4", lwd = 2, lty = 1)
# Legend
legend("topright",
       col = c("red", "black", "yellow", "green4"),
       lwd = 2,
       lty = c(1, 2, 1, 1),
       legend = c(expression(paste(sigma, " = 1.4, ", mu, " = 0.7")),
                  expression(paste(sigma, " = 1.2, ", mu, " = 0.3")),
                  expression(paste(sigma, " = 1.0, ", mu, " = 3.0")),
                  expression(paste(sigma, " = 1.0, ", mu, " = 6.0"))),
       bty = "n")

# Example 2
# Checking if the cumulative curves converge to 1
curve(pGLIN(x, mu=0.7, sigma=1.4),
      from=0.00001, to=40,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pGLIN(x, mu=0.3, sigma=1.2),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.7, sigma=1.4",
                               "mu=0.3, sigma=1.2"),
       col=c("royalblue1", "tomato", "seagreen"), lwd=2, cex=0.5)

# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qGLIN(p, mu=3, sigma=1), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pGLIN(x, mu=3, sigma=1),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4
# The random function
set.seed(123)
x <- rGLIN(5000, mu=0.7, sigma=1.4)
hist(x, breaks=50, freq=FALSE,
     main="rGLIN vs theory density",
     xlab="x", col="lightblue", border="white")
```

```
curve(dGLIN(x, mu=0.7, sigma=1.4),
      add=TRUE, col="red", lwd=2)

# Example 5
# The Hazard function
curve(hGLIN(x, mu=0.7, sigma=1.4), from=0.001, to=40,
      col="tomato", ylab="Hazard function", las=1)
```

---

dGMW *The Generalized modified Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the generalized modified weibull distribution with parameters mu, sigma, nu and tau.

Usage

```
dGMW(x, mu, sigma, nu, tau, log = FALSE)

pGMW(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qGMW(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

rGMW(n, mu, sigma, nu, tau)

hGMW(x, mu, sigma, nu, tau, log = FALSE)
```

Arguments

x, q	vector of quantiles.
mu	scale parameter.
sigma	shape parameter.
nu	shape parameter.
tau	acceleration parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The generalized modified weibull with parameters mu, sigma, nu and tau has density given by
$f(x) = \mu\sigma x^{\nu-1}(\nu+\tau x)\exp(\tau x - \mu x^{\nu}e^{\tau x})[1-\exp(-\mu x^{\nu}e^{\tau x})]^{\sigma-1}$,
for $x > 0$.

Value

dGMW gives the density, pGMW gives the distribution function, qGMW gives the quantile function, rGMW generates random deviates and hGMW gives the hazard function.

See Also

GMW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5), from=0, to=0.8,
      ylim=c(0, 2), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5),
      from=0, to=1.2, col="red", las=1, ylab="F(x)")
curve(pGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5, lower.tail=FALSE),
      from=0, to=1.2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qGMW(p, mu=2, sigma=0.5, nu=2, tau=1.5), y=p, xlab="Quantile",
    las=1, ylab="Probability")
curve(pGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5), from=0, add=TRUE, col="red")

## The random function
hist(rGMW(n=1000, mu=2, sigma=0.5, nu=2,tau=1.5), freq=FALSE,
    xlab="x", main ="", las=1)
curve(dGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5),  from=0, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hGMW(x, mu=2, sigma=0.5, nu=2, tau=1.5), from=0, to=1, ylim=c(0, 16),
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dGWF *Generalized Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the generalized Weibull distribution with parameters mu, sigma and nu.

Usage

```
dGWF(x, mu, sigma, nu, log = FALSE)

pGWF(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qGWF(p, mu, sigma, nu)

rGWF(n, mu, sigma, nu)

hGWF(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter one.
sigma	parameter two.
nu	parameter three.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The generalized Weibull with parameters mu, sigma and nu has density given by

$$f(x) = \mu\sigma x^{\sigma-1}\left(1-\mu\nu x^{\sigma}\right)^{\frac{1}{\nu}-1}$$

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $-\infty < \nu < \infty$.

Value

dGWF gives the density, pGWF gives the distribution function, qGWF gives the quantile function, rGWF generates random deviates and hGWF gives the hazard function.

Author(s)

Jaime Mosquera, <jmosquerag@unal.edu.co>

References

Mudholkar, G. S., & Kollia, G. D. (1994). Generalized Weibull family: a structural analysis. Communications in statistics-theory and methods, 23(4), 1149-1171.

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(
    dGWF(x, mu = 5, sigma = 2, nu = -0.2),
    from = 0, to = 5, col = "red", las = 1, ylab = "f(x)"
)

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(
    pGWF(x, mu = 5, sigma = 2, nu = -0.2),
    from = 0, to = 5, ylim = c(0, 1),
    col = "red", las = 1, ylab = "F(x)"
)
curve(
    pGWF(
        x, mu = 5, sigma = 2, nu = -0.2,
        lower.tail = FALSE
    ),
    from = 0, to = 5, ylim = c(0, 1),
    col = "red", las = 1, ylab = "R(x)"
)

## The quantile function
p <- seq(from = 0, to = 0.999, length.out = 100)
plot(
    x = qGWF(p, mu = 5, sigma = 2, nu = -0.2),
    y = p, xlab = "Quantile", las = 1,
    ylab = "Probability"
)
curve(
    pGWF(x, mu = 5, sigma = 2, nu = -0.2),
    from = 0, add = TRUE, col = "red"
)

## The random function
hist(
    rGWF(n = 10000, mu = 5, sigma = 2, nu = -0.2),
    freq = FALSE, xlab = "x", las = 1, main = "", ylim = c(0, 2.0)
)
curve(dGWF(x, mu = 5, sigma = 2, nu = -0.2),
    from = 0, add = TRUE, col = "red"
)

## The Hazard function
par(mfrow = c(1, 1))
curve(
    hGWF(x, mu = 0.003, sigma = 5e-6, nu = 0.025),
    from = 0, to = 250, col = "red",
    ylab = "Hazard function", las = 1
```

```
)

par(old_par) # restore previous graphical parameters
```

---

dIPXLIN *The Inverse Power XLindley distribution - Hassan et al. (2025)*

Description

Density, distribution function, quantile function, random generation and hazard function for the Inverse Power XLindley distribution with parameters `mu` and `sigma`.

Usage

```
dIPXLIN(x, mu = 1, sigma = 1, log = FALSE)

pIPXLIN(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

qIPXLIN(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rIPXLIN(n, mu = 1, sigma = 1)

hIPXLIN(x, mu = 1, sigma = 1)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter representing η (`mu > 0`).
`sigma`	parameter representing σ (`sigma > 0`).
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
`p`	vector of probabilities.
`n`	number of observations.

Details

The Inverse Power XLindley with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{\sigma\mu^2}{(1+\mu)^2} x^{-2\sigma-1}\left(1+(2+\mu)x^{\sigma}\right)e^{-\mu x^{-\sigma}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, μ is the scale parameter and σ is the shape parameter.

Value

`dIPXLIN` gives the density, `pIPXLIN` gives the distribution function, `qIPXLIN` gives the quantile function, `rIPXLIN` generates random deviates and `hIPXLIN` gives the hazard function.

Author(s)

Sebastián Ándres Rios Romero, <srios.romero@udea.edu.co>

References

Hassan, A. S., Alsadat, N., Chesneau, C., Elgarhy, M., Kayid, M., Nasiru, S., & Gemeay, A. M. (2025). Inverse power XLindley distribution with statistical inference and applications to engineering data. Scientific Reports, 15, 4385.

See Also

IPXLIN.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dIPXLIN(x, mu=0.5, sigma=1.5),
      from=0.001, to=2.5,
      col="royalblue1", lwd=2,
      main="Density function",
      xlab="x", ylab="f(x)")
curve(dIPXLIN(x, mu=1.5, sigma=3.5),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("topright", legend=c("mu=0.5, sigma=1.5",
                            "mu=1.5, sigma=3.5"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.6)


# Example 2
# Checking if the cumulative curves converge to 1
curve(pIPXLIN(x, mu=0.5, sigma=1.5),
      from=0.00001, to=4,
      ylim=c(0, 1),
      col="royalblue1", lwd=2,
      main="Cumulative Distribution Function",
      xlab="x", ylab="F(x)")
curve(pIPXLIN(x, mu=1.5, sigma=4.0),
      col="tomato",
      lwd=2,
      add=TRUE)
legend("bottomright", legend=c("mu=0.5, sigma=1.5",
                               "mu=1.5, sigma=4.0"),
       col=c("royalblue1", "tomato"), lwd=2, cex=0.5)


# Example 3
p <- seq(from=0, to=0.99, length.out=100)
plot(x=qIPXLIN(p, mu=0.5, sigma=1.5), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
```

```
curve(pIPXLIN(x, mu=0.5, sigma=1.5),
      from=0, add=TRUE, col="tomato", lwd=2.5)


# Example 4
# The random function
x <- rIPXLIN(n=1000, mu=0.5, sigma=3.5)
hist(x, freq=FALSE, breaks=50, xlim=c(0,4))
curve(dIPXLIN(x, mu=0.5, sigma=3.5),
      add=TRUE, col="tomato", lwd=2)


# Example 5
# The Hazard function
curve(hIPXLIN(x, mu=0.5, sigma=1.5), from=0.001, to=4,
      col="tomato", ylab="Hazard function", las=1)
```

---

dIW *The Inverse Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the inverse weibull distribution with parameters mu and sigma.

Usage

```
dIW(x, mu, sigma, log = FALSE)

pIW(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qIW(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rIW(n, mu, sigma)

hIW(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	scale parameter.
sigma	shape parameters.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The inverse weibull distribution with parameters mu and sigma has density given by

$f(x) = \mu\sigma x^{-\sigma-1}\exp(\mu x^{-\sigma})$

for $x > 0$, $\mu > 0$ and $\sigma > 0$

Value

dIW gives the density, pIW gives the distribution function, qIW gives the quantile function, rIW generates random deviates and hIW gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Drapella, A. (1993). The complementary Weibull distribution: unknown or just forgotten?. Quality and reliability engineering international, 9(4), 383-385.

See Also

IW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dIW(x, mu=5, sigma=2.5), from=0, to=10,
      ylim=c(0, 0.55), col="red", las=1, ylab="f(x)")
#'
## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pIW(x, mu=5, sigma=2.5),
      from=0, to=10,  col="red", las=1, ylab="F(x)")
curve(pIW(x, mu=5, sigma=2.5, lower.tail=FALSE),
      from=0, to=10, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qIW(p, mu=5, sigma=2.5), y=p, xlab="Quantile",
  las=1, ylab="Probability")
curve(pIW(x, mu=5, sigma=2.5), from=0, add=TRUE, col="red")

## The random function
hist(rIW(n=10000, mu=5, sigma=2.5), freq=FALSE, xlim=c(0,60),
  xlab="x", las=1, main="")
curve(dIW(x, mu=5, sigma=2.5), from=0, add=TRUE, col="red")
```

```
## The Hazard function
par(mfrow=c(1,1))
curve(hIW(x, mu=5, sigma=2.5), from=0, to=15, ylim=c(0, 0.9),
   col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dKumIW *The Kumaraswamy Inverse Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Kumaraswamy Inverse Weibull distribution with parameters mu, sigma and nu.

Usage

```
dKumIW(x, mu, sigma, nu, log = FALSE)

pKumIW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qKumIW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rKumIW(n, mu, sigma, nu)

hKumIW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Kumaraswamy Inverse Weibull Distribution with parameters mu, sigma and nu has density given by

$f(x) = \mu\sigma\nu x^{-\mu-1} \exp -\sigma x^{-\mu}(1 - \exp -\sigma x^{-\mu})^{\nu-1}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dKumIW gives the density, pKumIW gives the distribution function, qKumIW gives the quantile function, rKumIW generates random deviates and hKumIW gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Shahbaz, M. Q., Shahbaz, S., & Butt, N. S. (2012). The Kumaraswamy Inverse Weibull Distribution. Pakistan journal of statistics and operation research, 479-489.

See Also

KumIW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
par(mfrow = c(1, 1))
curve(dKumIW(x, mu = 1.5, sigma=  1.5, nu = 1), from = 0, to = 8.5,
      col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pKumIW(x, mu = 1.5, sigma=  1.5, nu = 1), from = 0, to = 8.5,
      ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pKumIW(x, mu = 1.5, sigma=  1.5, nu = 1, lower.tail = FALSE),
      from = 0, to = 6, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qKumIW(p=p, mu = 1.5, sigma=  1.5, nu = 10), y = p,
     xlab = "Quantile", las = 1, ylab = "Probability")
curve(pKumIW(x, mu = 1.5, sigma=  1.5, nu = 10), from = 0, add = TRUE,
      col = "red")

## The random function
hist(rKumIW(1000, mu = 1.5, sigma=  1.5, nu = 5), freq = FALSE, xlab = "x",
     las = 1, ylim = c(0, 1.5), main = "")
curve(dKumIW(x, mu = 1.5, sigma=  1.5, nu = 5), from = 0, to =8, add = TRUE,
      col = "red")

## The Hazard function
par(mfrow=c(1,1))
curve(hKumIW(x, mu = 1.5, sigma=  1.5, nu = 1), from = 0, to = 3,
```

```
      ylim = c(0, 0.7), col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dLIN *Lindley distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Lindley distribution with parameter mu.

Usage

```
dLIN(x, mu, log = FALSE)

pLIN(q, mu, lower.tail = TRUE, log.p = FALSE)

qLIN(p, mu, lower.tail = TRUE, log.p = FALSE)

rLIN(n, mu)

hLIN(x, mu, log = FALSE)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

Lindley Distribution with parameter mu has density given by

$f(x) = \frac{\mu^2}{\mu+1}(1+x)\exp(-\mu x)$,

for $x > 0$ and $\mu > 0$. These function were taken form LindleyR package.

Value

dLIN gives the density, pLIN gives the distribution function, qLIN gives the quantile function, rLIN generates random deviates and hLIN gives the hazard function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Lindley, D. V. (1958). Fiducial distributions and Bayes' theorem. Journal of the Royal Statistical Society. Series B (Methodological), 102-107.

See Also

LIN

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dLIN(x, mu=1.5), from=0.0001, to=10,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pLIN(x, mu=2), from=0.0001, to=10, col="red", las=1, ylab="F(x)")
curve(pLIN(x, mu=2, lower.tail=FALSE), from=0.0001,
      to=10, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qLIN(p, mu=2), y=p, xlab="Quantile", las=1, ylab="Probability")
curve(pLIN(x, mu=2), from=0, add=TRUE, col="red")

## The random function
hist(rLIN(n=10000, mu=2), freq=FALSE, xlab="x", las=1, main="")
curve(dLIN(x, mu=2), from=0.09, to=5, add=TRUE, col="red")

## The Hazard function
curve(hLIN(x, mu=2), from=0.001, to=10, col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dLW *The Log-Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Log-Weibull distribution with parameters `mu` and `sigma`.

Usage

```
dLW(x, mu, sigma, log = FALSE)

pLW(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qLW(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rLW(n, mu, sigma)

hLW(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Log-Weibull Distribution with parameters mu and sigma has density given by

$f(y) = (1/\sigma)e^{((y-\mu)/\sigma)}exp\{-e^{((y-\mu)/\sigma)}\}$,

for $-\infty < y < \infty$.

Value

dLW gives the density, pLW gives the distribution function, qLW gives the quantile function, rLW generates random deviates and hLW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Gumbel, E. J. (1958). Statistics of extremes. Columbia university press.

See Also

LW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dLW(x, mu=0, sigma=1.5), from=-8, to=5,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pLW(x, mu=0, sigma=1.5),
      from=-8, to=5,  col="red", las=1, ylab="F(x)")
curve(pLW(x, mu=0, sigma=1.5, lower.tail=FALSE),
      from=-8, to=5, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qLW(p, mu=0, sigma=1.5), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pLW(x, mu=0, sigma=1.5), from=-8, to=5, add=TRUE, col="red")

## The random function
hist(rLW(n=10000, mu=0, sigma=1.5), freq=FALSE,
     xlab="x", las=1, main="")
curve(dLW(x, mu=0, sigma=1.5), from=-15, to=6, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hLW(x, mu=0, sigma=1.5), from=-8, to=7,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dMCWEI *The Modified Cosine-Weibull distribution (MCWEI)*

Description

Density function, cumulative distribution function, quantile function, random generation and hazard function for the Modified Cosine-Weibull distribution with parameters mu, sigma and nu.

Usage

```
dMCWEI(x, mu = 2.2, sigma = 1.2, nu = 0.5, log = TRUE)

pMCWEI(q, mu = 2.2, sigma = 1.2, nu = 0.5, lower.tail = TRUE, log.p = FALSE)

qMCWEI(p, mu = 2.2, sigma = 1.2, nu = 0.5, lower.tail = TRUE, log.p = FALSE)

rMCWEI(n, mu = 2.2, sigma = 1.2, nu = 0.5)
```

```
hMCWEI(x, mu = 2.2, sigma = 1.2, nu = 0.5)
```

Arguments

x, q	vector of quantiles.
mu	parameter representing the shape parameter ϕ (mu > 0).
sigma	parameter representing the scale parameter τ (sigma > 0).
nu	parameter representing the additional modified cosine parameter σ (nu != 0).
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Modified Cosine-Weibull with parameters mu, sigma and nu has density given by

$f(x|\mu,\sigma,\nu) = \frac{\pi\mu\sigma\nu x^{\mu-1}e^{-\sigma x^{\mu}}\cos(\frac{\pi}{2}e^{-\sigma x^{\mu}})\sin(\frac{\pi}{2}e^{-\sigma x^{\mu}})}{e^{\nu}-1}\cdot e^{\nu\left(1-\cos^2(\frac{\pi}{2}e^{-\sigma x^{\mu}})\right)}$

for $x \geq 0$, $\mu > 0$, $\sigma > 0$ and $\nu \neq 0$.

Value

dMCWEI gives the density, pMCWEI gives the cumulative distribution function, qMCWEI gives the quantile function, rMCWEI generates random deviates and hMCWEI gives the hazard function.

Author(s)

Juan Andres Henao Arias, <juhenaoar@unal.edu.co>

References

Su, R., Aloraini, N. M., Alkhathami, A. A., Alshanbari, H. M., & Khalifa, H. A. E. W. (2025). A new statistical distribution: Its empirical exploration using the reliability and lifespan data in fashion industry. Alexandria Engineering Journal, 116, 660-671.

See Also

BS.

Examples

```
# Example 1: Plotting the density function (dMCWEI) for different values.
mu_ <- c(2.8, 4.4)
sigma_ <- c( 0.1, 0.01)
nu_ <- c( 0.1, 0.01)
X_ <- seq(0.0001, 5, length=350)
```

```
curve(dMCWEI(x, log = FALSE), type = "l", col= "royalblue", lwd=2.5,
     from = 0.001, to = 5, ylim=c(0,3), xlim = c(0,4),
     xlab = "x", ylab = "f(x)")
title("Density Function")

colors <- c("red", "green")

for(k in seq(1, 2)) {
  curve(
    dMCWEI(x, mu=mu_[k], sigma=sigma_[k], nu = nu_[k], log = FALSE ),
    type = "l", col = colors[k], lwd=2, lty = 3,
    from = 0.001, to=5, add = TRUE)
}

legend("topright",
       legend = c(
         expression(mu==2.2 ~ sigma==1.2 ~ nu==0.50),
         expression(mu==2.8 ~ sigma==0.1 ~ nu==0.10),
         expression(mu==4.4 ~ sigma==0.01 ~ nu==0.01)
       ),
       lwd=2,
       col=c("royalblue",colors),
       lty = c(1,3,3),
       bty="n")

# Example 2: Plotting the Cumulative Distribution function
# (pMCWEI) for differente values.

parameters <- data.frame(
  mu=c(0.5, 1.5, 2.5),
  sigma=c(1,0.5,1.2),
  nu=c(0.8,1,1.5))

colors <- c("royalblue", "red", "green")
curve(pMCWEI(x, mu=parameters$mu[1],
             sigma = parameters$sigma[1],
             nu = parameters$nu[1]),
      lwd=2.5, col=colors[1],
      from = 0.001, to=5,
      xlab = "x", ylab = "F(x)")
title("Cumulative Probability")

for(k in seq(2, 3)) {
curve(pMCWEI(x,
             mu=parameters$mu[k],
             sigma = parameters$sigma[k],
             nu = parameters$nu[k]),
      lwd=2, col=colors[k], add = TRUE, lty=3)

}

legend(
  "bottomright",
```

```
  legend = c(
    expression(mu==0.5 ~" "  ~sigma==1 ~ " " ~ nu==0.8),
    expression(mu==1.5 ~" " ~  sigma==0.5 ~  " " ~ nu==1.0),
    expression(mu==2.5 ~" "~ sigma==1.2 ~ " "~nu==1.5)
  ),
  lwd = 2, lty = c(1,3,3), bty="n")


# Example 3
# The quantile function
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qMCWEI(p, mu=2.3, sigma=1.7, nu=1.3), y=p, xlab="Quantile",
     las=1, ylab="Probability", main="Quantile function ")
curve(pMCWEI(x, mu=2.3, sigma=1.7, nu=1.3),
      from=0, add=TRUE, col="tomato", lwd=2.5)

# Example 4: Generating a Random Sample for the distribution.

set.seed(5)
hist(rMCWEI(200), freq=FALSE, col = "orange",
     xlab = "x", ylab = "y",
     main = "Theoretical values V.S Experimental values")
curve(dMCWEI(x, log = FALSE), add = TRUE,
      from = 0.0001, to=5, col="royalblue", lwd=3)

legend("topright",
       legend = c(expression(f(x))),
       lwd = 2, lty = 1, bty="n", col="royalblue")
```

---

dMOEIW *The Marshall-Olkin Extended Inverse Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Marshall-Olkin Extended Inverse Weibull distribution with parameters `mu`, `sigma` and `nu`.

Usage

```
dMOEIW(x, mu, sigma, nu, log = FALSE)

pMOEIW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qMOEIW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rMOEIW(n, mu, sigma, nu)

hMOEIW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Marshall-Olkin Extended Inverse Weibull distribution mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu x^{-(\sigma+1)} exp\{-\mu x^{-\sigma}\}}{\{\nu-(\nu-1)exp\{-\mu x^{-\sigma}\}\}^2}$,

for $x > 0$.

Value

dMOEIW gives the density, pMOEIW gives the distribution function, qMOEIW gives the quantile function, rMOEIW generates random deviates and hMOEIW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Okasha, H. M., El-Baz, A. H., Tarabia, A. M. K., & Basheer, A. M. (2017). Extended inverse Weibull distribution with reliability application. Journal of the Egyptian Mathematical Society, 25(3), 343-349.

See Also

MOEIW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dMOEIW(x, mu=0.6, sigma=1.7, nu=0.3), from=0, to=2,
      col="red", ylab="f(x)", las=1)

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pMOEIW(x, mu=0.6, sigma=1.7, nu=0.3),
      from=0.0001, to=2, col="red", las=1, ylab="F(x)")
```

```
curve(pMOEIW(x, mu=0.6, sigma=1.7, nu=0.3, lower.tail=FALSE),
      from=0.0001, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qMOEIW(p, mu=0.6, sigma=1.7, nu=0.3), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pMOEIW(x, mu=0.6, sigma=1.7, nu=0.3),
      from=0, add=TRUE, col="red")

## The random function
hist(rMOEIW(n=1000, mu=0.6, sigma=1.7, nu=0.3), freq=FALSE,
     xlab="x", las=1, main="")
curve(dMOEIW(x, mu=0.6, sigma=1.7, nu=0.3),
      from=0.001, to=4, add=TRUE, col="red")

## The Hazard function
curve(hMOEIW(x, mu=0.5, sigma=0.7, nu=1), from=0.001, to=3,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dMOEW *The Marshall-Olkin Extended Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Marshall-Olkin Extended Weibull distribution with parameters `mu`, `sigma` and `nu`.

Usage

```
dMOEW(x, mu, sigma, nu, log = FALSE)

pMOEW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qMOEW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rMOEW(n, mu, sigma, nu)

hMOEW(x, mu, sigma, nu)
```

Arguments

`x, q`	vector of quantiles.
`mu`	parameter.
`sigma`	parameter.
`nu`	parameter.

log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Marshall-Olkin Extended Weibull distribution mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu(\nu x)^{\sigma-1}exp\{-(\nu x)^{\sigma}\}}{\{1-(1-\mu)exp\{-(\nu x)^{\sigma}\}\}^2}$,

for $x > 0$.

Value

dMOEW gives the density, pMOEW gives the distribution function, qMOEW gives the quantile function, rMOEW generates random deviates and hMOEW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Ghitany, M. E., Al-Hussaini, E. K., & Al-Jarallah, R. A. (2005). Marshall–Olkin extended Weibull distribution and its application to censored data. Journal of Applied Statistics, 32(10), 1025-1034.

See Also

MOEW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dMOEW(x, mu=0.5, sigma=0.7, nu=1), from=0.001, to=1,
      col="red", ylab="f(x)", las=1)

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pMOEW(x, mu=0.5, sigma=0.7, nu=1),
      from=0.0001, to=2, col="red", las=1, ylab="F(x)")
curve(pMOEW(x, mu=0.5, sigma=0.7, nu=1, lower.tail=FALSE),
      from=0.0001, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qMOEW(p, mu=0.5, sigma=0.7, nu=1), y=p, xlab="Quantile",
```

```
     las=1, ylab="Probability")
curve(pMOEW(x, mu=0.5, sigma=0.7, nu=1),
      from=0, add=TRUE, col="red")

## The random function
hist(rMOEW(n=100, mu=0.5, sigma=0.7, nu=1), freq=FALSE,
     xlab="x", ylim=c(0, 1), las=1, main="")
curve(dMOEW(x, mu=0.5, sigma=0.7, nu=1),
      from=0.001, to=2, add=TRUE, col="red")

## The Hazard function
curve(hMOEW(x, mu=0.5, sigma=0.7, nu=1), from=0.001, to=3,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dMOK *The Marshall-Olkin Kappa distribution*

Description

Desnsity, distribution function, quantile function, random generation and hazard function for the Marshall-Olkin Kappa distribution with parameters mu, sigma, nu and tau.

Usage

```
dMOK(x, mu, sigma, nu, tau, log = FALSE)

pMOK(q, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

qMOK(p, mu, sigma, nu, tau, lower.tail = TRUE, log.p = FALSE)

rMOK(n, mu, sigma, nu, tau)

hMOK(x, mu, sigma, nu, tau)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
tau	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Marshall-Olkin Kappa distribution with parameters mu, sigma, nu and tau has density given by:

$$f(x) = \frac{\tau \frac{\mu\nu}{\sigma}\left(\frac{x}{\sigma}\right)^{\nu-1}\left(\mu+\left(\frac{x}{\sigma}\right)^{\mu\nu}\right)^{-\frac{\mu+1}{\mu}}}{\left[\tau+(1-\tau)\left(\frac{\left(\frac{x}{\sigma}\right)^{\mu\nu}}{\mu+\left(\frac{x}{\sigma}\right)^{\mu\nu}}\right)^{\frac{1}{\mu}}\right]^2}$$

for $x > 0$.

Value

dMOK gives the density, pMOK gives the distribution function, qMOK gives the quantile function, rMOK generates random deviates and hMOK gives the hazard function.

Author(s)

Angel Muñoz,

References

Javed, M., Nawaz, T., & Irfan, M. (2019). The Marshall-Olkin kappa distribution: properties and applications. Journal of King Saud University-Science, 31(4), 684-691.

See Also

MOK

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
par(mfrow = c(1,1))
curve(dMOK(x = x, mu = 1, sigma = 3.5, nu = 3, tau = 2), from = 0, to = 15,
      ylab = 'f(x)', col = 2, las = 1)

## The cumulative distribution and the Reliability function

par(mfrow = c(1,2))
curve(pMOK(q = x, mu = 1, sigma = 2.5, nu = 3, tau = 2), from = 0, to = 10,
     col = 2, lwd = 2, las = 1, ylab = 'F(x)')
curve(pMOK(q = x, mu = 1, sigma = 2.5, nu = 3, tau = 2, lower.tail = FALSE), from = 0, to = 10,
      col = 2, lwd = 2, las = 1, ylab = 'R(x)')

## The quantile function
p <- seq(from = 0.00001, to = 0.99999, length.out = 100)
plot(x = qMOK(p = p, mu = 4, sigma = 2.5, nu = 3, tau = 2), y = p, xlab = 'Quantile',
     las = 1, ylab = 'Probability')
curve(pMOK(q = x, mu = 4, sigma = 2.5, nu = 3, tau = 2), from = 0, to = 15,
      add = TRUE, col = 2)
```

```
## The random function

hist(rMOK(n = 10000, mu = 1, sigma = 2.5, nu = 3, tau = 2), freq = FALSE,
     xlab = "x", las = 1, main = '', ylim = c(0,.3), xlim = c(0,20), breaks = 50)
curve(dMOK(x, mu = 1, sigma = 2.5, nu = 3, tau = 2), from = 0, to = 15, add = TRUE, col = 2)

## The Hazard function

par(mfrow = c(1,1))
curve(hMOK(x = x, mu = 1, sigma = 2.5, nu = 3, tau = 2), from = 0, to = 20,
      col = 2, ylab = 'Hazard function', las = 1)

par(old_par) # restore previous graphical parameters
```

---

dMW *The Modified Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the modified weibull distribution with parameters mu, sigma and nu.

Usage

```
dMW(x, mu, sigma, nu, log = FALSE)

pMW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qMW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rMW(n, mu, sigma, nu)

hMW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	shape parameter one.
sigma	parameter two.
nu	scale parameter three.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The modified weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \mu(\sigma + \nu x)x^{\sigma-1}\exp(\nu x)\exp(-\mu x^{\sigma}\exp(\nu x))$

for $x > 0$, $\mu > 0$, $\sigma \geq 0$ and $\nu \geq 0$.

Value

dMW gives the density, pMW gives the distribution function, qMW gives the quantile function, rMW generates random deviates and hMW gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Lai, C. D., Xie, M., & Murthy, D. N. P. (2003). A modified Weibull distribution. IEEE Transactions on reliability, 52(1), 33-37.

See Also

MW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dMW(x, mu=2, sigma=1.5, nu=0.2), from=0, to=2,
  ylim=c(0, 1.5), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pMW(x, mu=2, sigma=1.5, nu=0.2), from=0, to=2,
 col = "red", las=1, ylab="F(x)")
curve(pMW(x, mu=2, sigma=1.5, nu=0.2, lower.tail = FALSE),
from=0, to=2, col="red", las=1, ylab ="R(x)")

## The quantile function
p <- seq(from=0, to=0.9999, length.out=100)
plot(x=qMW(p, mu=2, sigma=1.5, nu=0.2), y=p, xlab="Quantile",
 las=1, ylab="Probability")
curve(pMW(x, mu=2, sigma=1.5, nu=0.2), from=0, add=TRUE, col="red")

## The random function
hist(rMW(n=1000, mu=2, sigma=1.5, nu=0.2), freq=FALSE,
 xlab="x", las=1, main="")
curve(dMW(x, mu=2, sigma=1.5, nu=0.2), from=0, add=TRUE, col="red")
```

```
## The Hazard function
par(mfrow=c(1,1))
curve(hMW(x, mu=2, sigma=1.5, nu=0.2), from=0, to=1.5, ylim=c(0, 5),
 col="red", las=1, ylab="H(x)", las=1)

par(old_par) # restore previous graphical parameters
```

---

dNEE *The New Exponentiated Exponential distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the two-parameter New Exponentiated Exponential with parameters `mu` and `sigma`.

Usage

```
dNEE(x, mu = 1, sigma = 1, log = FALSE)

pNEE(q, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

qNEE(p, mu = 1, sigma = 1, lower.tail = TRUE, log.p = FALSE)

rNEE(n = 1, mu = 1, sigma = 1)

hNEE(x, mu, sigma, log = FALSE)
```

Arguments

`x`, `q`	vector of quantiles.
`mu`	parameter.
`sigma`	parameter.
`log`, `log.p`	logical; if TRUE, probabilities p are given as log(p).
`lower.tail`	logical; if TRUE (default), probabilities are $P[X <= x]$, otherwise, $P[X > x]$.
`p`	vector of probabilities.
`n`	number of observations.

Details

The New Exponentiated Exponential distribution with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \log(2^{\sigma})\mu \exp(-\mu x)(1-\exp(-\mu x))^{\sigma-1} 2^{(1-\exp(-\mu x))^{\sigma}}$,

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

Note: In this implementation we changed the original parameters θ for μ and α for σ, we did it to implement this distribution within gamlss framework.

Value

dNEE gives the density, pNEE gives the distribution function, qNEE gives the quantile function, rNEE generates random deviates and hNEE gives the hazard function.

Author(s)

Juliana Garcia, <juliana.garciav@udea.edu.co>

References

Hassan, Anwar, I. H. Dar, and M. A. Lone. "A New Class of Probability Distributions With An Application to Engineering Data." Pakistan Journal of Statistics and Operation Research 20.2 (2024): 217-231.

See Also

NEE

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dNEE(x, mu=0.2, sigma=0.3),
      from=0, to=8, col="cadetblue3", las=1, ylab="f(x)")

curve(dNEE(x, mu=1, sigma=4),
      add=TRUE, col= "purple")

curve(dNEE(x, mu=1.5, sigma=22),
      add=TRUE, col="goldenrod")

curve(dNEE(x, mu=0.5, sigma=2),
      add=TRUE, col="green3")

legend("topright", col=c("cadetblue3", "purple", "goldenrod", "green3"), lty=1, bty="n",
       legend=c("mu=0.2, sigma=0.3",
                "mu=1.0, sigma=4",
                "mu=1.5, sigma=22",
                "mu=0.5, sigma=2"))

# Example 2
# Checking if the cumulative curves converge to 1
curve(pNEE(x, mu=0.2, sigma=0.3), ylim=c(0, 1),
      from=0, to=8, col="cadetblue3", las=1, ylab="F(x)")

curve(pNEE(x, mu=1, sigma=4),
      add=TRUE, col= "purple")

curve(pNEE(x, mu=1.5, sigma=22),
      add=TRUE, col="goldenrod")
```

```
curve(pNEE(x, mu=0.5, sigma=2),
      add=TRUE, col="green3")

legend("bottomright", col=c("cadetblue3", "purple", "goldenrod", "green3"), lty=1, bty="n",
       legend=c("mu=0.2, sigma=0.3",
                "mu=1.0, sigma=4",
                "mu=1.5, sigma=22",
                "mu=0.5, sigma=2"))

# Example 3
# Checking the quantile function
mu <- 0.5
sigma <- 2
p <- seq(from=0, to=0.999, length.out=100)
plot(x=qNEE(p, mu=mu, sigma=sigma), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pNEE(x, mu=mu, sigma=sigma), from=0, add=TRUE, col="red")

# Example 4
# Comparing the random generator output with
# the theoretical probabilities
mu <- 0.5
sigma <- 2
x <- rNEE(n=10000, mu=mu, sigma=sigma)
hist(x, freq=FALSE)
curve(dNEE(x, mu=mu, sigma=sigma), col="tomato", add=TRUE)
```

---

dOW *The Odd Weibull Distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Odd Weibull distribution with parameters mu, sigma and nu.

Usage

```
dOW(x, mu, sigma, nu, log = FALSE)

pOW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qOW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rOW(n, mu, sigma, nu)

hOW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter one.
sigma	parameter two.
nu	parameter three.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[T <= t], otherwise, P[T > t].
p	vector of probabilities.
n	number of observations.

Details

The Odd Weibull with parameters mu, sigma and nu has density given by

$$f(x) = \left(\frac{\sigma\nu}{x}\right)(\mu x)^{\sigma} e^{(\mu x)^{\sigma}} \left(e^{(\mu x)^{\sigma}} - 1\right)^{\nu-1} \left[1 + \left(e^{(\mu x)^{\sigma}} - 1\right)^{\nu}\right]^{-2}$$

for $x > 0$.

Value

dOW gives the density, pOW gives the distribution function, qOW gives the quantile function, rOW generates random deviates and hOW gives the hazard function.

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

References

Cooray, K. (2006). Generalization of the Weibull distribution: the odd Weibull family. Statistical Modelling, 6(3), 265-277.

See Also

OW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dOW(x, mu=2, sigma=3, nu=0.2), from=0, to=4, ylim=c(0, 2),
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pOW(x, mu=2, sigma=3, nu=0.2), from=0, to=4, ylim=c(0, 1),
      col="red", las=1, ylab="F(x)")
curve(pOW(x, mu=2, sigma=3, nu=0.2, lower.tail=FALSE), from=0,
```

```
      to=4,  ylim=c(0, 1), col="red", las=1,
      ylab = "R(x)")

## The quantile function
p <- seq(from=0, to=0.998, length.out=100)
plot(x = qOW(p, mu=2, sigma=3, nu=0.2), y=p, xlab="Quantile", las=1,
     ylab="Probability")
curve(pOW(x, mu=2, sigma=3, nu=0.2), from=0, add=TRUE, col="red")

## The random function
hist(rOW(n=10000, mu=2, sigma = 3, nu = 0.2), freq=FALSE, ylim = c(0, 2),
     xlab = "x", las = 1, main = "")
curve(dOW(x, mu=2, sigma=3, nu=0.2),  from=0, ylim=c(0, 2), add=TRUE,
      col = "red")

## The Hazard function
par(mfrow=c(1,1))
curve(hOW(x, mu=2, sigma=3, nu=0.2), from=0, to=2.5, ylim=c(0, 3),
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dPL *The Power Lindley distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Power Lindley distribution with parameters mu and sigma.

Usage

```
dPL(x, mu, sigma, log = FALSE)

pPL(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qPL(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rPL(n, mu, sigma)

hPL(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).

lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Power Lindley Distribution with parameters mu and sigma has density given by

$f(x) = \frac{\mu\sigma^2}{\sigma+1}(1 + x^\mu)x^{\mu-1}\exp(-\sigma x^\mu)$,

for $x > 0$.

Value

dPL gives the density, pPL gives the distribution function, qPL gives the quantile function, rPL generates random deviates and hPL gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Ghitany, M. E., Al-Mutairi, D. K., Balakrishnan, N., & Al-Enezi, L. J. (2013). Power Lindley distribution and associated inference. Computational Statistics & Data Analysis, 64, 20-33.

See Also

PL

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dPL(x, mu=1.5, sigma=0.2), from=0.1, to=10,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pPL(x, mu=1.5, sigma=0.2),
      from=0.1, to=10, col="red", las=1, ylab="F(x)")
curve(pPL(x, mu=1.5, sigma=0.2, lower.tail=FALSE),
      from=0.1, to=10, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qPL(p, mu=1.5, sigma=0.2), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pPL(x, mu=1.5, sigma=0.2), from=0.1, add=TRUE, col="red")
```

```
## The random function
hist(rPL(n=1000, mu=1.5, sigma=0.2), freq=FALSE,
     xlab="x", las=1, main="")
curve(dPL(x, mu=1.5, sigma=0.2), from=0.1, to=15, add=TRUE, col="red")

## The Hazard function
par(mfrow=c(1,1))
curve(hPL(x, mu=1.5, sigma=0.2), from=0.1, to=15,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dQXGP *The Quasi XGamma Poisson distribution*

Description

Density, distribution function,quantile function, random generation and hazard function for the Quasi XGamma Poisson distribution with parameters mu, sigma and nu.

Usage

```
dQXGP(x, mu, sigma, nu, log = FALSE)

pQXGP(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qQXGP(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rQXGP(n, mu, sigma, nu)

hQXGP(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Quasi XGamma Poisson distribution with parameters mu, sigma and nu has density given by:

$f(x) = K(\mu,\sigma,\nu)(\frac{\sigma^2 x^2}{2} + \mu)exp(\frac{\nu exp(-\sigma x)(1+\mu+\sigma x+\frac{\sigma^2 x^2}{2})}{1+\mu} - \sigma x)$,

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 1$.

where

$K(\mu,\sigma,\nu) = \frac{\nu\sigma}{(exp(\nu)-1)(1+\mu)}$

Value

dQXGP gives the density, pQXGP gives the distribution function, qQXGP gives the quantile function, rQXGP generates random deviates and hQXGP gives the hazard function.

Author(s)

Simon Zapata

References

Sen, S., Korkmaz, M. Ç., & Yousof, H. M. (2018). The quasi XGamma-Poisson distribution: properties and application. Istatistik Journal of The Turkish Statistical Association, 11(3), 65-76.

See Also

QXGP

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dQXGP(x, mu=0.5, sigma=1, nu=1), from=0.1, to=8,
      ylim=c(0, 0.6), col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pQXGP(x, mu=0.5, sigma=1, nu=1),
      from=0.1, to=8,  col="red", las=1, ylab="F(x)")
curve(pQXGP(x,  mu=0.5, sigma=1, nu=1, lower.tail=FALSE),
      from=0.1, to=8, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qQXGP(p, mu=0.5, sigma=1, nu=1), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pQXGP(x, mu=0.5, sigma=1, nu=1),
      from=0.1, add=TRUE, col="red")

## The random function
hist(rQXGP(n=1000, mu=0.5, sigma=1, nu=1), freq=FALSE,
```

```
     xlab="x", ylim=c(0, 0.4), las=1, main="", xlim=c(0, 15))
curve(dQXGP(x, mu=0.5, sigma=1, nu=1),
      from=0.001, to=500, add=TRUE, col="red")

## The Hazard function
curve(hQXGP(x, mu=0.5, sigma=1, nu=1), from=0.01, to=3,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dRNMW *The Reduced New Modified Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the reduced new modified Weibull distribution with parameters mu, sigma and nu.

Usage

```
dRNMW(x, mu, sigma, nu, log = FALSE)

pRNMW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qRNMW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rRNMW(n, mu, sigma, nu)

hRNMW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter one.
sigma	parameter two.
nu	parameter three.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[T <= t], otherwise, P[T > t].
p	vector of probabilities.
n	number of observations.

Details

The reduced new modified Weibull with parameters mu, sigma and nu has density given by

$$f(x) = \frac{1}{2\sqrt{x}}\left(\mu + \sigma(1+2\nu x)e^{\nu x}\right) e^{-\mu\sqrt{x}-\sigma\sqrt{x}e^{\nu x}}$$

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dRNMW gives the density, pRNMW gives the distribution function, qRNMW gives the quantile function, rRNMW generates random deviates and hRNMW gives the hazard function.

Author(s)

Jaime Mosquera, <jmosquerag@unal.edu.co>

References

Almalki, S. J. (2018). A reduced new modified Weibull distribution. Communications in Statistics-Theory and Methods, 47(10), 2297-2313.

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(
    dRNMW(x, mu = 0.05, sigma = 0.00025, nu = 2.2),
    from = 0, to = 5, col = "red", las = 1, ylab = "f(x)"
)

## The cualphalative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(
    pRNMW(x, mu = 0.05, sigma = 0.00025, nu = 2.2),
    from = 0, to = 5, ylim = c(0, 1),
    col = "red", las = 1, ylab = "F(x)"
)
curve(
    pRNMW(
        x, mu = 0.05, sigma = 0.00025, nu = 2.2,
        lower.tail = FALSE
    ),
    from = 0, to = 5, ylim = c(0, 1),
    col = "red", las = 1, ylab = "R(x)"
)

## The quantile function
p <- seq(from = 0, to = 0.999, length.out = 100)
plot(
    x = qRNMW(p, mu = 0.05, sigma = 0.00025, nu = 2.2),
    y = p, xlab = "Quantile", las = 1,
    ylab = "Probability"
)
curve(
    pRNMW(x, mu = 0.05, sigma = 0.00025, nu = 2.2),
    from = 0, add = TRUE, col = "red"
)

## The random function
```

```
hist(
    rRNMW(n = 10000, mu = 0.05, sigma = 0.00025, nu = 2.2),
    freq = FALSE, xlab = "x", las = 1, main = "", ylim = c(0,0.8)
)
curve(dRNMW(x, mu = 0.05, sigma = 0.00025, nu = 2.2),
    from = 0, add = TRUE, col = "red"
)

## The Hazard function
par(mfrow = c(1, 1))
curve(
    hRNMW(x, mu = 0.003, sigma = 5e-6, nu = 0.025),
    from = 0, to = 250, col = "red",
    ylab = "Hazard function", las = 1
)

par(old_par) # restore previous graphical parameters
```

---

dRW *The Reflected Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Reflected Weibull Distribution with parameters mu and sigma.

Usage

```
dRW(x, mu, sigma, log = FALSE)

pRW(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qRW(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rRW(n, mu, sigma)

hRW(x, mu, sigma)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Reflected Weibull Distribution with parameters mu and sigma has density given by

$f(x) = \mu\sigma(-x)^{\sigma-1}e^{-\mu(-x)^{\sigma}}$,

for $x < 0$.

Value

dRW gives the density, pRW gives the distribution function, qRW gives the quantile function, rRW generates random deviates and hRW gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Cohen, A. C. (1973). The reflected Weibull distribution. Technometrics, 15(4), 867-873.

See Also

RW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dRW(x, mu=1, sigma=1), from=-5, to=-0.01,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pRW(x, mu=1, sigma=1),
      from=-5, to=-0.01, col="red", las=1, ylab="F(x)")
curve(pRW(x, mu=1, sigma=1, lower.tail=FALSE),
      from=-5, to=-0.01, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qRW(p, mu=1, sigma=1), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pRW(x, mu=1, sigma=1), from=-5, add=TRUE, col="red")

## The random function
hist(rRW(n=10000, mu=1, sigma=1), freq=FALSE,
     xlab="x", las=1, main="")
curve(dRW(x, mu=1, sigma=1), from=-5, to=-0.01, add=TRUE, col="red")
```

```
## The Hazard function
par(mfrow=c(1,1))
curve(hRW(x, mu=1, sigma=1), from=-0.3, to=-0.01,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

---

dSZMW *The Sarhan and Zaindin's Modified Weibull distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for Sarhan and Zaindins modified weibull distribution with parameters mu, sigma and nu.

Usage

```
dSZMW(x, mu, sigma, nu, log = FALSE)

pSZMW(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qSZMW(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rSZMW(n, mu, sigma, nu)

hSZMW(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	scale parameter.
sigma	shape parameter.
nu	shape parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Sarhan and Zaindins modified weibull with parameters mu, sigma and nu has density given by

$f(x) = (\mu + \sigma\nu x^{\nu-1}) \exp(-\mu x - \sigma x^{\nu})$

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dSZMW gives the density, pSZMW gives the distribution function, qSZMW gives the quantile function, rSZMW generates random deviates and hSZMW gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Sarhan, A. M., & Zaindin, M. (2009). Modified Weibull distribution. APPS. Applied Sciences, 11, 123-136.

See Also

SZMW

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dSZMW(x, mu = 2, sigma = 1.5, nu = 0.2), from = 0, to = 2,
      ylim = c(0, 1.7), col = "red", las = 1, ylab = "f(x)")
## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pSZMW(x, mu = 2, sigma = 1.5, nu = 0.2), from = 0, to = 2, ylim = c(0, 1),
      col = "red", las = 1, ylab = "F(x)")
curve(pSZMW(x, mu = 2, sigma = 1.5, nu = 0.2, lower.tail = FALSE), from = 0,
      to = 2, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qSZMW(p = p, mu = 2, sigma = 1.5, nu = 0.2), y = p, xlab = "Quantile",
     las = 1, ylab = "Probability")
curve(pSZMW(x, mu = 2, sigma = 1.5, nu = 0.2), from = 0, add = TRUE, col = "red")

## The random function
hist(rSZMW(n = 1000, mu = 2, sigma = 1.5, nu = 0.2), freq = FALSE, xlab = "x",
     las = 1, main = "")
curve(dSZMW(x, mu = 2, sigma = 1.5, nu = 0.2),  from = 0, add = TRUE, col = "red")

## The Hazard function
par(mfrow=c(1,1))
curve(hSZMW(x, mu = 2, sigma = 1.5, nu = 0.2), from = 0, to = 3, ylim = c(0, 8),
      col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

dWALD *The Wald distribution*

Description

These functions define the density, distribution function, quantile function and random generation for the Wald distribution with parameter μ and σ.

Usage

```
dWALD(x, mu, sigma, log = FALSE)

pWALD(q, mu, sigma, lower.tail = TRUE, log.p = FALSE)

qWALD(p, mu, sigma, lower.tail = TRUE, log.p = FALSE)

rWALD(n, mu, sigma)
```

Arguments

x, q	vector of (non-negative integer) quantiles.
mu	vector of the mu parameter.
sigma	vector of the sigma parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of random values to return.

Details

The Wald distribution with parameters μ and σ has density given by

$f(x|\mu,\sigma) = \frac{\sigma}{\sqrt{2\pi x^3}} \exp\left[-\frac{(\sigma-\mu x)^2}{2x}\right],$

for $x < 0$.

Value

dWALD gives the density, pWALD gives the distribution function, qWALD gives the quantile function, rWALD generates random deviates.

Author(s)

Sofia Cuartas, <scuartasg@unal.edu.co>

References

Heathcote, A. (2004). Fitting Wald and ex-Wald distributions to response time data: An example using functions for the S-PLUS package. Behavior Research Methods, Instruments, & Computers, 36, 678-694.

See Also

WALD

WALD.

Examples

```
# Example 1
# Plotting the mass function for different parameter values
curve(dWALD(x, mu=1, sigma=1),
      from=0, to=3, col="cadetblue3", las=1, ylab="f(x)")

curve(dWALD(x, mu=1, sigma=2),
      add=TRUE, col= "purple")

curve(dWALD(x, mu=2, sigma=4),
      add=TRUE, col="goldenrod")

legend("topright", col=c("cadetblue3", "purple", "goldenrod"),
       lty=1, bty="n",
       legend=c("mu=1, sigma=1",
                "mu=1, sigma=2",
                "mu=2, sigma=4"))

# Example 2
# Checking if the cumulative curves converge to 1
curve(pWALD(x, mu=1, sigma=1), ylim=c(0, 1),
      from=0, to=5, col="cadetblue3", las=1, ylab="F(x)")

curve(pWALD(x, mu=1, sigma=2),
      add=TRUE, col= "purple")

curve(pWALD(x, mu=2, sigma=4),
      add=TRUE, col="goldenrod")

legend("bottomright", col=c("cadetblue3", "purple", "goldenrod"),
       lty=1, bty="n",
       legend=c("mu=1, sigma=1",
                "mu=1, sigma=2",
                "mu=2, sigma=4"))

# Example 3
# Checking the quantile function
mu <- 1
sigma <- 2
p <- seq(from=0, to=0.999, length.out=100)
```

```
plot(x=qWALD(p, mu=mu, sigma=sigma), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pWALD(x, mu=mu, sigma=sigma), from=0, add=TRUE, col="red")

# Example 4
# Comparing the random generator output with
# the theoretical probabilities
mu <- 1
sigma <- 20
x <- rWALD(n=10000, mu=mu, sigma=sigma)
hist(x, freq=FALSE)
curve(dWALD(x, mu=mu, sigma=sigma), col="tomato", add=TRUE)
```

---

dWG *The Weibull Geometric distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the weibull geometric distribution with parameters mu, sigma and nu.

Usage

```
dWG(x, mu, sigma, nu, log = FALSE)

pWG(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qWG(p, sigma, mu, nu, lower.tail = TRUE, log.p = FALSE)

rWG(n, mu, sigma, nu)

hWG(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	scale parameter.
sigma	shape parameter.
nu	parameter of geometric random variable.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Weibull geometric distribution with parameters mu, sigma and nu has density given by
$f(x) = (\sigma\mu^{\sigma}(1-\nu)x^(\sigma-1)\exp(-(\mu x)^{\sigma}))(1-\nu\exp(-(\mu x)^{\sigma}))^{-2}$,
for $x > 0$, $\mu > 0$, $\sigma > 0$ and $0 < \nu < 1$.

Value

dWG gives the density, pWG gives the distribution function, qWG gives the quantile function, rWG generates random deviates and hWG gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Barreto-Souza, W., de Morais, A. L., & Cordeiro, G. M. (2011). The Weibull-geometric distribution. Journal of Statistical Computation and Simulation, 81(5), 645-657.

See Also

WG

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dWG(x, mu = 0.9, sigma = 2, nu = 0.5), from = 0, to = 3,
ylim = c(0, 1.1), col = "red", las = 1, ylab = "f(x)")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pWG(x, mu = 0.9, sigma = 2, nu = 0.5), from = 0, to = 3,
ylim = c(0, 1), col = "red", las = 1, ylab = "F(x)")
curve(pWG(x, mu = 0.9, sigma = 2, nu = 0.5, lower.tail = FALSE),
from = 0, to = 3, ylim = c(0, 1), col = "red", las = 1, ylab = "R(x)")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qWG(p = p, mu = 0.9, sigma = 2, nu = 0.5), y = p,
xlab = "Quantile", las = 1, ylab = "Probability")
curve(pWG(x,mu = 0.9, sigma = 2, nu = 0.5), from = 0, add = TRUE,
col = "red")

## The random function
hist(rWG(1000, mu = 0.9, sigma = 2, nu = 0.5), freq = FALSE, xlab = "x",
ylim = c(0, 1.8), las = 1, main = "")
curve(dWG(x, mu = 0.9, sigma = 2, nu = 0.5),  from = 0, add = TRUE,
col = "red", ylim = c(0, 1.8))
```

```
## The Hazard function(
par(mfrow=c(1,1))
curve(hWG(x, mu = 0.9, sigma = 2, nu = 0.5), from = 0, to = 8,
ylim = c(0, 12), col = "red", ylab = "Hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

---

dWGEE *The Weighted Generalized Exponential-Exponential distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Weighted Generalized Exponential-Exponential distribution with parameters mu, sigma and nu.

Usage

```
dWGEE(x, mu, sigma, nu, log = FALSE)

pWGEE(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qWGEE(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rWGEE(n, mu, sigma, nu)

hWGEE(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Weighted Generalized Exponential-Exponential Distribution with parameters mu, sigma and nu has density given by

$f(x) = \sigma\nu \exp(-\nu x)(1 - \exp(-\nu x))^{\sigma-1}(1 - \exp(-\mu\nu x))/1 - \sigma B(\mu + 1, \sigma),$

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

dWGEE gives the density, pWGEE gives the distribution function, qWGEE gives the quantile function, rWGEE generates random deviates and hWGEE gives the hazard function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Mahdavi, A. (2015). Two weighted distributions generated by exponential distribution. Journal of Mathematical Extension, 9, 1-12.

See Also

WGEE

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dWGEE(x, mu = 5, sigma = 0.5, nu = 1), from = 0, to = 6,
ylim = c(0, 1), col = "red", las = 1, ylab = "The probability density function")

## The cumulative distribution and the Reliability function
par(mfrow = c(1, 2))
curve(pWGEE(x, mu = 5, sigma = 0.5, nu = 1), from = 0, to = 6,
ylim = c(0, 1), col = "red", las = 1, ylab = "The cumulative distribution function")
curve(pWGEE(x, mu = 5, sigma = 0.5, nu = 1, lower.tail = FALSE),
from = 0, to = 6, ylim = c(0, 1), col = "red", las = 1, ylab = "The Reliability function")

## The quantile function
p <- seq(from = 0, to = 0.99999, length.out = 100)
plot(x = qWGEE(p = p, mu = 5, sigma = 0.5, nu = 1), y = p,
xlab = "Quantile", las = 1, ylab = "Probability")
curve(pWGEE(x, mu = 5, sigma = 0.5, nu = 1), from = 0, add = TRUE,
col = "red")

## The random function
hist(rWGEE(1000, mu = 5, sigma = 0.5, nu = 1), freq = FALSE, xlab = "x",
ylim = c(0, 1), las = 1, main = "")
curve(dWGEE(x, mu = 5, sigma = 0.5, nu = 1),  from = 0, add = TRUE,
col = "red", ylim = c(0, 1))

## The Hazard function(
par(mfrow=c(1,1))
curve(hWGEE(x, mu = 5, sigma = 0.5, nu = 1), from = 0, to = 6,
ylim = c(0, 1.4), col = "red", ylab = "The hazard function", las = 1)

par(old_par) # restore previous graphical parameters
```

dWP *The Weibull Poisson distribution*

Description

Density, distribution function, quantile function, random generation and hazard function for the Weibull Poisson distribution with parameters mu, sigma and nu.

Usage

```
dWP(x, mu, sigma, nu, log = FALSE)

pWP(q, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

qWP(p, mu, sigma, nu, lower.tail = TRUE, log.p = FALSE)

rWP(n, mu, sigma, nu)

hWP(x, mu, sigma, nu)
```

Arguments

x, q	vector of quantiles.
mu	parameter.
sigma	parameter.
nu	parameter.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are P[X <= x], otherwise, P[X > x].
p	vector of probabilities.
n	number of observations.

Details

The Weibull Poisson distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu e^{-\nu}}{1-e^{-\nu}} x^{\mu-1} \exp(-\sigma x^{\mu} + \nu \exp(-\sigma x^{\mu}))$,

for $x > 0$.

Value

dWP gives the density, pWP gives the distribution function, qWP gives the quantile function, rWP generates random deviates and hWP gives the hazard function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Lu, Wanbo, and Daimin Shi. "A new compounding life distribution: the Weibull–Poisson distribution." Journal of applied statistics 39.1 (2012): 21-38.

See Also

WP

Examples

```
old_par <- par(mfrow = c(1, 1)) # save previous graphical parameters

## The probability density function
curve(dWP(x, mu=1.5, sigma=0.5, nu=10), from=0.0001, to=2,
      col="red", las=1, ylab="f(x)")

## The cumulative distribution and the Reliability function
par(mfrow=c(1, 2))
curve(pWP(x, mu=1.5, sigma=0.5, nu=10),
      from=0.0001, to=2, col="red", las=1, ylab="F(x)")
curve(pWP(x, mu=1.5, sigma=0.5, nu=10, lower.tail=FALSE),
      from=0.0001, to=2, col="red", las=1, ylab="R(x)")

## The quantile function
p <- seq(from=0, to=0.99999, length.out=100)
plot(x=qWP(p, mu=1.5, sigma=0.5, nu=10), y=p, xlab="Quantile",
     las=1, ylab="Probability")
curve(pWP(x, mu=1.5, sigma=0.5, nu=10),
      from=0, add=TRUE, col="red")

## The random function
hist(rWP(n=10000, mu=1.5, sigma=0.5, nu=10), freq=FALSE,
     xlab="x", ylim=c(0, 2.2), las=1, main="")
curve(dWP(x, mu=1.5, sigma=0.5, nu=10),
      from=0.001, to=4, add=TRUE, col="red")

## The Hazard function
curve(hWP(x, mu=1.5, sigma=0.5, nu=10), from=0.001, to=5,
      col="red", ylab="Hazard function", las=1)

par(old_par) # restore previous graphical parameters
```

EEG *The Extended Exponential Geometric family*

Description

The Extended Exponential Geometric family

Usage

```
EEG(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Extended Exponential Geometric distribution with parameters mu and sigma has density given by

$f(x) = \mu\sigma \exp(-\mu x)(1-(1-\sigma)\exp(-\mu x))^{-2}$,

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

Value

Returns a gamlss.family object which can be used to fit a EEG distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Adamidis, K., Dimitrakopoulou, T., & Loukas, S. (2005). On an extension of the exponential-geometric distribution. Statistics & probability letters, 73(3), 259-269.

See Also

dEEG

Examples

```
# Generating some random values with
# known mu, sigma, nu and tau
y <- rEEG(n=100, mu = 1, sigma =1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, family=EEG,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what='mu'))
```

```
exp(coef(mod, what='sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.1, max=0.2)
x2 <- runif(n, min=0.1, max=0.15)
mu <- exp(0.75 - x1)
sigma <- exp(0.5 - x2)
x <- rEEG(n=n, mu, sigma)

mod <- gamlss(x~x1, sigma.fo=~x2, family=EEG,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

EGG *The four parameter Exponentiated Generalized Gamma family*

Description

The four parameter Exponentiated Generalized Gamma distribution

Usage

```
EGG(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.
tau.link	defines the tau.link, with "log" link as the default for the tau parameter.

Details

Four parameter Exponentiated Generalized Gamma distribution with parameters mu, sigma, nu and tau has density given by

$$f(x) = \frac{\nu\sigma}{\mu\Gamma(\tau)}\left(\frac{x}{\mu}\right)^{\sigma\tau-1}\exp\left\{-\left(\frac{x}{\mu}\right)^{\sigma}\right\}\left\{\gamma_1\left(\tau,\left(\frac{x}{\mu}\right)^{\sigma}\right)\right\}^{\nu-1},$$

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a EGG distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Cordeiro, G. M., Ortega, E. M., & Silva, G. O. (2011). The exponentiated generalized gamma distribution with application to lifetime data. Journal of statistical computation and simulation, 81(7), 827-842.

See Also

dEGG

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau

set.seed(123456)
y <- rEGG(n=100, mu=0.1, sigma=0.8, nu=10, tau=1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1,
              family=EGG,
              control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what="mu"))
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))


# Example 2
# Generating random values under some model


# A function to simulate a data set with Y ~ EGG
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(-0.8 + -3 * x1)
  sigma <- exp(0.77 - 2 * x2)
  nu    <- 10
  tau   <- 1.5
```

```
  y <- rEGG(n=n, mu=mu, sigma=sigma, nu=nu, tau)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(12345)
dat <- gendat(n=200)

mod <- gamlss(y~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~1,
              family=EGG, data=dat,
              control=gamlss.control(n.cyc=500, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))
```

EMWEx *The Exponentiated Modifien Weibull Extension family*

Description

The Exponentiated Modifien Weibull Extension family

Usage

```
EMWEx(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.
tau.link	defines the tau.link, with "log" link as the default for the tau parameter.

Details

The Beta-Weibull distribution with parameters mu, sigma, nu and tau has density given by
$f(x) = \nu\sigma\tau(\frac{x}{\mu})^{\sigma-1}\exp((\frac{x}{\mu})^{\sigma} + \nu\mu(1-\exp((\frac{x}{\mu})^{\sigma})))(1-\exp(\nu\mu(1-\exp((\frac{x}{\mu})^{\sigma}))))^{\tau-1}$,
for $x > 0$, $\nu > 0$, $\mu > 0$, $\sigma > 0$ and $\tau > 0$.

Value

Returns a gamlss.family object which can be used to fit a EMWEx distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Sarhan, A. M., & Apaloo, J. (2013). Exponentiated modified Weibull extension distribution. Reliability Engineering & System Safety, 112, 137-144.

See Also

dEMWEx

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
y <- rEMWEx(n=100, mu = 1, sigma =1.21, nu=1, tau=2)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family=EMWEx,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))
exp(coef(mod, what='tau'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(0.75 - x1)
sigma <- exp(0.5 - x2)
nu <- 1
tau <- 2
x <- rEMWEx(n=n, mu, sigma, nu, tau)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~1, family=EMWEx,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

```
exp(coef(mod, what="tau"))
```

EOFNH *The Extended Odd Frechet-Nadarajah-Haghighi family*

Description

The Extended Odd Frechet-Nadarjad-Hanhighi family

Usage

```
EOFNH(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.
tau.link	defines the tau.link, with "log" link as the default for the tau parameter.

Details

The Extended Odd Frechet-Nadarajah-Haghighi distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = \frac{\mu\sigma\nu\tau(1+\nu x)^{\sigma-1}e^{(1-(1+\nu x)^{\sigma})}[1-(1-e^{(1-(1+\nu x)^{\sigma})})^{\mu}]^{\tau-1}}{(1-e^{(1-(1+\nu x)^{\sigma})})^{\mu\tau+1}} e^{-[(1-e^{(1-(1+\nu x)^{\sigma})})^{-\mu}-1]^{\tau}}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 0$ and $\tau > 0$.

Value

Returns a gamlss.family object which can be used to fit a EOFNH distribution in the gamlss() function.

Author(s)

Helber Santiago Padilla, <hspadillar@unal.edu.co>

References

Nasiru, S. (2018). Extended Odd Fréchet-G Family of Distributions Journal of Probability and Statistics, 2018(1), 2931326.

See Also

dEOFNH

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
set.seed(123)
y <- rEOFNH(n=100, mu=1, sigma=2.1, nu=0.8, tau=1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family=EOFNH,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what="mu"))
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))

# Example 2
# Generating random values under the model
n <- 100
x1 <- runif(n)
x2 <- runif(n)
mu <- exp(0.5 - 1.2 * x1)
sigma <- 2.1
nu <- 0.8
tau <- 1
y <- rEOFNH(n=n, mu, sigma, nu, tau)

mod <- gamlss(y~x1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family=EOFNH,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))
```

---

equipment *Electronic equipment data*

Description

Time to failure in hours of 18 units of the same electronic device.

Usage

```
data(equipment)
```

Format

A vector with 18 observations.

Examples

```
data(equipment)
hist(equipment, main="", xlab="Time (h)")
```

---

estim_mu_sigma_GLIN *estim_mu_sigma_GLIN*

Description

This function generates initial values for the GLIN distribution

Usage

```
estim_mu_sigma_GLIN(y)
```

Arguments

y	vector with the random sample

Examples

```
y <- rGLIN(n = 100, mu = 3, sigma = 1.2)
estim_mu_sigma_GLIN(y = y)
```

EW *The Exponentiated Weibull family*

Description

The Exponentiated Weibull distribution

Usage

```
EW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Exponentiated Weibull Distribution with parameters mu, sigma and nu has density given by

$f(x) = \nu\mu\sigma x^{\sigma-1}\exp(-\mu x^{\sigma})(1-\exp(-\mu x^{\sigma}))^{\nu-1}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a EW distribution in the gamlss() function.

See Also

dEW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
# Will not be run this example because high number is cycles
# is needed in order to get good estimates
## Not run:
y <- rEW(n=100, mu=2, sigma=1.5, nu=0.5)

# Fitting the model
require(gamlss)
mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='EW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

## End(Not run)

# Example 2
# Generating random values under some model
# Will not be run this example because high number is cycles
# is needed in order to get good estimates
## Not run:
n <- 200
x1 <- rpois(n, lambda=2)
x2 <- runif(n)
mu <- exp(2 + -3 * x1)
sigma <- exp(3 - 2 * x2)
nu <- 2
x <- rEW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=EW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))
```

```
coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))

## End(Not run)
```

EXL *The exponentiated XLindley family*

Description

The function `EXL()` defines The exponentiated XLindley, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
EXL(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The exponentiated XLindley with parameters `mu` and `sigma` has density given by

$$f(x) = \frac{\sigma\mu^2(2+\mu+x)\exp(-\mu x)}{(1+\mu)^2}\left[1-\left(1+\frac{\mu x}{(1+\mu)^2}\right)\exp(-\mu x)\right]^{\sigma-1}$$

for $x \geq 0$, $\mu \geq 0$ and $\sigma \geq 0$.

Note: In this implementation we changed the original parameters δ for μ and α for σ we did it to implement this distribution within gamlss framework.

Value

Returns a gamlss.family object which can be used to fit a EXL distribution in the `gamlss()` function.

Author(s)

Manuel Gutierrez Tangarife, <mgutierrezta@unal.edu.co>

References

Alomair, A. M., Ahmed, M., Tariq, S., Ahsan-ul-Haq, M., & Talib, J. (2024). An exponentiated XLindley distribution with properties, inference and applications. Heliyon, 10(3).

See Also

EXL.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rEXL(n=300, mu=0.75, sigma=1.3)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=EXL,
               control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))


# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ EXL
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rEXL(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=100)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=EXL, data=dat,
               control=gamlss.control(n.cyc=5000, trace=FALSE))

summary(mod2)

# Example 3
# Mortality rate due to COVID-19 for 30 days (31st March to April 30, 2020)
# recorded for the Netherlands.
# Taken from Alomair et al. (2024) page 12.

x <- c(14.918, 10.656, 12.274, 10.289, 10.832, 7.099, 5.928, 13.211,
       7.968, 7.584, 5.555, 6.027, 4.097, 3.611, 4.960, 7.498, 6.940,
       5.307, 5.048, 2.857, 2.254, 5.431, 4.462, 3.883,
       3.461, 3.647, 1.974, 1.273, 1.416, 4.235)
```

```
mod3 <- gamlss(x~1, sigma.fo=~1, family=EXL,
               control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Replicating figure 4 from Alomair et al. (2024)
# Hist and estimated pdf
hist(x, freq=FALSE)
curve(dEXL(x, mu=0.4089915, sigma=2.710467), add=TRUE,
      col="tomato", lwd=2)
# Empirical cdf and estimated ecdf
plot(ecdf(x))
curve(pEXL(x, mu=0.4089915, sigma=2.710467), add=TRUE,
      col="tomato", lwd=2)
# QQplot
qqplot(x, rEXL(n=30, mu=0.4089915, sigma=2.710467),
       col="tomato")
qqline(x, distribution=function(p) qEXL(p, mu=0.4089915, sigma=2.710467))


# Example 4
# Precipitation in inches
# Taken from Alomair et al. (2024) page 13.

# Manuel
```

ExW *The Extended Weibull family*

Description

The Extended Weibull family

Usage

```
ExW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Extended Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu x^{\sigma-1} exp(-\mu x^{\sigma})}{[1-(1-\nu)exp(-\mu x^{\sigma})]^2}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a ExW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Zhang, T., & Xie, M. (2007). Failure data analysis with extended Weibull distribution. Communications in Statistics—Simulation and Computation, 36(3), 579-592.

See Also

dExW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rExW(n=200, mu=0.3, sigma=2, nu=0.05)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='ExW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 500
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(-2 + 3 * x1)
```

```
sigma <- exp(1.3 - 2 * x2)
nu <- 0.05
x <- rExW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=ExW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

ExWALD *The Ex-Wald family*

Description

The function ExWALD() defines the Ex-wALD distribution, three-parameter continuous distribution for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
ExWALD(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Ex-Wald distribution with parameters μ, σ and ν has density given by

$f(x|\mu,\sigma,\nu) = \frac{1}{\nu}\exp(\frac{-x}{\nu} + \sigma(\mu-k))F_W(x|k,\sigma)$ for $k \geq 0$

$f(x|\mu,\sigma,\nu) = \frac{1}{\nu}\exp\left(\frac{-(\sigma-\mu)^2}{2x}\right) Re\left(w(k'\sqrt{x/2} + \frac{\sigma i}{\sqrt{2x}})\right)$ for $k < 0$

where $k = \sqrt{\mu^2 - \frac{2}{\nu}}$, $k' = \sqrt{\frac{2}{\nu} - \mu^2}$ and F_W corresponds to the cumulative function of the Wald distribution.

More details about those expressions can be found on page 680 from Heathcote (2004).

Value

Returns a gamlss.family object which can be used to fit a Ex-WALD distribution in the gamlss() function.

Author(s)

Freddy Hernandez, <fhernanb@unal.edu.co>

References

Schwarz, W. (2001). The ex-Wald distribution as a descriptive model of response times. Behavior Research Methods, Instruments, & Computers, 33, 457-469.

Heathcote, A. (2004). Fitting Wald and ex-Wald distributions to response time data: An example using functions for the S-PLUS package. Behavior Research Methods, Instruments, & Computers, 36, 678-694.

See Also

dExWALD.

Examples

```
# Example 1
# Generating random values with
# known mu, sigma and nu

mu <- 0.20
sigma <- 70
nu <- 115

set.seed(123)
y <- rExWALD(n=100, mu, sigma, nu)

library(gamlss)
mod1 <- gamlss(y~1, family=ExWALD,
               control=gamlss.control(n.cyc=1000, trace=TRUE))

exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
exp(coef(mod1, what="nu"))

# Example 2
# Generating random values under some model


# A function to simulate a data set with Y ~ ExWALD
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(-1 + 2.8 * x1) # 1.5 approximately
  sigma <- exp( 1 - 1.2 * x2) # 1.5 approximately
  nu    <- 2
  y <- rExWALD(n=n, mu=mu, sigma=sigma, nu=nu)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(1234)
dat <- gendat(n=200)

# Fitting the model
```

```
mod2 <- gamlss(y ~ x1,
               sigma.fo = ~ x2,
               nu.fo = ~ 1,
               family = ExWALD,
               data = dat,
               control = gamlss.control(n.cyc=1000,
                                        trace=TRUE))
summary(mod2)
```

FWE *The Flexible Weibull Extension family*

Description

The function FWE() defines the Flexible Weibull distribution, a two parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
FWE(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Flexible Weibull extension with parameters mu and sigma has density given by

$f(x) = (\mu + \sigma/x^2)exp(\mu x - \sigma/x)exp(-exp(\mu x - \sigma/x))$

for $x > 0$.

Value

Returns a gamlss.family object which can be used to fit a FWE distribution in the gamlss() function.

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rFWE(n=100, mu=0.75, sigma=1.3)

# Fitting the model
require(gamlss)
mod <- gamlss(y~1, sigma.fo=~1, family='FWE',
```

```
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n)
x2 <- runif(n)
mu <- exp(1.21 - 3 * x1)
sigma <- exp(1.26 - 2 * x2)
x <- rFWE(n=n, mu, sigma)

mod <- gamlss(x~x1, sigma.fo=~x2, family=FWE,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

GammaW *The Gamma Weibull family*

Description

The Gamma Weibull family

Usage

```
GammaW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Gamma Weibull distribution with parameters mu, sigma and nu has density given by
$f(x) = \frac{\sigma\mu^{\nu}}{\Gamma(\nu)} x^{\nu\sigma-1} \exp(-\mu x^{\sigma})$,
for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a GammaW distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Stacy, E. W. (1962). A generalization of the gamma distribution. The Annals of mathematical statistics, 1187-1192.

See Also

dGammaW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rGammaW(n=100, mu = 0.5, sigma = 2, nu=1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='GammaW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n     <- 200
x1    <- runif(n)
x2    <- runif(n)
mu    <- exp(1.2 -1.6 * x1)
sigma <- exp(1.1 - 1 * x2)
nu    <- 1
y     <- rGammaW(n=n, mu, sigma, nu)

mod <- gamlss(y~x1, mu.fo=~x1, sigma.fo=~x2, nu.fo=~1, family=GammaW,
              control=gamlss.control(n.cyc=50000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

GAo *The gamma family in its original parameterization*

Description

The function `GAo()` defines The gamma, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
GAo(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The gamma original with parameters `mu` and `sigma` has density given by

$f(x|\mu,\sigma) = \frac{x^{\mu-1}e^{-x/\sigma}}{\sigma^{\mu}\Gamma(\mu)}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. The parameter μ is the shape parameter and σ is the scale parameter. In this parameterization μ is the median of X, $E(X) = \mu\sigma$ and $Var(X) = \mu\sigma^2$.

Value

Returns a gamlss.family object which can be used to fit a GAo distribution in the `gamlss()` function.

References

Abramowitz M, Stegun IA (1972). Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables. Dover Publications, New York. ISBN 0486612724. Chapter 6: Gamma and Related Functions.

See Also

dGAo

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rGAo(n=100, mu=0.75, sigma=1.3)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=GAo)
```

```
# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y as GAo
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rGAo(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
dat <- gendat(n=500)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=GAo, data=dat)

summary(mod2)
```

GGD *The Generalized Gompertz family*

Description

The Generalized Gompertz family

Usage

```
GGD(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Generalized Gompertz Distribution with parameters mu, sigma and nu has density given by
$f(x) = \nu\mu \exp(-\frac{\mu}{\sigma}(\exp(\sigma x - 1)))(1 - \exp(-\frac{\mu}{\sigma}(\exp(\sigma x - 1))))^{(\nu-1)}$,
for $x \geq 0$, $\mu > 0$, $\sigma \geq 0$ and $\nu > 0$

Value

Returns a gamlss.family object which can be used to fit a GGD distribution in the `gamlss()` function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

#' El-Gohary, A., Alshamrani, A., & Al-Otaibi, A. N. (2013). The generalized Gompertz distribution. Applied mathematical modelling, 37(1-2), 13-24.

See Also

dGGD

Examples

```
#Example 1
# Generating some random values with
# known mu, sigma, nu and tau
y <- rGGD(n=1000, mu=1, sigma=0.3, nu=1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='GGD',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(0.5 - x1)
sigma <- exp(-1 - x2)
nu <- 1.5
x <- rGGD(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=GGD,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

GIW *The Generalized Inverse Weibull family*

Description

The Generalized Inverse Weibull family

Usage

```
GIW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Generalized Inverse Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \nu\sigma\mu^{\sigma}x^{-(\sigma+1)}exp\{-\nu(\frac{\mu}{x})^{\sigma}\}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a GIW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

De Gusmao, F. R., Ortega, E. M., & Cordeiro, G. M. (2011). The generalized inverse Weibull distribution. Statistical Papers, 52, 591-619.

See Also

dGIW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rGIW(n=200, mu=3, sigma=5, nu=0.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='GIW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 500
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(-1.02 + 3 * x1)
sigma <- exp(1.69 - 2 * x2)
nu <- 0.5
x <- rGIW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=GIW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

GLIN *The Generalized Lindley Type II family*

Description

The Generalized Lindley Type II (GLIN) family for fitting positive continuous lifetime data within the GAMLSS framework.

Usage

```
GLIN(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter (mu > 0).
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma parameter (sigma > 0).

Details

The Generalized Lindley Type II distribution with parameters `mu` and `sigma` has probability density function

$f(x|\mu,\sigma) = \frac{\mu^2}{\mu+1}\left(1+\frac{\mu^{\sigma-2}x^{\sigma-1}}{\Gamma(\sigma)}\right)e^{-\mu x},$

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

The distribution is a two-parameter extension of the classical Lindley distribution and belongs to the class of finite mixtures involving exponential and gamma components. It provides additional flexibility for modeling positively skewed lifetime data.

The original parameters of the distribution are denoted by θ and α. In the GAMLSS implementation, they are re-parameterized as $\mu = \theta$ and $\sigma = \alpha$.

The r-th raw moment is given by

$E(X^r) = \frac{1}{\mu^r(\mu+1)}\left[\mu\Gamma(r+1)+\frac{\Gamma(r+\sigma)}{\Gamma(\sigma)}\right].$

In particular, the mean is

$E(X) = \frac{\mu+\sigma}{\mu(\mu+1)}.$

and the variance is

$Var(X) = \frac{\mu^2+\mu(\sigma^2-\sigma+2)+\sigma}{\mu^2(\mu+1)^2}.$

The GLIN distribution has been proposed for modeling lifetime and survival data and has shown greater flexibility than the classical Lindley and Exponential distributions in several applications.

Value

Returns a gamlss.family object which can be used to fit a GLIN distribution in the `gamlss()` function.

Author(s)

Sofia Cadavid Rueda, <socadavidr@unal.edu.co>

References

Ekhosuehi, N., Opone, F., & Odobaire, F. (2018). A New Generalized Two Parameter Lindley Distribution. Journal of the Nigerian Statistical Association, 30, 547-566.

See Also

dGLIN

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
set.seed(1234)
y <- rGLIN(n=500, mu=0.75, sigma=1.3)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=GLIN)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y as GLIN
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)   # Approx 0.95
  sigma <- exp(2 - 1.5 * x2) # Approx 3.50
  y <- rGLIN(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}
set.seed(1234)
dat <- gendat(n=1000)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=GLIN, data=dat,
               control=gamlss.control(n.cyc=50, trace=FALSE))

summary(mod2)

# Example 3
# Remission times (in months) of 128 bladder cancer patients
# Taken from Lee and Wang (2003)
# Ekhosuehi et al. (2018) Table 4

y <- c(0.08, 2.09, 3.48, 4.87, 6.94, 8.66, 13.11, 23.63,
       0.20, 2.23, 3.52, 4.98, 6.97, 9.02, 13.29, 0.40,
       2.26, 3.57, 5.06, 7.09, 9.22, 13.80, 25.74, 0.50,
       2.46, 3.64, 5.09, 7.26, 9.47, 14.24, 25.82, 0.51,
       2.54, 3.70, 5.17, 7.28, 9.74, 14.76, 26.31, 0.81,
       2.62, 3.82, 5.32, 7.32, 10.06, 14.77, 32.15, 2.64,
       3.88, 5.32, 7.39, 10.34, 14.83, 34.26, 0.90, 2.69,
       4.18, 5.34, 7.59, 10.66, 15.96, 36.66, 1.05, 2.69,
       4.23, 5.41, 7.62, 10.75, 16.62, 43.01, 1.19, 2.75,
       4.26, 5.41, 7.63, 17.12, 46.12, 1.26, 2.83, 4.33,
```

```
        5.49, 7.66, 11.25, 17.14, 79.05, 1.35, 2.87, 5.62,
        7.87, 11.64, 17.36, 1.40, 3.02, 4.34, 5.71, 7.93,
        11.79, 18.10, 1.46, 4.40, 5.85, 8.26, 11.98, 19.13,
        1.76, 3.25, 4.50, 6.25, 8.37, 12.02, 2.02, 3.31,
        4.51, 6.54, 8.53, 12.03, 20.28, 2.02, 3.36, 6.76,
        12.07, 21.73, 2.07, 3.36, 6.93, 8.65, 12.63, 22.69)

require(gamlss)
mod3 <- gamlss(y ~ 1, sigma.fo = ~1, family = GLIN)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Comparing the empirical histogram with the estimated density
hist(y, breaks=15, freq=FALSE,
     xlab="y", col="lightblue", border="white")
curve(dGLIN(x, mu=0.1247079, sigma=1.189219),
      add=TRUE, col="red", lwd=2)
```

GMW *The Generalized Modified Weibull family*

Description

The Generalized modified Weibull distribution

Usage

```
GMW(mu.link = "log", sigma.link = "log", nu.link = "sqrt", tau.link = "sqrt")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "sqrt" link as the default for the nu parameter.
tau.link	defines the tau.link, with "sqrt" link as the default for the tau parameter.

Details

The Generalized modified Weibull distribution with parameters mu, sigma, nu and tau has density given by

$f(x) = \mu\sigma x^{\nu-1}(\nu + \tau x)\exp(\tau x - \mu x^{\nu}e^{\tau x})[1 - \exp(-\mu x^{\nu}e^{\tau x})]^{\sigma-1}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a GMW distribution in the gamlss() function.

See Also

dGMW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
y <- rGMW(n=100, mu=2, sigma=0.5, nu=2, tau=1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~ 1, family='GMW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
(coef(mod, what='nu'))^2
(coef(mod, what='tau'))^2

# Example 2
# Generating random values under some model
## Not run:
n <- 1000
x1 <- runif(n)
x2 <- runif(n)
mu <- exp(2 + -3 * x1)
sigma <- exp(3 - 2 * x2)
nu <- 2
tau <- 1.5
x <- rGMW(n=n, mu, sigma, nu, tau)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~ 1, family="GMW",
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
coef(mod, what="nu")^2
coef(mod, what="tau")^2

## End(Not run)
```

initValuesOW *Initial values and search region for Odd Weibull distribution*

Description

This function can be used so as to get suggestions about initial values and the search region for parameter estimation in OW distribution.

Usage

```
initValuesOW(
  formula,
  data = NULL,
  local_reg = loess.options(),
  interpolation = interp.options(),
  ...
)
```

Arguments

formula	an object of class formula with the response on the left of an operator ~. The right side must be 1.
data	an optional data frame containing the response variables. If data is not specified, the variables are taken from the environment from which initValuesOW is called.
local_reg	a list of control parameters for LOESS. See loess.options.
interpolation	a list of control parameters for interpolation function. See interp.options.
...	further arguments passed to TTTE_Analytical.

Details

This function performs a non-parametric estimation of the empirical total time on test (TTT) plot. Then, this estimated curve can be used so as to get suggestions about initial values and the search region for parameters based on hazard shape associated to the shape of empirical TTT plot.

Value

Returns an object of class c("initValOW", "HazardShape") containing:

- sigma.start value for $sigma$ parameter of OW distribution.
- nu.start value for nu parameter of OW distribution.
- sigma.valid search region for $sigma$ parameter of OW distribution.
- nu.valid search region for nu parameter of OW distribution.
- TTTplot Total Time on Test transform computed from the data.
- hazard_type shape of the hazard function determined from the TTT plot.

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

Examples

```
# Example 1
# Bathtuh hazard and its corresponding TTT plot
y1 <- rOW(n = 1000, mu = 0.1, sigma = 7, nu = 0.08)
my_initial_guess1 <- initValuesOW(formula=y1~1)
summary(my_initial_guess1)
plot(my_initial_guess1, par_plot=list(mar=c(3.7,3.7,1,2.5),
                                      mgp=c(2.5,1,0)))

curve(hOW(x, mu = 0.022, sigma = 8, nu = 0.01), from = 0,
      to = 80, ylim = c(0, 0.04), col = "red",
      ylab = "Hazard function", las = 1)

# Example 2
# Bathtuh hazard and its corresponding TTT plot with right censored data

y2 <- rOW(n = 1000, mu = 0.1, sigma = 7, nu = 0.08)
status <- c(rep(1, 980), rep(0, 20))
my_initial_guess2 <- initValuesOW(formula=Surv(y2, status)~1)
summary(my_initial_guess2)
plot(my_initial_guess2, par_plot=list(mar=c(3.7,3.7,1,2.5),
                                      mgp=c(2.5,1,0)))

curve(hOW(x, mu = 0.022, sigma = 8, nu = 0.01), from = 0,
      to = 80, ylim = c(0, 0.04), col = "red",
      ylab = "Hazard function", las = 1)
```

IPXLIN *The Inverse Power XLindley family - Hassan et al. (2025)*

Description

The Inverse Power XLindley family

Usage

```
IPXLIN(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "logit" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter.

Details

The Inverse Power XLindley distribution with parameters mu, and sigma has density given by

$f(x|\mu,\sigma) = \frac{\sigma\mu^2}{(1+\mu)^2} x^{-2\sigma-1}\left(1+(2+\mu)x^{\sigma}\right)e^{-\mu x^{-\sigma}}$

for $x > 0$, $\mu > 0$ and $\sigma > 0$. In this parameterization, μ is the scale parameter and σ is the shape parameter.

Value

Returns a gamlss.family object which can be used to fit a IPXLIN distribution in the gamlss() function.

References

Hassan, A. S., Alsadat, N., Chesneau, C., Elgarhy, M., Kayid, M., Nasiru, S., & Gemeay, A. M. (2025). Inverse power XLindley distribution with statistical inference and applications to engineering data. Scientific Reports, 15, 4385.

See Also

dIPXLIN

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rIPXLIN(n=500, mu=0.5, sigma=3.5)

# Fitting the model
require(gamlss)
mod1 <- gamlss(y~1, sigma.fo=~1, family=IPXLIN)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y as BS
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(1.45 - 3 * x1)
  sigma <- exp(2 - 1.5 * x2)
  y <- rIPXLIN(n=n, mu=mu, sigma=sigma)
  data.frame(y=y, x1=x1, x2=x2)
}
```

```
set.seed(123)
dat <- gendat(n=300)

mod2 <- gamlss(y~x1, sigma.fo=~x2,
               family=IPXLIN, data=dat)

summary(mod2)
```

IW *The Inverse Weibull family*

Description

The Inverse Weibull distribution

Usage

```
IW(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Inverse Weibull distribution with parameters mu, sigma has density given by

$f(x) = \mu\sigma x^{-\sigma-1}\exp(\mu x^{-\sigma})$

for $x > 0$, $\mu > 0$ and $\sigma > 0$

Value

Returns a gamlss.family object which can be used to fit a IW distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Drapella, A. (1993). The complementary Weibull distribution: unknown or just forgotten?. Quality and reliability engineering international, 9(4), 383-385.

See Also

dIW

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rIW(n=100, mu=5, sigma=2.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, mu.fo=~1, sigma.fo=~1, family='IW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- rpois(n, lambda=2)
x2 <- runif(n)
mu <- exp(2 + -1 * x1)
sigma <- exp(2 - 2 * x2)
x <- rIW(n=n, mu, sigma)

mod <- gamlss(x~x1, mu.fo=~1, sigma.fo=~x2, family=IW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

KumIW *The Kumaraswamy Inverse Weibull family*

Description

The Kumaraswamy Inverse Weibull family

Usage

```
KumIW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Kumaraswamy Inverse Weibull Distribution with parameters mu, sigma and nu has density given by

$f(x) = \mu\sigma\nu x^{-\mu-1} \exp -\sigma x^{-\mu}(1 - \exp -\sigma x^{-\mu})^{\nu-1}$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a KumIW distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Shahbaz, M. Q., Shahbaz, S., & Butt, N. S. (2012). The Kumaraswamy Inverse Weibull Distribution. Pakistan journal of statistics and operation research, 479-489.

See Also

dKumIW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
y <- rKumIW(n=100, mu = 1.5, sigma=  1.5, nu = 5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family="KumIW",
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what="mu"))
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
```

```
mu <- exp(1 - x1)
sigma <- exp(1 - x2)
nu <- 5
x <- rKumIW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=KumIW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

LIN *The Lindley family*

Description

The function LIN() defines the Lindley distribution with only one parameter for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
LIN(mu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.

Details

The Lindley with parameter mu has density given by

$f(x) = \frac{\mu^2}{\mu+1}(1+x)\exp(-\mu x)$,

for x > 0 and $\mu > 0$.

Value

Returns a gamlss.family object which can be used to fit a LIN distribution in the gamlss() function.

Author(s)

Freddy Hernandez <fhernanb@unal.edu.co>

References

Lindley, D. V. (1958). Fiducial distributions and Bayes' theorem. Journal of the Royal Statistical Society. Series B (Methodological), 102-107.

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rLIN(n=200, mu=2)

# Fitting the model
require(gamlss)
mod <- gamlss(y ~ 1, family="LIN")

# Extracting the fitted values for mu
# using the inverse link function
exp(coef(mod, what='mu'))

# Example 2
# Generating random values under some model
n <- 100
x1 <- runif(n=n)
x2 <- runif(n=n)
eta <- 1 + 3 * x1 - 2 * x2
mu <- exp(eta)
y <- rLIN(n=n, mu=mu)

mod <- gamlss(y ~ x1 + x2, family=LIN)

coef(mod, what='mu')
```

---

logLik_GLIN *logLik_GLIN*

Description

Auxiliary function to compute the log-likelihood of the GLIN distribution.

Usage

```
logLik_GLIN(param = c(0, 0), x)
```

Arguments

param	Numeric vector containing the values of the parameters
x	Numeric vector containing the observations.

Examples

```
y <- rGLIN(n = 100, mu = 3, sigma = 1.2)
logLik_GLIN(param = c(0, 0), x = y)
```

LW *The Log-Weibull family*

Description

The Log-Weibull distribution

Usage

```
LW(mu.link = "identity", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Log-Weibull Distribution with parameters mu and sigma has density given by

$f(y) = (1/\sigma)e^{((y-\mu)/\sigma)}exp\{-e^{((y-\mu)/\sigma)}\}$,

for $-\infty < y < \infty$.

Value

Returns a gamlss.family object which can be used to fit a LW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Gumbel, E. J. (1958). Statistics of extremes. Columbia university press.

See Also

dLW

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rLW(n=100, mu=0, sigma=1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, family= 'LW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
coef(mod, 'mu')
exp(coef(mod, 'sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- 1.5 - 3 * x1
sigma <- exp(1.4 - 2 * x2)
x <- rLW(n=n, mu, sigma)

mod <- gamlss(x~x1, sigma.fo=~x2, family=LW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

`make.link.gamlss` *Create a Link for GAMLSS families*

Description

The function `make.link.gamlss()` is used with `gamlss.family` distributions in package **gamlss()**.Given a link, it returns a link function, an inverse link function, the derivative dpar/deta where 'par' is the appropriate distribution parameter and a function for checking the domain. It differs from the usual `make.link` of `glm()` by having extra links as the `logshifto1`, and the own. For the use of the own link see the example bellow. `show.link` provides a way in which the user can identify the link functions available for each gamlss distribution. If your required link function is not available for any of the gamlss distributions you can add it in.

Usage

```
make.link.gamlss(link)
```

Arguments

link	character or numeric; one of "logit", "probit", "cloglog", "identity", "log", "sqrt", "1/mu^2", "inverse", "logshifted", "logitshifted", or number, say lambda resulting in power link μ^{λ}.

Details

The own link function is added to allow the user greater flexibility. In order to used the own link function for any of the parameters of the distribution the own link should appear in the available links for this parameter. You can check this using the function show.link. If the own do not appear in the list you can create a new function for the distribution in which own is added in the list. For example the first line of the code of the binomial distribution, BI, has change from

"mstats <- checklink("mu.link", "Binomial", substitute(mu.link), c("logit", "probit", "cloglog", "log")), in version 1.0-0 of gamlss, to

"mstats <- checklink("mu.link", "Binomial", substitute(mu.link), c("logit", "probit", "cloglog", "log", "own"))

in version 1.0-1. Given that the parameter has own as an option the user needs also to define the following four new functions in order to used an own link.

i) own.linkfun

ii) own.linkinv

iii) own.mu.eta and

iv) own.valideta.

An example is given below.

Only one parameter of the distribution at a time is allowed to have its own link, (unless the same four own functions above are suitable for more that one parameter of the distribution).

Note that from **gamlss** version 1.9-0 the user can introduce its own link function by define an appropriate function, (see the example below).

Value

For the make.link.gamlss a list with components

linkfun: Link function function(parameter)

linkinv: Inverse link function function(eta)

mu.eta: Derivative function(eta) dparameter/deta

valideta: function(eta) TRUE if all of eta is in the domain of linkinv.

For the show.link a list with components the available links for the distribution parameters

Note

For the links involving parameters as in logshifted and logitshifted the parameters can be passed in the definition of the distribution by calling the checklink function, for example in the definition of the tau parameter in BCPE distribution the following call is made: tstats <- checklink("tau.link","Box Cox Power Exponential", substitute(tau.link),c("logshifted", "log", "identity"), par.link = c(1))

This function is the same `make.link.gamlss` fuction from gamlss.dist package.

`mice` *Mice mortality data*

Description

The ages at death in weeks for male mice exposed to 240r of gamma radiation.

Usage

```
data(mice)
```

Format

A vector with 208 data points.

Examples

```
data(mice)
hist(mice, main="", xlab="Time (weeks)", freq=FALSE)
lines(density(mice), col="blue", lwd=2)
```

`MOEIW` *The Marshall-Olkin Extended Inverse Weibull family*

Description

The Marshall-Olkin Extended Inverse Weibull family

Usage

```
MOEIW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.
`nu.link`	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Marshall-Olkin Extended Inverse Weibull distribution with parameters `mu`, `sigma` and `nu` has density given by

$f(x) = \frac{\mu\sigma\nu x^{-(\sigma+1)} exp\{-\mu x^{-\sigma}\}}{\{\nu-(\nu-1)exp\{-\mu x^{-\sigma}\}\}^2}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a MOEIW distribution in the `gamlss()` function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Okasha, H. M., El-Baz, A. H., Tarabia, A. M. K., & Basheer, A. M. (2017). Extended inverse Weibull distribution with reliability application. Journal of the Egyptian Mathematical Society, 25(3), 343-349.

See Also

dMOEIW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
set.seed(123456)
y <- rMOEIW(n=100, mu=0.6, sigma=1.7, nu=0.3)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family="MOEIW",
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what="mu"))
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ MOEIW
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu    <- exp(-2.02 + 3 * x1) # 0.60 approximately
  sigma <- exp(2.23 - 2 * x2)  # 3.42 approximately
  nu    <- 2
  y <- rMOEIW(n=n, mu=mu, sigma=sigma, nu=nu)
  data.frame(y=y, x1=x1, x2=x2)
}
```

```
set.seed(123)
dat <- gendat(n=100)

mod <- gamlss(y~x1, sigma.fo=~x2, nu.fo=~1,
              family=MOEIW, data=dat,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

MOEW *The Marshall-Olkin Extended Weibull family*

Description

The Marshall-Olkin Extended Weibull family

Usage

```
MOEW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Marshall-Olkin Extended Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu(\nu x)^{\sigma-1}exp\{-(\nu x)^{\sigma}\}}{\{1-(1-\mu)exp\{-(\nu x)^{\sigma}\}\}^2}$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a MOEW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Ghitany, M. E., Al-Hussaini, E. K., & Al-Jarallah, R. A. (2005). Marshall–Olkin extended Weibull distribution and its application to censored data. Journal of Applied Statistics, 32(10), 1025-1034.

See Also

dMOEW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rMOEW(n=400, mu=0.5, sigma=0.7, nu=1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='MOEW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 500
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(-1.20 + 3 * x1)
sigma <- exp(0.84 - 2 * x2)
nu <- 1
x <- rMOEW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=MOEW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

MOK *The Marshall-Olkin Kappa family*

Description

The Marshall-Olkin Kappa family

Usage

```
MOK(mu.link = "log", sigma.link = "log", nu.link = "log", tau.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.
tau.link	defines the tau.link, with "log" link as the default for the tau parameter.

Details

The Marshall-Olkin Kappa distribution with parameters mu, sigma, nu and tau has density given by

$$f(x) = \frac{\tau\frac{\mu\nu}{\sigma}\left(\frac{x}{\sigma}\right)^{\nu-1}\left(\mu+\left(\frac{x}{\sigma}\right)^{\mu\nu}\right)^{-\frac{\mu+1}{\mu}}}{\left(\tau+(1-\tau)\left(\frac{\left(\frac{x}{\sigma}\right)^{\mu\nu}}{\mu+\left(\frac{x}{\sigma}\right)^{\mu\nu}}\right)^{\frac{1}{\mu}}\right)^{2}}$$

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a MOK distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Javed, M., Nawaz, T., & Irfan, M. (2019). The Marshall-Olkin kappa distribution: properties and applications. Journal of King Saud University-Science, 31(4), 684-691.

See Also

dMOK

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma, nu and tau
y <- rMOK(n=100, mu = 1, sigma = 3.5, nu = 3, tau = 2)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, tau.fo=~1, family=MOK,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma, nu and tau
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))
exp(coef(mod, what='tau'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(0.5 + x1)
sigma <- exp(0.8 + x2)
nu <- 1
tau <- 0.5
x <- rMOK(n=n, mu, sigma, nu, tau)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, tau.fo=~1, family=MOK,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
exp(coef(mod, what="tau"))
```

MW *The Modified Weibull family*

Description

#' The Modified Weibull distribution

Usage

```
MW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Modified Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = \mu(\sigma + \nu x)x^{\sigma-1}\exp(\nu x)\exp(-\mu x^{\sigma}\exp(\nu x))$,

for $x > 0$, $\mu > 0$, $\sigma \geq 0$ and $\nu \geq 0$.

Value

Returns a gamlss.family object which can be used to fit a MW distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Lai, C. D., Xie, M., & Murthy, D. N. P. (2003). A modified Weibull distribution. IEEE Transactions on reliability, 52(1), 33-37.

See Also

dMW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rMW(n=100, mu = 2, sigma = 1.5, nu = 0.2)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family= 'MW',
               control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))
```

```
# Example 2
# Generating random values under some model
n     <- 200
x1    <- rpois(n, lambda=2)
x2    <- runif(n)
mu    <- exp(3 -1 * x1)
sigma <- exp(2 - 2 * x2)
nu    <- 0.2
x     <- rMW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, mu.fo=~x1, sigma.fo=~x2, nu.fo=~1, family=MW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
coef(mod, what='nu')
```

`myOW_region` *Custimized region search for odd Weibull distribution*

Description

This function can be used to modify `OW` `gamlss.family` object in order to set a customized region search for `gamlss()` function.

Usage

```
myOW_region(family = OW, valid.values = "auto", initVal)
```

Arguments

`family`	The `OW` family. This arguments allows the user to modify input arguments of the family, like the `link` functions.
`valid.values`	a list of character elements specifying the region for `sigma` and/or `nu`. See **Details** and **Examples** section to learn about its use.
`initVal`	An `initValOW` object generated with `initValuesOW` function.

Details

This function was created to help users to fit `OW` distribution easily bounding the parametric space for `sigma` and `nu`.

The `valid.values` must be defined as a list of characters containing a call of the `all` function.

Value

Returns a `gamlss.family` object which can be used to fit an OW distribution in the `gamlss()` function.

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rOW(n=200, mu=0.2, sigma=4, nu=0.05)

# Custom search region
myvalues <- list(sigma="all(sigma > 1)",
                 nu="all(nu < 1) & all(nu < 1)")

my_initial_guess <- initValuesOW(formula=y~1)
summary(my_initial_guess)

# OW family modified with 'myOW_region'
require(gamlss)
myOW <- myOW_region(valid.values=myvalues, initVal=my_initial_guess)
mod1 <- gamlss(y~1, sigma.fo=~1, nu.fo=~1,
               sigma.start=param.startOW('sigma', my_initial_guess),
               nu.start=param.startOW('nu', my_initial_guess),
               control=gamlss.control(n.cyc=300, trace=FALSE),
               family=myOW)

exp(coef(mod1, what='mu'))
exp(coef(mod1, what='sigma'))
exp(coef(mod1, what='nu'))

# Example 2
# Same example using another link function and using 'myOW_region'
# in the argument 'family'
mod2 <- gamlss(y~1, sigma.fo=~1, nu.fo=~1,
               sigma.start=2, nu.start=0.1,
               control=gamlss.control(n.cyc=300, trace=FALSE),
               family=myOW_region(family=OW(sigma.link='identity'),
                                  valid.values=myvalues,
                                  initVal=my_initial_guess))

exp(coef(mod2, what='mu'))
coef(mod2, what='sigma')
exp(coef(mod2, what='nu'))
```

NEE *New Exponentiated Exponential family*

Description

The function `NEE()` defines the New Exponentiated Exponential distribution, a two parameter distribution, for a `gamlss.family` object to be used in GAMLSS fitting using the function `gamlss()`.

Usage

```
NEE(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "logit" link as the default for the sigma.

Details

The New Exponentiated Exponential distribution with parameters mu and sigma has density given by

$f(x|\mu,\sigma) = \log(2^{\sigma})\mu\exp(-\mu x)(1-\exp(-\mu x))^{\sigma-1}2^{(1-\exp(-\mu x))^{\sigma}}$,

for $x > 0$, $\mu > 0$ and $\sigma > 0$.

Note: In this implementation we changed the original parameters θ for μ and α for σ, we did it to implement this distribution within gamlss framework.

Value

Returns a gamlss.family object which can be used to fit a NEE distribution in the gamlss() function.

References

Hassan, Anwar, I. H. Dar, and M. A. Lone. "A New Class of Probability Distributions With An Application to Engineering Data." Pakistan Journal of Statistics and Operation Research 20.2 (2024): 217-231.

See Also

dNEE

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rNEE(n=500, mu=2.5, sigma=3.5)

# Fitting the model
require(gamlss)

mod1 <- gamlss(y~1, sigma.fo=~1, family=NEE,
               control=gamlss.control(n.cyc=5000, trace=TRUE))

# Extracting the fitted values for mu, sigma
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
```

```
# Example 2
# Generating random values under some model
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(-0.2 + 1.5 * x1)
  sigma <- exp(1 - 0.7 * x2)
  y <- rNEE(n=n, mu, sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

set.seed(123)
datos <- gendat(n=500)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=NEE, data=datos,
               control=gamlss.control(n.cyc=5000, trace=TRUE))

summary(mod2)

# Example 3  ------------------------------------------------
# Obtained from Hassan (2024) page 226
# The data set consists of 63 observations of the gauge lengths of 10mm.

y <- c(1.901, 2.132, 2.203, 2.228, 2.257, 2.350, 2.361, 2.396, 2.397,
       2.445, 2.454, 2.474, 2.518, 2.522, 2.525, 2.532,  2.575, 2.614,
       2.616, 2.618, 2.624, 2.659, 2.675, 2.738, 2.740, 2.856, 2.917,
       2.928, 2.937, 2.937, 2.977, 2.996,  3.030, 3.125, 3.139, 3.145,
       3.220, 3.223, 3.235, 3.243, 3.264, 3.272, 3.294, 3.332, 3.346,
       3.377, 3.408, 3.435,  3.493, 3.501, 3.537, 3.554, 3.562, 3.628,
       3.852, 3.871, 3.886, 3.971, 4.024, 4.027, 4.225, 4.395, 5.020)

mod3 <- gamlss(y~1, family=NEE)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod3, what="mu"))
exp(coef(mod3, what="sigma"))

# Hist and estimated pdf
hist(y, freq=FALSE, ylim=c(0, 0.7))
curve(dNEE(x, mu=2.076862, sigma=255.2289),
      add=TRUE, col="tomato", lwd=2)

# Empirical cdf and estimated ecdf
plot(ecdf(y))
curve(pNEE(x, mu=2.076862, sigma=255.2289),
      add=TRUE, col="tomato", lwd=2)
# QQplot
qqplot(y, rNEE(n=length(y), mu=2.076862, sigma=255.2289), col="tomato")
qqline(y, distribution=function(p) qNEE(p, mu=2.076862, sigma=255.2289))

# Example 4  ------------------------------------------------
# Obtained from Hassan (2024) page 226
```

```
# The dataset was reported by Bader and Priest (1982) on failure
# stresses (in GPa) of 65 single carbon fibers of lengths 50 mm

y <- c(0.564, 0.729, 0.802, 0.95, 1.053, 1.111, 1.115, 1.194, 1.208,
       1.216, 1.247, 1.256, 1.271, 1.277, 1.305, 1.313, 1.348,
       1.39, 1.429, 1.474, 1.49, 1.503, 1.52, 1.522, 1.524, 1.551,
       1.551, 1.609, 1.632, 1.632, 1.676, 1.684, 1.685, 1.728, 1.74,
       1.761, 1.764, 1.785, 1.804, 1.816, 1.824, 1.836, 1.879, 1.883,
       1.892, 1.898, 1.934, 1.947, 1.976, 2.02, 2.023, 2.05, 2.059,
       2.068, 2.071, 2.098, 2.13, 2.204, 2.317, 2.334, 2.34, 2.346,
       2.378, 2.483, 2.269)

mod4 <- gamlss(y~1, family=NEE)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod4, what="mu"))
exp(coef(mod4, what="sigma"))

hist(y, freq=FALSE)
curve(dNEE(x, mu=2.400515, sigma=25.15236),
      add=TRUE, col="tomato", lwd=2)

# Empirical cdf and estimated ecdf
plot(ecdf(y))
curve(pNEE(x, mu=2.400515, sigma=25.15236),
      add=TRUE, col="tomato", lwd=2)
# QQplot
qqplot(y, rNEE(n=length(y), mu=2.400515, sigma=25.15236), col="tomato")
qqline(y, distribution=function(p) qNEE(p, mu=2.400515, sigma=25.15236))

# Example 5 ------------------------------------------------------------------
# 69 Observations of the gauge lengths of 20m.
y <- c(1.312,1.314,1.479,1.552,1.700,1.803,1.861,1.865,1.944,1.958,1.966,1.997,
       2.006,2.021,2.027,2.055, 2.063,2.098,2.140,2.179,2.224,2.240,2.253,2.270,
       2.272,2.274,2.301,2.301,2.359,2.382,2.382,2.426, 2.434,2.435,2.478,2.490,
       2.511,2.514,2.535,2.554,2.566,2.570,2.586,2.629,2.633,2.642,2.648,2.684,
       2.697,2.726,2.770,2.773,2.800,2.809,2.818,2.821,2.848,2.880,2.954,3.012,
       3.067,3.084,3.090,3.096, 3.128,3.233,3.433,3.585,3.585)

mod5 <- gamlss(y~1, sigma.fo=~1, family = NEE)

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod5, what="mu"))
exp(coef(mod5, what="sigma"))

hist(y, freq=FALSE)
curve(dNEE(x, mu=2.197771, sigma=100.8888), add=TRUE,
      col="tomato", lwd=2)
# Empirical cdf and estimated ecdf
plot(ecdf(y))
curve(pNEE(x, mu=2.197771, sigma=100.8888), add=TRUE,
```

```
      col="tomato", lwd=2)
# QQplot
qqplot(y, rNEE(n=length(y), mu=2.197771, sigma=100.8888), col="tomato")
qqline(y, distribution=function(p) qNEE(p, mu=2.197771, sigma=100.8888))
```

OW *The Odd Weibull family*

Description

The function OW() defines the Odd Weibull distribution, a three parameter distribution, for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
OW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu.

Details

The odd Weibull with parameters mu, sigma and nu has density given by

$$f(t) = \left(\frac{\sigma\nu}{t}\right)(\mu t)^{\sigma} e^{(\mu t)^{\sigma}} \left(e^{(\mu t)^{\sigma}} - 1\right)^{\nu-1} \left[1 + \left(e^{(\mu t)^{\sigma}} - 1\right)^{\nu}\right]^{-2}$$

for $x > 0$.

Value

Returns a gamlss.family object which can be used to fit a OW distribution in the gamlss() function.

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

References

Cooray, K. (2006). Generalization of the Weibull distribution: the odd Weibull family. Statistical Modelling, 6(3), 265-277.

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rOW(n=200, mu=0.1, sigma=7, nu = 1.1)

# Fitting the model
require(gamlss)
mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family="OW",
              control=gamlss.control(n.cyc=500, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what="mu"))
exp(coef(mod, what="sigma"))
exp(coef(mod, what="nu"))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n)
x2 <- runif(n)
x3 <- runif(n)
mu <- exp(1.2 + 2 * x1)
sigma <- 2.12 + 3 * x2
nu <- exp(0.2 - x3)
y <- rOW(n=n, mu, sigma, nu)

mod <- gamlss(y~x1, sigma.fo=~x2, nu.fo=~x3,
              family=OW(sigma.link="identity"),
              control=gamlss.control(n.cyc=300, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
coef(mod, what="nu")
```

---

param.startOW *Initial values extraction for Odd Weibull distribution*

Description

This function can be used to extract initial values found with empirical time on test transform (TTT) through `initValuesOW` function. This is used for parameter estimation in `OW` distribution.

Usage

```
param.startOW(param, initValOW)
```

Arguments

param	a character used to specify the parameter required. It can take the values "sigma" or "nu".
initValOW	an initValOW object generated with initValuesOW function.

Details

This function just gets initial values computed with initValuesOW for OW family. It must be called in sigma.start and nu.start arguments from gamlss function. This function is useful only if user want to set start values automatically with TTT plot. See example for an illustration.

Value

A length-one vector numeric value corresponding to the initial value of the parameter specified in param extracted from a initValuesOW object specified in the initValOW input argument.

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

Examples

```
# Random data generation (OW distributed)
y <- rOW(n=500, mu=0.05, sigma=0.6, nu=2)

# Initial values with TTT plot
iv <- initValuesOW(formula = y ~ 1)
summary(iv)

# This data is from unimodal hazard
# See TTT estimate from sample
plot(iv, legend_options=list(pos=1.03))

# See the true hazard
curve(hOW(x, mu=0.05, sigma=0.6, nu=2), to=100, lwd=3, ylab="h(x)")

# Finally, we fit the model
require(gamlss)
con.out <- gamlss.control(n.cyc = 300, trace = FALSE)
con.in <- glim.control(cyc = 300)

(sigma.start <- param.startOW("sigma", iv))
(nu.start <- param.startOW("nu", iv))

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, control=con.out, i.control=con.in,
              family=myOW_region(OW(sigma.link="identity", nu.link="identity"),
                                 valid.values="auto", iv),
              sigma.start=sigma.start, nu.start=nu.start)

# Estimates are close to actual values
(mu <- exp(coef(mod, what = "mu")))
```

```
(sigma <- coef(mod, what = "sigma"))
(nu <- coef(mod, what = "nu"))
```

PL *The Power Lindley family*

Description

Power Lindley distribution

Usage

```
PL(mu.link = "log", sigma.link = "log")
```

Arguments

`mu.link`	defines the mu.link, with "log" link as the default for the mu parameter.
`sigma.link`	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Power Lindley Distribution with parameters `mu` and `sigma` has density given by

$f(x) = \frac{\mu\sigma^2}{\sigma+1}(1+x^{\mu})x^{\mu-1}\exp(-\sigma x^{\mu})$,

for x > 0.

Value

Returns a gamlss.family object which can be used to fit a PL distribution in the `gamlss()` function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Ghitany, M. E., Al-Mutairi, D. K., Balakrishnan, N., & Al-Enezi, L. J. (2013). Power Lindley distribution and associated inference. Computational Statistics & Data Analysis, 64, 20-33.

See Also

dPL

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rPL(n=100, mu=1.5, sigma=0.2)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, family= 'PL',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod, 'mu'))
exp(coef(mod, 'sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(1.2 - 2 * x1)
sigma <- exp(0.8 - 3 * x2)
x <- rPL(n=n, mu, sigma)

mod <- gamlss(x~x1, sigma.fo=~x2, family=PL,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

QXGP *The Quasi XGamma Poisson family*

Description

The Quasi XGamma Poisson family

Usage

```
QXGP(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Quasi XGamma Poisson distribution with parameters mu, sigma and nu has density given by

$f(x) = K(\mu,\sigma,\nu)(\frac{\sigma^2 x^2}{2} + \mu)exp(\frac{\nu exp(-\sigma x)(1+\mu+\sigma x+\frac{\sigma^2 x^2}{2})}{1+\mu} - \sigma x)$,

for $x > 0$, $\mu > 0$, $\sigma > 0$, $\nu > 1$.

where

$K(\mu,\sigma,\nu) = \frac{\nu\sigma}{(exp(\nu)-1)(1+\mu)}$

Value

Returns a gamlss.family object which can be used to fit a QXGP distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Sen, S., Korkmaz, M. Ç., & Yousof, H. M. (2018). The quasi XGamma-Poisson distribution: properties and application. Istatistik Journal of The Turkish Statistical Association, 11(3), 65-76.

See Also

dQXGP

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rQXGP(n=200, mu=4, sigma=2, nu=3)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='QXGP',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 2000
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
```

```
mu <- exp(-2.19 + 3 * x1)
sigma <- exp(1 - 2 * x2)
nu <- 1
x <- rQXGP(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=QXGP,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

RW *The Reflected Weibull family*

Description

Reflected Weibull distribution

Usage

```
RW(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.

Details

The Reflected Weibull Distribution with parameters mu and sigma has density given by

$f(y) = \mu\sigma(-y)^{\sigma-1}e^{-\mu(-y)^{\sigma}}$,

for y < 0

Value

Returns a gamlss.family object which can be used to fit a RW distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Cohen, A. C. (1973). The reflected Weibull distribution. Technometrics, 15(4), 867-873.

See Also

dRW

Examples

```
# Example 1
# Generating some random values with
# known mu and sigma
y <- rRW(n=100, mu=1, sigma=1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, family= 'RW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu and sigma
# using the inverse link function
exp(coef(mod, 'mu'))
exp(coef(mod, 'sigma'))

# Example 2
# Generating random values under some model
n <- 200
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(1.5 - 1.5 * x1)
sigma <- exp(2 - 2 * x2)
x <- rRW(n=n, mu, sigma)

mod <- gamlss(x~x1, sigma.fo=~x2, family=RW,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
```

---

summary.initValOW *Summary of* initValOW *objects*

Description

This summary method displays initial values and search regions for OW family.

Usage

```
## S3 method for class 'initValOW'
summary(object, ...)
```

Arguments

object	an object of class initVal, generated with initValuesOW.
...	extra arguments

Value

No return value, it just prints out in the console the initial values and the search regions for $sigma$ and nu from OW distribution (see dOW).

Author(s)

Jaime Mosquera Gutiérrez <jmosquerag@unal.edu.co>

SZMW *The Sarhan and Zaindin's Modified Weibull family*

Description

The Sarhan and Zaindin's Modified Weibull distribution

Usage

```
SZMW(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Sarhan and Zaindin's Modified Weibull distribution with parameters mu, sigma and nu has density given by

$f(x) = (\mu + \sigma\nu x^{\nu-1}) \exp(-\mu x - \sigma x^{\nu})$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a SZMW distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Almalki, S. J., & Nadarajah, S. (2014). Modifications of the Weibull distribution: A review. Reliability Engineering & System Safety, 124, 32-55.

Sarhan, A. M., & Zaindin, M. (2009). Modified Weibull distribution. APPS. Applied Sciences, 11, 123-136.

See Also

dSZMW

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rSZMW(n=100, mu = 1, sigma = 1, nu = 1.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='SZMW',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n     <- 200
x1    <- runif(n)
x2    <- runif(n)
mu    <- exp(-1.6 * x1)
sigma <- exp(0.9 - 1 * x2)
nu    <- 1.5
x     <- rSZMW(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, mu.fo=~x1, sigma.fo=~x2, nu.fo=~1, family=SZMW,
              control=gamlss.control(n.cyc=50000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
coef(mod, what='nu')
```

WALD *The Wald family*

Description

The function WALD() defines the wALD distribution, two-parameter continuous distribution for a gamlss.family object to be used in GAMLSS fitting using the function gamlss().

Usage

```
WALD(mu.link = "log", sigma.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma parameter.

Details

The Wald distribution with parameters μ and $sigma$ has density given by

$$\mathrm{f}(x|\mu,\sigma) = \frac{\sigma}{\sqrt{2\pi x^3}} \exp\left[-\frac{(\sigma-\mu x)^2}{2x}\right], x > 0$$

Value

Returns a gamlss.family object which can be used to fit a WALD distribution in the gamlss() function.

Author(s)

Sofia Cuartas García, <scuartasg@unal.edu.co>

References

Heathcote, A. (2004). Fitting Wald and ex-Wald distributions to response time data: An example using functions for the S-PLUS package. Behavior Research Methods, Instruments, & Computers, 36, 678-694.

See Also

dWALD.

Examples

```
# Example 1
# Generating random values with
# known mu and sigma
require(gamlss)
mu <- 1.5
sigma <- 4.0

y <- rWALD(10000, mu, sigma)

mod1 <- gamlss(y~1, sigma.fo=~1,  family="WALD",
               control=gamlss.control(n.cyc=5000, trace=TRUE))

exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))

# Example 2
# Generating random values under some model

# A function to simulate a data set with Y ~ WALD
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(0.75 - 0.69 * x1)   # Approx 1.5
  sigma <- exp(0.5 - 0.64 * x2) # Approx 1.20
  y <- rWALD(n, mu, sigma)
  data.frame(y=y, x1=x1, x2=x2)
}

dat <- gendat(n=200)

mod2 <- gamlss(y~x1, sigma.fo=~x2, family=WALD, data=dat,
               control=gamlss.control(n.cyc=5000, trace=TRUE))

summary(mod2)
```

WG *The Weibull Geometric family*

Description

The Weibull Geometric distribution

Usage

```
WG(mu.link = "log", sigma.link = "log", nu.link = "logit")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The weibull geometric distribution with parameters mu, sigma and nu has density given by
$f(x) = (\sigma\mu^{\sigma}(1-\nu)x^(\sigma-1)\exp(-(\mu x)^{\sigma}))(1-\nu\exp(-(\mu x)^{\sigma}))^{-2}$,
for $x > 0$, $\mu > 0$, $\sigma > 0$ and $0 < \nu < 1$.

Value

Returns a gamlss.family object which can be used to fit a WG distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Barreto-Souza, W., de Morais, A. L., & Cordeiro, G. M. (2011). The Weibull-geometric distribution. Journal of Statistical Computation and Simulation, 81(5), 645-657.

See Also

dWG

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rWG(n=100,  mu = 0.9, sigma = 2, nu = 0.5)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='WG',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n     <- 200
```

```
x1    <- runif(n)
x2    <- runif(n)
mu    <- exp(- 0.2 * x1)
sigma <- exp(1.2 - 1 * x2)
nu    <- 0.5
x     <- rWG(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, mu.fo=~x1, sigma.fo=~x2, nu.fo=~1, family=WG,
              control=gamlss.control(n.cyc=50000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
coef(mod, what='nu')
```

WGEE *The Weigted Generalized Exponential-Exponential family*

Description

The Weigted Generalized Exponential-Exponential family

Usage

```
WGEE(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Weigted Generalized Exponential-Exponential distribution with parameters mu, sigma and nu has density given by

$f(x) = \sigma\nu \exp(-\nu x)(1-\exp(-\nu x))^{\sigma-1}(1-\exp(-\mu\nu x))/1-\sigma B(\mu+1,\sigma)$,

for $x > 0$, $\mu > 0$, $\sigma > 0$ and $\nu > 0$.

Value

Returns a gamlss.family object which can be used to fit a WGEE distribution in the gamlss() function.

Author(s)

Johan David Marin Benjumea, <johand.marin@udea.edu.co>

References

Mahdavi, A. (2015). Two weighted distributions generated by exponential distribution. Journal of Mathematical Extension, 9, 1-12.

See Also

dWGEE

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and  nu
y <- rWGEE(n=1000, mu = 5, sigma = 0.5, nu = 1)

# Fitting the model
require(gamlss)

mod <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family='WGEE',
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod, what='mu'))
exp(coef(mod, what='sigma'))
exp(coef(mod, what='nu'))

# Example 2
# Generating random values under some model
n <- 500
x1 <- runif(n, min=0.4, max=0.6)
x2 <- runif(n, min=0.4, max=0.6)
mu <- exp(2 - x1)
sigma <- exp(1 - 3*x2)
nu <- 1
x <- rWGEE(n=n, mu, sigma, nu)

mod <- gamlss(x~x1, sigma.fo=~x2, nu.fo=~1, family=WGEE,
              control=gamlss.control(n.cyc=50000, trace=FALSE))

coef(mod, what="mu")
coef(mod, what="sigma")
exp(coef(mod, what="nu"))
```

WP *The Weibull Poisson family*

Description

The Weibull Poisson family

Usage

```
WP(mu.link = "log", sigma.link = "log", nu.link = "log")
```

Arguments

mu.link	defines the mu.link, with "log" link as the default for the mu parameter.
sigma.link	defines the sigma.link, with "log" link as the default for the sigma.
nu.link	defines the nu.link, with "log" link as the default for the nu parameter.

Details

The Weibull Poisson distribution with parameters mu, sigma and nu has density given by

$f(x) = \frac{\mu\sigma\nu e^{-\nu}}{1-e^{-\nu}} x^{\mu-1} \exp(-\sigma x^{\mu} + \nu \exp(-\sigma x^{\mu}))$,

for $x > 0$.

Value

Returns a gamlss.family object which can be used to fit a WP distribution in the gamlss() function.

Author(s)

Amylkar Urrea Montoya, <amylkar.urrea@udea.edu.co>

References

Lu, Wanbo, and Daimin Shi. "A new compounding life distribution: the Weibull–Poisson distribution." Journal of applied statistics 39.1 (2012): 21-38.

See Also

dWP

Examples

```
# Example 1
# Generating some random values with
# known mu, sigma and nu
y <- rWP(n=3000, mu=1.5, sigma=0.5, nu=0.5)

# Fitting the model
require(gamlss)

mod1 <- gamlss(y~1, sigma.fo=~1, nu.fo=~1, family=WP,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

# Extracting the fitted values for mu, sigma and nu
# using the inverse link function
exp(coef(mod1, what="mu"))
exp(coef(mod1, what="sigma"))
```

```
exp(coef(mod1, what="nu"))

# Example 2
# Generating random values for a regression model

# A function to simulate a data set with Y ~ WP
gendat <- function(n) {
  x1 <- runif(n)
  x2 <- runif(n)
  mu <- exp(-1.3 + 3.1 * x1)
  sigma <- exp(0.9 - 3.2 * x2)
  nu <- 0.5
  y <- rWP(n=n, mu, sigma, nu)
  data.frame(y=y, x1=x1, x2)
}

set.seed(1234)
dat <- gendat(n=100)

# Fitting the model
mod2 <- NULL
mod2 <- gamlss(y~x1, sigma.fo=~x2, nu.fo=~1,
               family=WP, data=dat,
              control=gamlss.control(n.cyc=5000, trace=FALSE))

coef(mod2, what="mu")
coef(mod2, what="sigma")
exp(coef(mod2, what="nu"))
```

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